

1 On the relationship between the mesospheric sodium layer and the meteoric input function

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9

10 Abstract

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12 This study examines the relationship between the concentration of atmospheric sodium and its
13 Meteoric Input Function (MIF). We use the measurements from the Colorado State University (CSU)
14 Lidar and the Andes Lidar Observatory (ALO) with a new numerical model that includes sodium
15 chemistry in the mesosphere and lower thermosphere (MLT) region. The model is based on the
16 continuity equation to treat all sodium-bearing species and runs at a high temporal resolution. The
17 model simulation employs data assimilation to compare the MIF inferred from the meteor radiant
18 distribution and the MIF derived from the new sodium chemistry model. The simulation captures the
19 seasonal variability of sodium number density compared with lidar observations over the CSU site.
20 However, there were discrepancies for the ALO site, which is close to the South Atlantic Anomaly (SAA)
21 region, indicating it is challenging for the model to capture the observed sodium over ALO. The CSU site
22 had significantly more lidar observations (27,930 hours) than the ALO sites (1872 hours). The simulation
23 revealed that the uptake of the sodium species on meteoric smoke particles was a critical factor in
24 determining the sodium concentration in MLT, with the sodium removal rate by uptake found to be
25 approximately three times that of the NaHCO₃ dimerization. Overall, the study's findings provide
26 valuable information on the correlation between MIF and sodium concentration in the MLT region,
27 contributing to a better understanding of the complex dynamics in this region. This knowledge can
28 inform future research and guide the development of more accurate models to enhance our
29 comprehension of the MLT region's behavior.

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31 **Keywords:** Sodium layer, sodium chemistry, Meteor radiant distribution, Meteoroid input function

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33 Key points:

- 34 ● A high-time resolution, time-dependent Na chemistry model is developed.
- 35 ● Ablated global meteoroid material inputs inferred from ALO and CSU observations are about
36 $83 \pm 28 \text{ t d}^{-1}$ and $53 \pm 23 \text{ t d}^{-1}$, respectively.
- 37 ● The frequency of meteor occurrences might not provide a precise reflection of the mass of
38 meteoroid material input.

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41 1. Introduction

42 Micro-meteoroids enter the Earth's atmosphere day and night, depositing their constituents into the
43 atmosphere via ablation, creating a region that hosts various metal species, for example, Fe, K, Si, Mg,
44 Ca, and Na, in both neutral and ion form (Plane et al., 2015; Plane et al., 2021; and references therein).
45 The region is commonly referred to as the mesosphere and lower thermosphere (MLT), located between
46 75 and 110 km altitude. The metal layers in the MLT often serve as the tracers that facilitate the
47 investigation of the dynamical and chemical processes within the region (Takahashi et al., 2014; Qiu et
48 al., 2021). Quantitative measurements of metal atoms have been made since the 1950s (Hunten, 1967)
49 through a variety of ground or space-borne technologies (Koch et al., 2021; Koch et al., 2022). The large
50 resonant scattering cross-section (Bowman et al., 1969) and the substantial presence of the sodium
51 atom in the MLT make it one of the most researched metal layers in the atmosphere (Yu et al., 2022).

52 The sodium layer is usually studied via observations carried out by resonance lidars, satellites, and
53 through Na D-line emission at 589.0nm and 589.6nm (Plane, 2010; Plane et al., 2012; Hedin and
54 Gumbel, 2011; Langowski et al., 2017; Andrioli et al., 2019; Li et al., 2020a). The sodium vertical profiles
55 retrieved by lidars have been commonly used as a tracer to study atmospheric dynamics, e.g., gravity
56 waves, wind shear, etc. The long-term seasonal and short-term diurnal variability of metallic species
57 have been investigated by several studies (Feng et al., 2013; Marsh et al., 2013; Cai et al., 2019a, b; Yu et
58 al., 2022). A typical sodium chemistry scheme consists of neutral chemistry, ion chemistry, and
59 photolysis. The sodium chemistry research in recent years has primarily been based on the sodium
60 chemistry model by Plane (2004), which has been cited in various subsequent works, including Bag et al.
61 (2015) and references therein.

62 As meteoroids are the primary source of metal layers in the atmosphere, including the sodium layer,
63 the Meteoroid Input Function (MIF) plays a crucial role in the modeling of metallic layers in the
64 atmosphere. The MIF is a function designed to model the temporal and spatial variability of the
65 meteoroid on the atmosphere (Pifko et al., 2013). Sporadic meteors are estimated to make up more
66 than 95% of the total meteoroid population by comparing the number of meteors originating in sporadic
67 sources to those originating in known shower meteor sources (Chau and Galindo, 2008). This highlights
68 the importance of incorporating sporadic meteor data in the MIF to accurately understand sodium
69 concentration in the mesosphere and lower thermosphere (MLT) region and its correlation with
70 meteoroid material input. It is well established that there are six apparent sources of sporadic meteors,
71 namely North and South Apex (NA and SA); North and South Toroidal (NT and ST); and Helion and Anti-
72 Helion sources (H and AH) (Campbell-Brown, 2008; Kero et al., 2012; Li et al., 2022). However, the
73 relative strength of these meteor radiant sources varies among the studies. For example, the NA and SA
74 sources are found to be much stronger than other sources in results obtained with High Power Large
75 Aperture (HPLA) radars (Chau et al., 2007; Kero et al., 2012; Li and Zhou, 2019), while specular meteor
76 radars found the difference to be much smaller (Campbell-Brown and Jones, 2005; Campbell-Brown,
77 2008). The detection sensitivity varies significantly among different facilities. For instance, the Arecibo
78 Observatory (AO) at 18° N, 66° W detects approximately 20 times more meteors per unit area per unit
79 time than the Jicamarca Radio Observatory (JRO) at 12° S, 77° W, and at least 800 times more meteors
80 than the Resolute Bay Incoherent Scatter North (RISR-N) radar at 75° N, 95° W, despite all being HPLA
81 facilities (Li et al., 2020, 2023a; Hedges et al., 2022). While meteor flux does exhibit variations based on
82 time and latitude, these fluctuations alone cannot explain the magnitude of the observed difference.

83 Consequently, the total mass of the meteors that enter the Earth's atmosphere is subject to significant
84 uncertainties. In the existing Whole Atmosphere Community Climate Model-Na (WACCM-Na) global
85 sodium model (Dunker et al., 2015), the meteor input function was modeled by placing a flux curve on
86 each radiant meteor source with a definite ratio (more details can be found in Marsh et al., 2013). The
87 flux curve model is based on observations carried out exclusively by the Arecibo Observatory. Although
88 the model can reproduce some of the flux characteristics of the meteors observed at Arecibo, it is a
89 relatively simple model and therefore has several limitations (Li et al., 2022). One of the limitations is
90 that the model cannot reproduce the velocity distribution of the meteors in observations.

91 This study introduces a new numerical model for sodium chemistry that utilizes the continuity equations
92 for all Na-related reactions without steady-state approximations. The main objective is to investigate the
93 relationship between the apparent sodium concentration and the Meteoroid Input Function (MIF) in the
94 MLT region. We then compare the results of the new model with measurements from two lidar
95 instruments, namely the Colorado State University (CSU) and the Andes Lidar Observatory (ALO).
96 Furthermore, we compared the MIF derived from the new sodium chemistry model and lidar
97 measurements from CSU and ALO, against the results of the high-resolution meteor radiant distribution
98 recently deduced from observations conducted at AO. Finally, we discuss the implications of these
99 comparisons and suggest possible explanations for the observed discrepancy between the MIF derived
100 from radar and those obtained from lidar observations.

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102 **2. The sodium chemistry model (NaChem)**

103 **2.1 Sodium chemistry**

104 Numerical airglow models have been extensively used to investigate atmospheric airglow chemistry and
105 gravity waves (Huang and Hickey, 2008; Huang and Richard, 2014; Huang, 2015). A new numerical
106 sodium chemistry model, hereafter referred to as NaChem, was developed for this study. Table 1 lists
107 the complete reactions and their corresponding rate coefficients used in NaChem, which includes
108 neutral chemistry, ion chemistry, and photochemistry. The dimerization reaction of NaHCO_3 (reaction 25
109 in Table 1) is the outlet that removes Na atoms in the chemistry scheme. The Na atoms can also be
110 removed by the uptake of sodium species onto meteoric smoke particles (Hunten et al., 1980;
111 Kalashnikova et al., 2000; Plane, 2004), a process that can be turned on or off in the model. This study
112 estimates the MIF in the numerical model by matching the amount of sodium atoms removed by the
113 dimerization reaction and uptake, i.e., sodium sink, to maintain the observed sodium presence in the
114 MLT. Throughout the rest of the paper, the MIF estimated from the sodium chemistry numerical model
115 will be referred to as MIF(s). On the other hand, the MIF derived from meteor radiant distribution will
116 be referred to as MIF(m). MIF is a function of time and latitude, representing the mass of meteoroid
117 material entering Earth's atmosphere. The MIF(m) is determined through a 3-D meteoroid orbital
118 simulation, a process similar to the seeding process discussed in section 3.1 of Li et al. (2022), based on
119 the meteor radiant distribution. MIF(m) is a relative unitless quantity. Note that the meteor mass cannot
120 be accurately determined via radar measurements, however, the seasonal variation of meteoroid
121 material input can be represented by MIF(m). The estimation of meteor mass is further discussed in
122 Section 5. In contrast, MIF(s) is expressed in units of $1/\text{cm}^3/\text{second}$.

123 The numerical model utilizes the continuity equation to track the time evolution of all 14 Na-related
124 species. Table 2 presents a comprehensive list of these species, along with their corresponding
125 production and loss rates. The background major gas species, including O₃, O₂, O, H, H₂, H₂O, etc., and
126 the temperature are provided by WACCM version 6 (Jiao et al., 2022). Here we use the dynamic version
127 of WACCM nudged with NASA's Modern Era Retrospective Analysis for Research and Application
128 MERRA2 reanalysis data set (Hunziker & Wendt, 1974; Molod et al., 2015; Gettelman et al., 2019). The
129 WACCM reference profiles are linearly interpolated to a resolution of one minute and updated every
130 minute during the simulation. It is worth noting that the Na-related reactions, which are illustrated in
131 Table 2, do not significantly impact the background gas species, as the effect is orders of magnitude
132 smaller than the variation of the major gas species themselves. Therefore, the major gas species are
133 simulated independently of Na-related reactions.

134 2.2 Numerical scheme

135 As discussed earlier, it is worth noting that the reactions of sodium chemistry in NaChem share
136 similarities with those in previous models (e.g., Plane et al., 2015 and references therein); however, the
137 implementation of the numerical chemistry scheme differs. NaChem uses continuity equations to treat
138 all chemicals involved, including short-lived intermediate species. Treating all species with the continuity
139 equation is a more straightforward yet accurate approach than using steady-state approximations.
140 Moreover, by treating all species in a uniform procedure, the numerical model is more compact and
141 easier to interpret. The computational capability of a personal computer nowadays has advanced
142 enough to process an ultra-fine time step (microseconds) that is necessary for numerical simulations of
143 short-lived species in a reasonable duration. Still, the differential equations for production and loss of
144 short-lived species can be numerically unstable unless microsecond or even sub-microsecond time step
145 is used (Higham, 2002). The concern of the differential equation instability can be largely mitigated by a
146 first-order exponential integrator (Hochbruck and Ostermann, 2010), i.e.,

$$147 \quad c = x_0 - \frac{a_0}{b_0}$$
$$148 \quad x_1 = \frac{a_0}{b_0} + ce^{-b_0\Delta t} \quad (1)$$

149 Where x_0 is the value of the current step. In the simulation, it is the number density of the species. a_0 is
150 the production of the species, b_0 is the loss of the species, Δt is the step size in time, and x_1 is the value
151 of the next step.

152 The exponential integrator, as expressed in Equation (1), is the solution to the continuity equation.
153 Notably, reaction 25 listed in Table 1 is an exception, which was carried out using explicit Euler
154 integrator in the simulation. This reaction's continuity equation is structured differently from the others
155 because it represents the only mechanism for removing Na atoms from the chemistry simulation, apart
156 from the uptakes of sodium species. Our testing indicates that both the exponential integrator and
157 explicit Euler integrator yield nearly identical results. However, for numerical stability, the explicit Euler
158 integrator requires a step size of $\sim 1\mu\text{s}$, which is orders of magnitude smaller than the exponential
159 integrator. The default time step of NaChem is 0.1 seconds with the exponential integrator.

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Table 1. Reactions in NaChem. f_a and f_x are branching ratios.

	Reaction	Rate Coefficient	reference
neutral chemistry			
1	$\text{Na} + \text{O}_3 \rightarrow \text{NaO(A)} + \text{O}_2$	$K_1 = 1.1 \times 10^{-9} \exp(-116/T)$	1
2	$\text{NaO(A)} + \text{O} \rightarrow \text{Na}^{(2)\text{P}} + \text{O}_2$	$K_2 = 2.2 \times 10^{-10} (T/200)^{0.5}$, $f_A = 0.14 \pm 0.4$	1,3
3	$\text{NaO(A)} + \text{O} \rightarrow \text{Na}^{(2)\text{S}} + \text{O}_2$	$K_3 = 2.2 \times 10^{-10} (T/200)^{0.5}$, $(1-f_A)$	1,3
4	$\text{NaO(A)} + \text{O}_2 \rightarrow \text{NaO(X)} + \text{O}_2$	$K_4 = 1 \times 10^{-11}$	1
5	$\text{Na} + \text{O}_2 + \text{M} \rightarrow \text{NaO}_2 + \text{M}$	$K_5 = 5.0 \times 10^{-30} (200/T)^{1.22}$	1
6	$\text{NaO}_2 + \text{O} \rightarrow \text{NaO(X)} + \text{O}_2$	$K_6 = 5 \times 10^{-10} \exp(-940/T)$	1
7	$\text{NaO(X)} + \text{O} \rightarrow \text{Na}^{(2)\text{P}} + \text{O}_2$	$K_7 = 2.2 \times 10^{-10} (T/200)^{0.5}$, $f_x = 0.167$	1,2
8	$\text{NaO(X)} + \text{O} \rightarrow \text{Na}^{(2)\text{S}} + \text{O}_2$	$k_8 = 2.2 \times 10^{-10} (T/200)^{0.5}$, $(1-f_x)$	1,2
9	$\text{NaO(X)} + \text{O}_3 \rightarrow \text{NaO}_2 + \text{O}_2$	$k_9 = 1.1 \times 10^{-9} \exp(-568/T)$	1
10	$\text{NaO(X)} + \text{O}_3 \rightarrow \text{Na} + 2\text{O}_2$	$k_{10} = 3.2 \times 10^{-10} \exp(-550/T)$	1
11	$\text{NaO(X)} + \text{O}_2 + \text{M} \rightarrow \text{NaO}_3 + \text{M}$	$k_{11} = 5.3 \times 10^{-30} (200/T)$	1
12	$\text{NaO(X)} + \text{H} \rightarrow \text{Na} + \text{OH}$	$k_{12} = 4.4 \times 10^{-10} \exp(-668/T)$	1
13	$\text{NaO(X)} + \text{H}_2 \rightarrow \text{NaOH} + \text{H}$	$k_{13} = 1.1 \times 10^{-9} \exp(-1100/T)$	1
14	$\text{NaO(X)} + \text{H}_2 \rightarrow \text{Na} + \text{H}_2\text{O}$	$k_{14} = 1.1 \times 10^{-9} \exp(-1400/T)$	1
15	$\text{NaO(X)} + \text{H}_2\text{O} \rightarrow \text{NaOH} + \text{OH}$	$k_{15} = 4.4 \times 10^{-10} \exp(-507/T)$	1
16	$\text{NaO(X)} + \text{CO}_2 + \text{M} \rightarrow \text{NaCO}_3 + \text{M}$	$K_{16} = 1.3 \times 10^{-27} (200/T)$	1
17	$\text{NaO}_2 + \text{H} \rightarrow \text{Na} + \text{HO}_2$	$K_{17} = 1.0 \times 10^{-9} \exp(-1000/T)$	1
18	$\text{NaO}_3 + \text{O} \rightarrow \text{Na} + 2\text{O}_2$	$k_{18} = 2.5 \times 10^{-10} (T/200)^{0.5}$	1
19	$\text{NaCO}_3 + \text{O} \rightarrow \text{NaO}_2 + \text{CO}_2$	$k_{19} = 5.0 \times 10^{-10} \exp(-1200/T)$	1
20	$\text{NaCO}_3 + \text{H} \rightarrow \text{NaOH} + \text{CO}_2$	$k_{20} = 1.0 \times 10^{-9} \exp(-1400/T)$	1
21	$\text{NaOH} + \text{H} \rightarrow \text{Na} + \text{H}_2\text{O}$	$k_{21} = 4.0 \times 10^{-11} \exp(-550/T)$	1
22	$\text{NaOH} + \text{CO}_2 + \text{M} \rightarrow \text{NaHCO}_3 + \text{M}$	$k_{22} = 1.9 \times 10^{-28} (200/T)^1$	1
23	$\text{NaHCO}_3 + \text{H} \rightarrow \text{Na} + \text{H}_2\text{O} + \text{CO}_2$	$k_{23} = 1.1 \times 10^{-11} \exp(-910/T)$	1
24	$\text{NaHCO}_3 + \text{H} \rightarrow \text{Na} + \text{H}_2\text{CO}_3$	$k_{24} = 1.84 \times 10^{-13} T^{0.777} \exp(-1014/T)$	1
25	$2\text{NaHCO}_3 + \text{M} \rightarrow (\text{NaHCO}_3)_2 + \text{M}$	$k_{25} = 8.8 \times 10^{-10} \exp(T/200)^{-0.23}$	1
26	$\text{Na}^{(2)\text{P}} \rightarrow \text{Na}^{(2)\text{S}} + h\nu(589.0-589.6 \text{ nm})$	$K_{26} = 6.26 \times 10^7$	1
ion-molecule chemistry			
27	$\text{Na} + \text{O}_2^+ \rightarrow \text{Na}^+ + \text{O}_2$	$K_{27} = 2.7 \times 10^{-9}$	1
28	$\text{Na} + \text{NO}^+ \rightarrow \text{Na}^+ + \text{NO}$	$K_{28} = 8.0 \times 10^{-10}$	1
29	$\text{Na}^+ + \text{N}_2 + \text{M} \rightarrow \text{NaN}_2^+ + \text{M}$	$k_{29} = 4.8 \times 10^{-30} (T/200)^{-2.2}$	1
30	$\text{Na}^+ + \text{CO}_2 + \text{M} \rightarrow \text{NaCO}_2^+ + \text{M}$	$k_{30} = 3.7 \times 10^{-29} (T/200)^{-2.9}$	1
31	$\text{NaN}_2^+ + \text{O} \rightarrow \text{NaO}^+ + \text{N}_2$	$k_{31} = 4.0 \times 10^{-10}$	1
32	$\text{NaO}^+ + \text{N}_2 \rightarrow \text{NaN}_2^+ + \text{O}$	$k_{32} = 1.0 \times 10^{-12}$	1
33	$\text{NaO}^+ + \text{O} \rightarrow \text{Na}^+ + \text{O}_2$	$k_{33} = 1.0 \times 10^{-11}$	1
34	$\text{NaO}^+ + \text{O}_2 \rightarrow \text{Na}^+ + \text{O}_3$	$k_{34} = 5.0 \times 10^{-12}$	1
35	$\text{NaN}_2^+ + \text{X} \rightarrow \text{NaX}^+ + \text{N}_2$ ($\text{X}=\text{CO}_2, \text{H}_2\text{O}$)	$k_{35} = 6.0 \times 10^{-10}$	1
36	$\text{NaY}^+ + \text{e} \rightarrow \text{Na} + \text{Y}$ ($\text{Y}=\text{N}_2, \text{CO}_2, \text{H}_2\text{O}, \text{O}$)	$k_{36} = 1.0 \times 10^{-6} (T/200)^{-0.5}$	1
photochemical reactions			
37	$\text{NaO(A)}/\text{NaO(X)} + h\nu \rightarrow \text{Na} + \text{O}$	$K_{37} = 5.5 \times 10^{-2}$	1

38	$\text{NaO}_2 + \text{h}\nu \rightarrow \text{Na} + \text{O}_2$	$K_{38} = 1.9 \times 10^{-2}$	1
39	$\text{NaOH} + \text{h}\nu \rightarrow \text{Na} + \text{OH}$	$K_{39} = 1.8 \times 10^{-2}$	1
40	$\text{NaHCO}_3 + \text{h}\nu \rightarrow \text{Na} + \text{HCO}_3$	$K_{40} = 1.3 \times 10^{-4}$	1
41	$\text{Na} + \text{h}\nu \rightarrow \text{Na}^+ + \text{e}^-$	$K_{41} = 2 \times 10^{-5}$	1

167 *1:Plane (2004), 2: Plane (2012), 3: Griffin et al. (2001). Units: $1/\text{cm}^3/\text{s}$

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169 Table 2. The production and loss terms of the sodium-related species.

	Species	Prod	Loss
a1	$\text{Na}(^2\text{P})$	$k_2[\text{a}_3][\text{O}] + k_7[\text{a}_5][\text{O}];$	1^*
a2	Na	$k_3[\text{a}_3][\text{O}] + k_8[\text{a}_5][\text{O}] + k_{10}[\text{a}_5][\text{O}_3] + k_{12}[\text{a}_5][\text{H}] + k_{14}[\text{a}_5][\text{H}_2] + k_{17}[\text{a}_4][\text{H}] + k_{18}[\text{a}_6][\text{O}] + k_{21}[\text{a}_7][\text{H}] + k_{23}[\text{a}_9][\text{H}] + k_{24}[\text{a}_9][\text{H}] + k_{36}[\text{a}_{11}][\text{e}] + k_{36}[\text{a}_{13}][\text{e}] + k_{36}[\text{a}_{12}][\text{e}] + k_{36}[\text{a}_{14}][\text{e}] + [\text{a}_1] + k_{37}[\text{a}_3][\text{h}\nu] + k_{37}[\text{a}_5][\text{h}\nu] + k_{38}[\text{h}\nu][\text{a}_4] + k_{39}[\text{h}\nu][\text{a}_7] + k_{40}[\text{h}\nu][\text{a}_9];$	$k_1[\text{O}_3] + k_5[\text{O}_3] + k_5[\text{O}_2][\text{M}] + k_{27}[\text{O}_2^+] + k_{28}[\text{NO}^+] + k_{41}[\text{h}\nu];$
a3	$\text{NaO}(\text{A})$	$k_1[\text{a}_2][\text{O}_3]$	$k_2[\text{O}] + k_3[\text{O}] + k_4[\text{O}_2] + k_{37}[\text{h}\nu]$
a4	NaO_2	$k_5[\text{a}_2][\text{O}_2][\text{M}] + k_9[\text{a}_5][\text{O}_3] + k_{19}[\text{a}_8][\text{O}]$	$k_6[\text{O}] + k_{17}[\text{H}] + k_{38}[\text{h}\nu]$
a5	$\text{NaO}(\text{X})$	$k_5[\text{a}][\text{O}_3] + k_4[\text{a}_3][\text{O}_2] + k_6[\text{a}_4][\text{O}]$	$k_7[\text{O}] + k_8[\text{O}] + k_9[\text{O}_3] + k_{10}[\text{O}_3] + k_{11}[\text{O}_2][\text{M}] + k_{12}[\text{H}] + k_{13}[\text{H}_2] + k_{14}[\text{H}_2] + k_{15}[\text{H}_2\text{O}] + k_{16}[\text{CO}_2][\text{M}] + k_{37}[\text{h}\nu]$
a6	NaO_3	$k_{11}[\text{a}_5][\text{O}_2][\text{M}]$	$k_{18}[\text{O}]$
a7	NaOH	$k_{13}[\text{a}_5][\text{H}_2] + k_{15}[\text{a}_5][\text{H}_2\text{O}] + k_{20}[\text{a}_8][\text{H}]$	$k_{21}[\text{H}] + k_{22}[\text{CO}_2][\text{M}] + k_{39}[\text{h}\nu]$
a8	NaCO_3	$k_{16}[\text{a}_5][\text{CO}][\text{M}]$	$k_{19}[\text{O}] + k_{20}[\text{H}]$
a9	NaHCO_3	$k_{22}[\text{a}_7][\text{CO}_2][\text{M}]$	$k_{23}[\text{H}] + k_{24}[\text{H}] + 2k_{25}[\text{a}_9][\text{M}] + k_{40}[\text{h}\nu]$
a10	Na^+	$k_{27}[\text{a}_2][\text{O}_2^+] + k_{28}[\text{a}_2][\text{NO}^+] + k_{33}[\text{a}_{13}][\text{O}] + k_{34}[\text{a}_{13}][\text{O}_2] + k_{41}[\text{h}\nu][\text{a}_2]$	$k_{29}[\text{N}_2][\text{M}] + k_{30}[\text{CO}_2][\text{M}]$
a11	NaN_2^+	$k_{29}[\text{a}_{10}][\text{N}_2][\text{M}] + k_{32}[\text{a}_{13}][\text{N}_2]$	$k_{31}[\text{O}] + k_{35}[\text{CO}_2] + k_{35}[\text{H}_2\text{O}] + k_{36}[\text{e}]$
a12	NaCO_2^+	$k_{30}[\text{a}_{10}][\text{CO}_2][\text{M}] + k_{35}[\text{a}_{11}][\text{CO}_2]$	$k_{36}[\text{e}]$
a13	NaO^+	$k_{31}[\text{a}_{11}][\text{O}]$	$k_{32}[\text{N}_2] + k_{33}[\text{O}] + k_{34}[\text{O}_2] + k_{36}[\text{e}]$
a14	NaH_2O^+	$k_{35}[\text{a}_{11}][\text{H}_2\text{O}]$	$k_{36}[\text{e}]$

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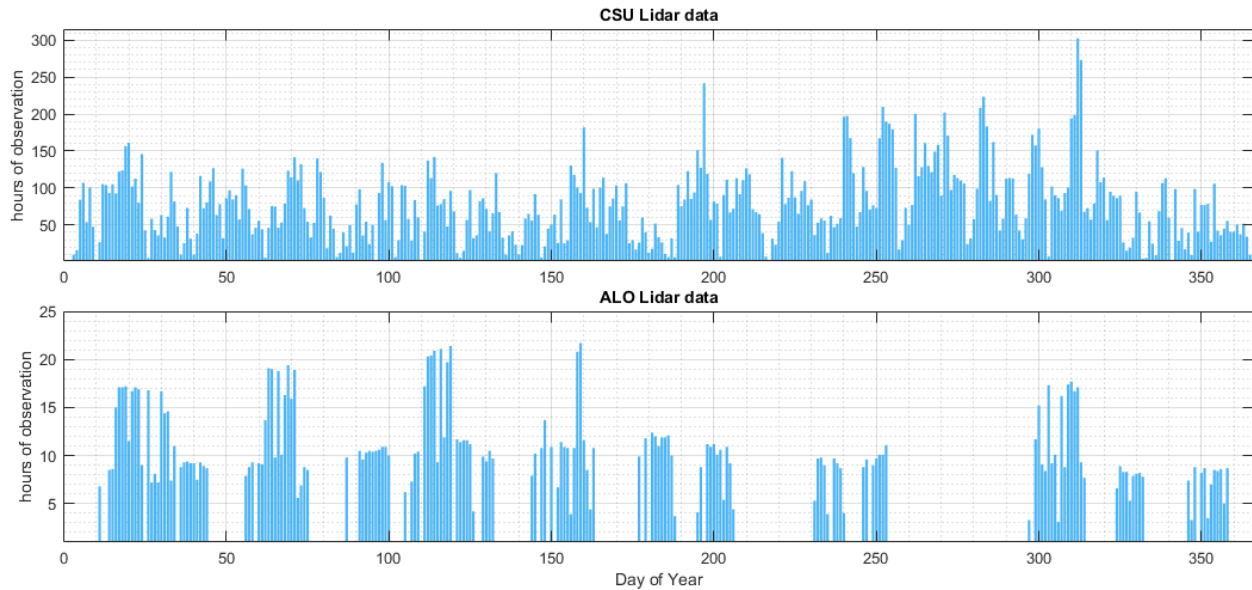
171 *In Species 1, as of the current state of the model, all $\text{Na}(^2\text{p})$ atoms return to their ground state
172 immediately, so the loss term is set to 1. The $[\text{h}\nu]$ is the term that represents loss via photoionization,
173 which is approximately a sinusoidal function based on the solar zenith angle of the respective local solar
174 time.

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176 3. CSU and ALO Sodium Lidar Observations and data processing

177 3.1 Observations

178 Several aspects of the current research, i.e., the presence of sodium in the MLT, require cross-validation
179 with the measurements. One primary objective of the present model is to match the observed seasonal
180 variation of the sodium layer. Measurements by the Colorado State University (CSU, 41.4°N, 111.5°W)
181 Lidar, also known as Utah State University (USU) Lidar, and the lidar data acquired by the Andes Lidar
182 Observatory (ALO, 30.3°S, 70.7°W), are used to facilitate the research in the current study. We are
183 unable to acquire more ALO data after 2019 as the COVID situation disrupted the site operation. The
184 CSU data comprises 27,930 hours of lidar observations between 1990 and 2020, whereas the ALO data
185 consists of 1872 hours between 2014 and 2019.



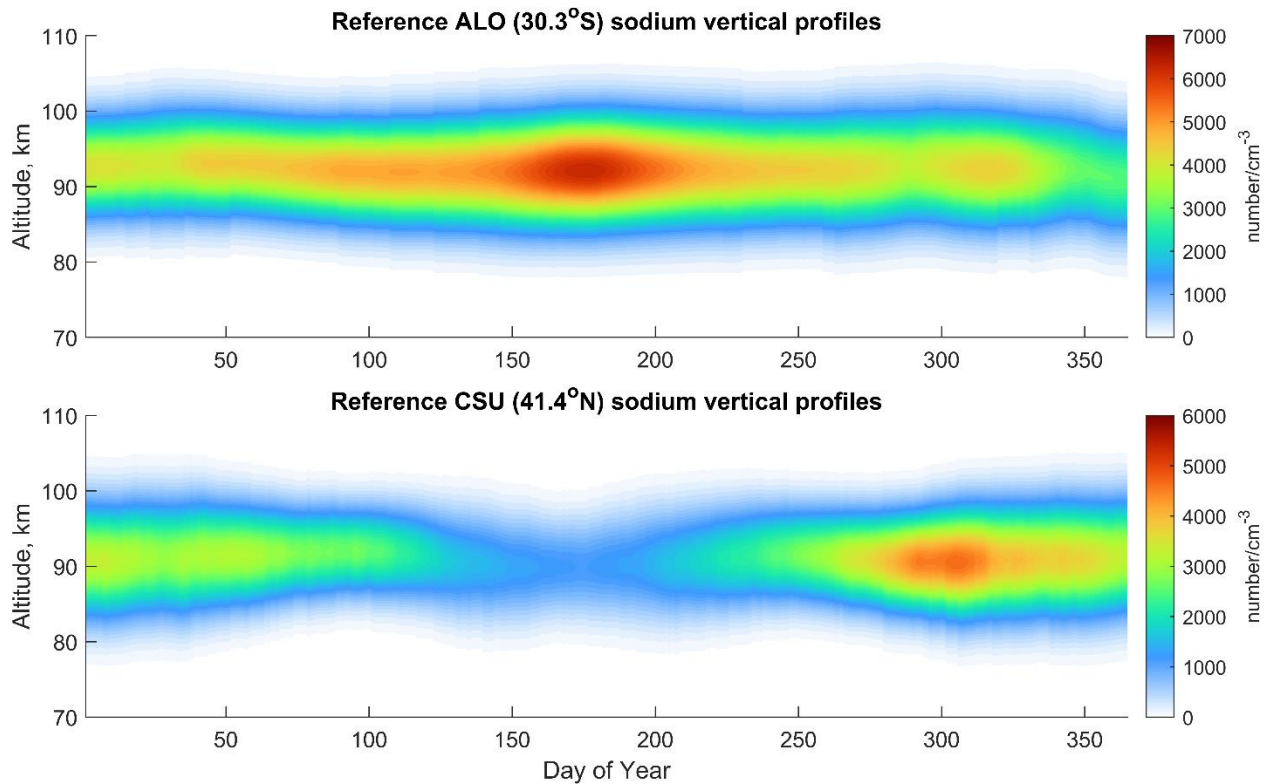
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187 **Figure 1.** Available hours of lidar observations. CSU lidar (1990-2020, upper plot) and ALO lidar (2014-
 188 2019, lower plot).

189 The statistics of CSU and ALO available data are presented in Figure 1. The Lidar observations of both
 190 sites consist of nocturnal observations only, and a typical nocturnal observation lasts between 8 and 11
 191 hours. Note that in Figure 1, there could be as many as 300 hours of sodium observations on a single day
 192 of year, which means the data of the date comprise observations of many years on that day in different
 193 years. The CSU data almost covered every day of the year with only a few exceptions, whereas the ALO
 194 data was much more sparse. As a result, due to the significantly larger number of CSU observations, the
 195 statistical reliability of the seasonal variation in the sodium layer derived from ALO observations may not
 196 be as strong as that of the CSU data. As depicted in Figure 2, the overall seasonal trend of the sodium
 197 vertical profile derived from CSU lidar observations closely aligns with the simulation-based estimate by
 198 Marsh et al. (2013). In contrast, ALO lidar observations deviate from the findings reported by Marsh et
 199 al. (2013). The ALO measurements exhibit a prominent peak around June, while the results in Marsh et
 200 al. (2013) show a double peak in March and October.

201 **3.2 Data processing**

202 The sodium layer in atmospheric observations is often affected by perturbations of atmospheric
 203 dynamics, which is why sodium is commonly used as a tracer in the study of the MLT dynamics (Plane et
 204 al., 2015). However, studying the sodium layer itself can be complicated due to the underlying chemical
 205 processes coupled with the dynamics. In order to mitigate the effects of atmospheric dynamics, we
 206 process the sodium vertical profiles from observations in three steps. First, we average the profiles by
 207 day of the year, meaning we take the average of the data from the same day of the year from different
 208 years. Missing data are treated using linear interpolation. Next, we smooth the averaged profiles using a
 209 15-day running average. Finally, the height profile for each time step is further smoothed by fitting it
 210 with a skew-normal distribution (Azzalini & Valle, 1996), using the least squares error method.



211

212 **Figure 2.** The reference annual sodium vertical profiles at ALO (top plot) and at CSU (bottom plot). The
 213 reference profiles are the averages throughout all the available data on the same days at the respective
 214 site, then fitted by a skew-normal distribution that mitigates atmospheric dynamics. In essence, the
 215 reference profiles are measurements with small-scale dynamics removed via steps discussed in section
 216 3.2.

217

218 Figure 2 displays the processed annual sodium vertical profiles from the lidar measurements, referred to
 219 as reference profiles hereafter. These profiles serve as references to guide the numerical simulation of
 220 the NaChem model. The reference profiles are Na lidar measurements fitted using a skew-normal
 221 distribution, smoothed by a 15-day running average, and processed through linear 2-D interpolation
 222 across time and altitude. The lidar measurements have an altitude resolution of 500m for ALO and from
 223 75m to 140m for CSU. These measurements are interpolated to a 100m resolution as inputs to the
 224 NaChem model. The time resolutions of the lidar measurements typically vary between 1 and 10
 225 minutes, depending on the experiment, and are linearly interpolated to 0.1 seconds. The reference
 226 profiles inherently include diffusion and other dynamic effects on the sodium species in the MLT, as
 227 these observational data represent snapshots of sodium diffusion at various times. By constantly
 228 matching the observed Na profile to the simulated Na profile, the diffusion is included implicitly in the
 229 model. The seasonal column densities of both ALO and CSU profiles is similar to a sinusoidal function,
 230 with ALO data peaking near June and CSU data peaking in November. The centroid height of the sodium
 231 layer is higher in the ALO data than in the CSU data.

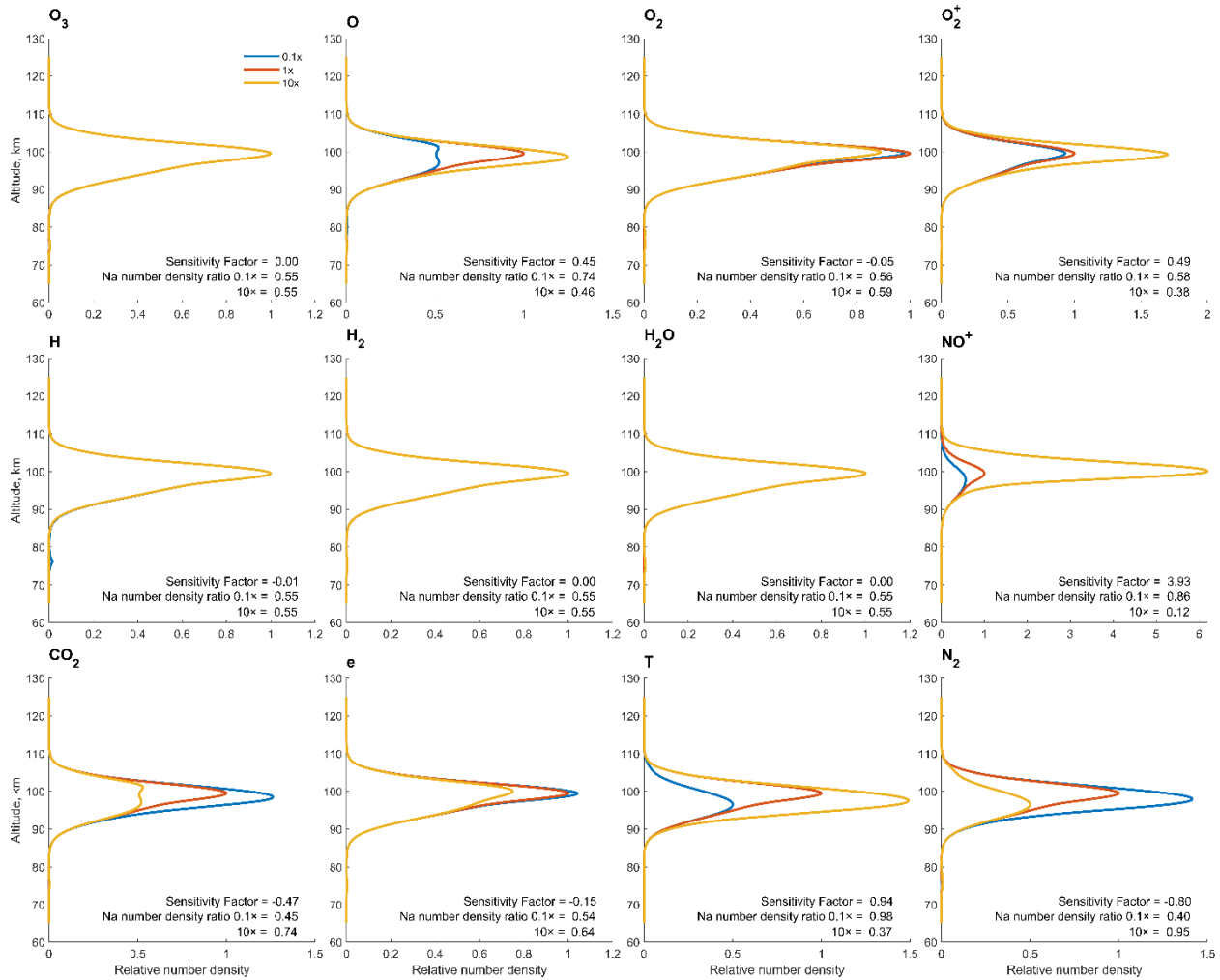
232

233 **4. Results**

234 **4.1 Sensitivity test**

235 Sodium in the atmosphere could manifest in many forms, i.e., in sodium-bearing neutral chemicals and
236 ionic chemicals. The sodium number densities are typically obtained via lidar measurements. Given the
237 complexity of the sodium chemistry, the observed sodium is merely a subset, possibly not even a major
238 constituent, of the total number of all the sodium-bearing species in the atmosphere. The total sodium
239 content is defined as the total number of sodium atoms in all 14 sodium-bearing species, as listed in
240 Table 2. In summary, the sodium that we can detect does not necessarily provide an accurate
241 representation of the total sodium content or the overall count of sodium-bearing species, as
242 unobservable species such as Na^+ and NaHCO_3 could constitute a substantial portion of the total sodium
243 content.

244 Understanding the impact of each background species, i.e., species listed in Figure 3., on the total
245 sodium content is essential to study the underlying mechanism of the chemical reactions. Therefore, we
246 present a sensitivity test by isolating variables. The sensitivity test is done by altering the number
247 density of background species in question by two orders of magnitude, i.e., with a factor of 0.1 and 10,
248 while keeping the number densities of other background species and the atomic sodium fixed. The
249 simulation is kept running until all the numbers are stable. The diurnal variations of the sodium and
250 background species are not considered in sensitivity test as they introduce unnecessary complexity. The
251 results of the sensitivity test of the 11 background species and temperatures involved in the numerical
252 simulation are shown in Figure 3. Each panel contains three lines, where the red curve shows the
253 unaltered vertical profile of the total sodium content. The results of the species altered by the factor of
254 0.1 and 10 are shown in light blue and yellow, respectively.



255

256 **Figure 3.** Sensitivity test of 11 background species and temperature on Na chemistry. The total sodium
 257 content vertical profile for the respective background species altered by 10x and 0.1x are shown in yellow
 258 and light blue. The reference sodium content vertical profiles are shown in red. Additionally, the
 259 sensitivity factor and the Na number density ratio to the concentration of all sodium species are
 260 presented on each panel.

261

262 In Figure 3, only the yellow curve is visible in some of the panels because the three curves are drawn on
 263 top of each other, indicating that the change of the respective background species bears little to no
 264 effect on the sodium chemistry. A sensitivity factor is defined to better quantify the weight of each
 265 background species in sodium chemistry. The factor is calculated by the following equation:

266

$$\text{Sensitivity Factor} = \frac{NaT_c^{10} - NaT_c^{0.1}}{NaT_c} \quad (2)$$

267 Where NaT_c^{10} is the column density of the total sodium content with the respective species altered by a
 268 factor of 10, and $NaT_c^{0.1}$ is the same operation as the previous one but altered by a factor of 0.1. The
 269 denominator, NaT_c , is the column density of the reference profile. The sensitivity factor provides a
 270 general insight into how variations in the background species correlate with sodium number density. A

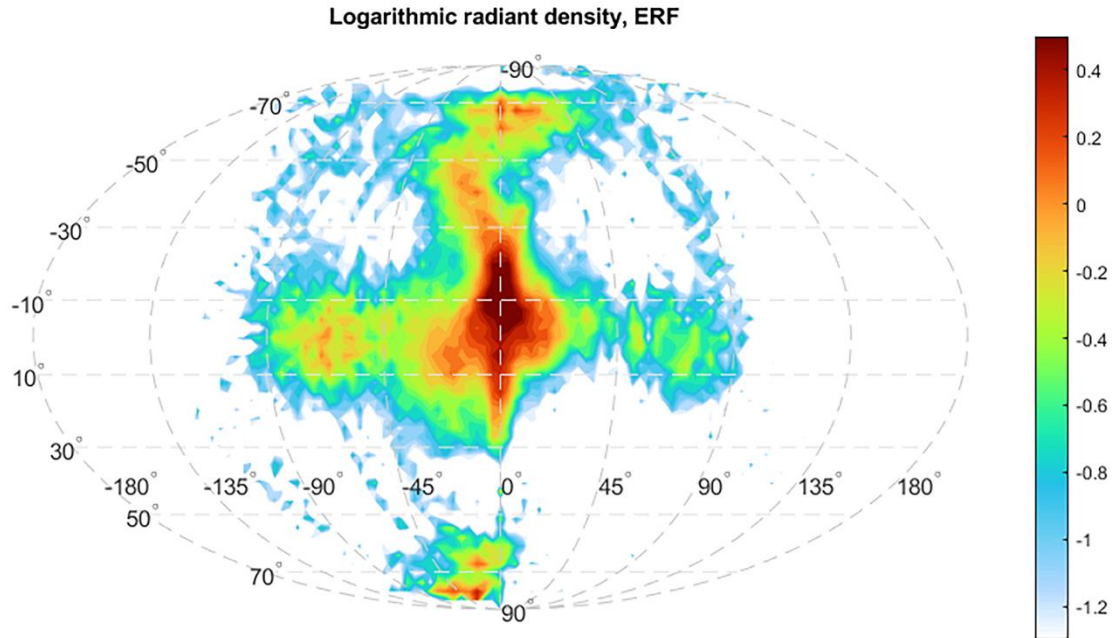
271 greater absolute value for the sensitivity factor indicates a stronger correlation. A positive sensitivity
272 factor indicates a positive correlation between the total sodium content and the respective species, and
273 vice versa. The reference profile is the total sodium content in steady-state in the background condition
274 of the midnight new year of 2002, giving a typical sodium vertical profile similar to the one shown in
275 Figure 5 of Plane (2004). In the simulation, a greater total sodium content implies that a smaller
276 percentage of the sodium chemicals are present as sodium atoms as the altitude profile of the sodium
277 atoms is fixed in the sensitivity test. In reality, instead of the sodium atoms, the total sodium content
278 should be more or less conserved. Hence a higher total sodium content in our simulation suggests less
279 sodium can be detected by the lidar.

280 Although the sensitivity factor could be different upon the change of the reference profile, it still gives
281 an insight into the significance of each background species to the sodium chemistry. Apparently, the
282 weight of some background species, namely O_3 , H, H_2 , and H_2O , is negligible in sodium chemistry,
283 meaning that removing these species and their associated reactions has no effect on the overall sodium
284 chemistry. Nevertheless, these species are still kept in our numerical model for completeness. The
285 impact of species that convert Na atom to Na^+ , as listed in reactions 27 and 28 of Table 1, is generally
286 strong. The effect of NO^+ , in particular, is the most significant according to the sensitivity factor, greater
287 than the combined effect of all the other species. Consequently, the number density of the observable
288 [Na] atom by lidar is strongly anti-correlated with the fluctuations of the NO^+ . In a nutshell, more NO^+
289 will directly lead to fewer observable Na atoms. That being said, the interaction between sodium and
290 background species is rather complex. The scope of the sensitivity factor in the present paper was
291 limited to column density. As a result of such, variations and behaviors of the sodium chemicals by
292 altitude are overlooked. The actual impact of the background species may differ at different altitudes.

293 **4.2 Meteor input function**

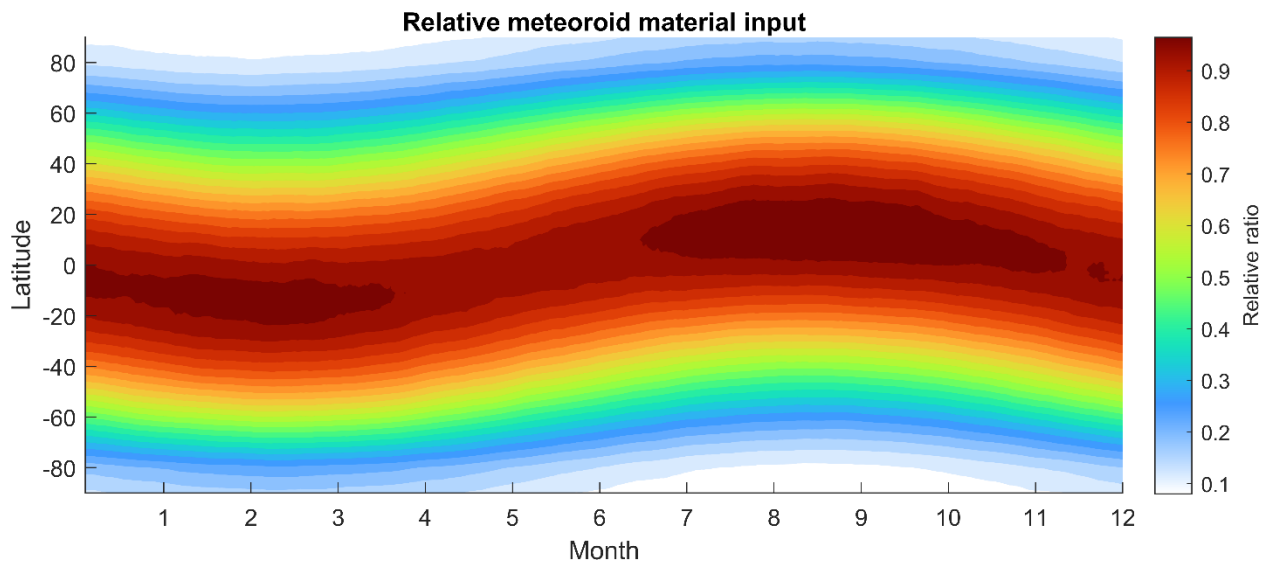
294 The estimation of meteoric influx is subject to many uncertainties among different techniques (Li et al.,
295 2022). Moreover, the meteor flux estimated by the sodium chemistry model also varies (Marsh et al.,
296 2014; Plane et al., 2015). The previous model of Plane (2004) and the following similar models indicate
297 that the rate of dimerization, or the speed of removing sodium from the system, is heavily correlated to
298 the vertical transport in the MLT. The NaChem model does not explicitly incorporate vertical transport,
299 but the vertical transport by diffusion is inherently embedded within the input of the observed sodium
300 vertical profile.

301 Unlike the previous models (Plane 2004; March et al. 2014; and references therein), the present
302 NaChem model took an indirect route to estimate the meteor mass input. During the simulation, the
303 $NaHCO_3$ dimerization and the uptake of the sodium species on meteoric smoke particles, which can be
304 turned on or off, create a deficit of sodium atoms. Meanwhile, a meteor input function injects an
305 appropriate amount of sodium atoms so that the present sodium vertical profile always matches the
306 reference profiles. This is carried out by finding the difference between the current sodium profile (with
307 the deficit) and the corresponding reference profile in every iteration and then replacing the former
308 with the latter. The study by Plane (2004) found that the diffusion coefficient is highly correlated with
309 the sodium sink, primarily because the dimerization reaction occurs predominantly at lower altitudes.
310 The simulation circumvents this uncertainty by directly incorporating the observational sodium vertical
311 profile, given that diffusion is already inherently in the measurements.



312

313 **Figure 4.** Logarithmic meteor radiant source distribution derived from the AO observations. The unit of
 314 this figure is [1/unit time/cell of equal area]. The figure illustrates the relative frequency of meteor
 315 occurrence at different radiant directions in the Earth Reference Frame (ERF), equivalent to ground-
 316 based observations. The latitude of the ERF is centered on the ecliptic plane. The longitude of the ERF is
 317 centered to the Apex direction, the moving direction of the Earth, where the highest number of meteors
 318 encounter Earth. The radiant distribution is derived from the number of meteor events. Figure
 319 reproduced from Li et al. (2022).

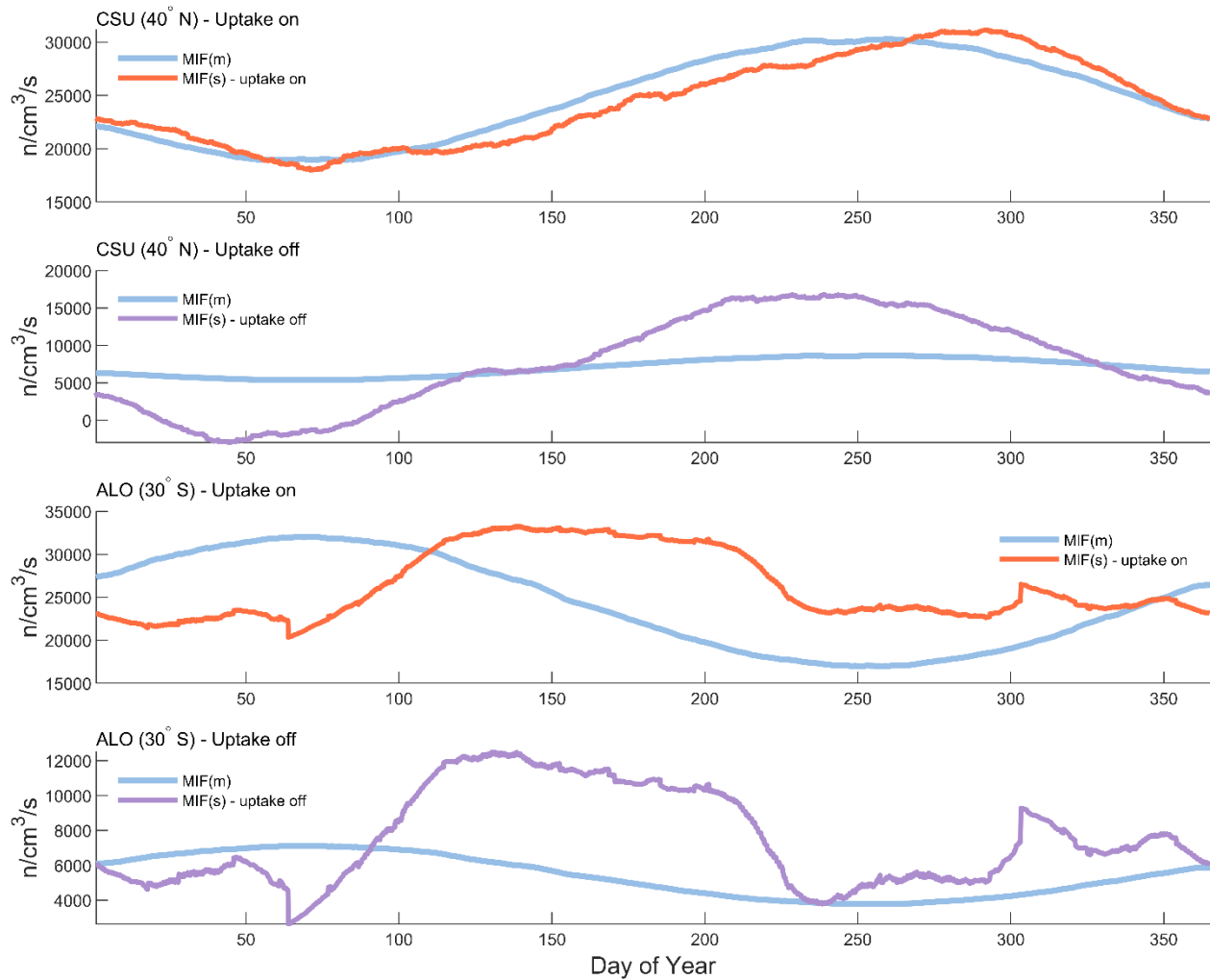


320

321 **Figure 5.** Relative seasonal and latitudinal meteoroid input by meteor occurrence, inferred from the
 322 radiant source distribution shown in Figure 4. The figure is normalized to its max value.

323

Sodium column injection rate



324

325 **Figure 6.** A comparison between two meteor input functions: $MIF(m)$, which is inferred from micro-
 326 meteor radiant distribution, and $MIF(s)$, which is derived using a Na chemistry model with sodium input
 327 from lidar observations.

328

329 Figure 4 shows the high-resolution meteor radiant source distribution recently inferred from the AO
 330 observations (Li et al., 2022). The typical mass of the Arecibo meteors is estimated to be around 10^{-13} kg
 331 based on flux rate (Li and Zhou, 2019). Mathews et al. (2001) estimated the limiting meteor mass of 10^{-14}
 332 kg based on the meteor ballistic parameter. Limiting mass is the smallest mass a meteoroid must have
 333 to generate sufficient ionization to be detected by radar. Despite these estimations being based on
 334 various simplified assumptions that may lead to inaccurate results, the estimated limiting mass at AO is
 335 still at least two orders of magnitude smaller than the estimations of other facilities by similar means.
 336 More than 95% of the meteoroid population in the Earth's atmosphere is found to be sporadic meteors
 337 by HPLA radar observation (Chau and Galindo, 2007), which typically are low-mass meteors evolved
 338 from the outer Solar system due to the Poynting-Robertson drag (Nesvorný et al., 2011; Koschny et al.,
 339 2019). That being said, the percentage of sporadic meteors, as well as the radiant source distribution,

340 are both estimated based on the occurrence. However, the occurrence of sporadic meteors may not be
341 able to represent their mass distribution. The relative seasonal and latitudinal meteoroid input by the
342 number of occurrences inferred from the new radiant distribution is depicted in Figure 5. The meteoroid
343 input generally follows a sinusoidal pattern and differs from the one used in the previous work, as
344 shown in Figure 1 of Marsh et al. (2013). Although the interplanetary dust (meteor) background on the
345 Earth's orbit could vary in different locations due to a variety of reasons, e.g., Jupiter resonance, it is still
346 safe to assume no change in the interplanetary dust background for our purpose. Taking a stable
347 interplanetary dust background, the MIF(m) 's seasonal sinusoidal pattern should follow the Earth's axis
348 rotation relative to the ecliptic plane.

349 Figure 6 shows a comparison between two types of meteor input function: MIF(m), which is inferred
350 from the micro-meteor radiant distribution, and MIF(s), which is derived using the Na chemistry model
351 with sodium input from the lidar observations. Same as MIF(m), MIF(s) is also smoothed by a 15-day
352 running average. For the MIF(s) model simulations, we did two scenarios, one with and one without
353 uptake by smoke particles, for the ALO and CSU data. The MIF(s) with uptake by smoke particles exhibit
354 a good match with the MIF(m) on the CSU dataset, while it does not show as good of a match on the
355 ALO dataset. The MIF(s) with smoke uptake off is represented by a purple line, while the MIF(s) with
356 smoke uptake turned on is depicted by an orange line. The MIF(s) could go negative when the reference
357 sodium vertical profile decreases faster than the removal rate by the dimerization, as shown in the
358 orange line in Figure 6, indicating that the dimerization process alone is not sufficient enough to account
359 for all the sodium atom depletion in the MLT region. MIF(m) is derived from a global micro-meteor
360 radiant distribution model, as depicted in Figure 4 and Figure 5. The smoke uptake of sodium species in
361 this study is implemented using a methodology similar to Plane (2004), but instead of applying smoke
362 uptake solely to the three major sodium species, namely Na, NaHCO₃, and Na⁺, it is applied to all 14
363 sodium-bearing species. The optimal uptake factor to obtain the best results was found to be 2×10^{-2}
364 ²/km/s. The smoke uptake and NaHCO₃ dimerization account for approximately 75% and 25% of the Na
365 sink, respectively.

366 According to the global meteoroid orbital model outlined in Li et al., (2022), the latitudes spanning 29.5°
367 S to 30.5° S (ALO) account for 0.52% of the total meteor input, while those between 39.5° N and 40.5° N
368 (CSU) represent 0.67%. The CSU site shares more meteor input due to its closer proximity to one of the
369 Apex meteor radiant sources. The global total sodium injection rate inferred from the ALO data-based
370 simulation is $(2.01 \pm 0.68) \times 10^{23}$ atoms per second, and the CSU-data-based simulation suggests a global
371 sodium injection rate of $(1.28 \pm 0.55) \times 10^{23}$ atoms per second. The error is determined by calculating the
372 standard deviation of the detrended, unsmoothed raw MIF(s). Note both MIF(m) and MIF(s) presented
373 in Fig.6 are smoothed by a 15-day running average. Assuming the relative sodium elemental abundance
374 in meteoroid material is 0.8% (Vondrak et al., 2008), the deduced total meteoroid material input of ALO-
375 based simulation was $83 \pm 28 \text{ t d}^{-1}$. From CSU-based simulation, the rate is $53 \pm 23 \text{ t d}^{-1}$. Both estimations
376 are close to 80-130 t d^{-1} , the value reported by the Long Duration Exposure Facility (Love and Brownlee,
377 1993; McBride et al., 1999). It is worth noting that the estimated total daily input of meteoroid materials
378 varies among previous studies, ranging from 4.6 t d^{-1} (Marsh et al., 2013) to 300 t d^{-1} (Nesvorný et al.,
379 2009), with an intermediate value of 20 t d^{-1} reported by Carrillo-Sánchez et al. (2020). While these
380 estimates seem quite disparate, the variance is relatively small given that the daily input rate is derived
381 from combinations of chemicals that can fluctuate by several orders of magnitude. For example, the

382 NO⁺, which exhibits the highest sensitivity factor according to the sensitivity test, undergoes diurnal
383 variations of approximately three orders of magnitudes.

384

385 5. Discussion

386 The sodium concentration in the sodium layer in the MLT region is governed by several factors, including
387 chemistry, dynamics, and the MIF. It's difficult to discern which of these three components is more
388 important than the others. In this section, we discuss various factors that may contribute to modeling
389 the sodium concentration in the MLT.

390 The mass of the meteoroids has been estimated and measured using various methods. These include
391 the ballistic parameter derived from meteor deceleration (Mathews et al., 2001), estimation of meteor
392 head echo plasma distribution through a combination of meteor ablation models and radar cross-
393 section measurements (Close et al., 2005; Sugar et al., 2021), flux rate determination (Zhou and Kelley,
394 1997), as well as spacecraft in-situ measurements (Leinert and Grun, 1990), among others. The mass
395 estimated by the meteor ballistic parameter is commonly referred to as momentum or dynamical mass.
396 The mass estimated by the meteor ablation model is usually called the scattering mass. The meteor
397 momentum mass from Arecibo Ultra-High-Frequency (UHF) radar observation is estimated to be $10^{-14} -$
398 10^{-7} kg, with the typical mass being 10^{-13} kg. On the other hand, the meteor scattering mass is estimated
399 to be $10^{-9} - 10^{-5.5}$ kg by data from EISCAT UHF radar (Kero et al., 2008) and $10^{-7} - 10^{-4.5}$ kg by data from
400 ALTAIR UHF radar (Close et al., 2005). While the detection sensitivity among different facilities differs,
401 these estimations are still off by many orders of magnitude. The assessments of either momentum mass
402 or scattering mass are based on a variety of simplified assumptions. They are subject to errors due to
403 the complexity of radar beam patterns, background atmosphere conditions, aspect sensitivity, meteor
404 radiant sources, and many other possible factors. For example, radar meteor observation is subject to
405 bias against low-mass, low-velocity meteors (Close et al., 2007; Janches et al., 2015).

406 Another aspect that may contribute to the MIF(m)'s uncertainty is the meteor radiant distribution. The
407 meteor radiant distributions shown in Figure 4 and many others (Chau et al., 2004; Campbell-Brown and
408 Jones, 2006; Kero et al., 2012) are inferred or measured by meteor occurrence instead of mass input.
409 Currently, retrieving a more accurate estimation of the meteor mass input is still a topic under active
410 research, and there is no quantitative study on the disparities between meteor occurrence and meteor
411 mass input. The radiant sources of the meteors are expected to differ by mass as their orbital evolution
412 is highly correlated to their mass. The interplanetary dust interacts with the solar wind while in the Solar
413 System, losing its momentum in the process and evolving into orbits with a smaller semi-major axis and
414 lower eccentricity. The effect is called the Poynting-Robertson effect (Robertson and Russell, 1937),
415 which behaves like a drag force and defines the evolution of interplanetary dust, and it could be the
416 major reason for the existence of sporadic meteors (Li and Zhou, 2019; Koschny et al., 2019). The
417 importance of the Poynting-Robertson effect is highly dependent on the density and mass of the object.
418 By and large, the orbits of the smaller particles evolve exponentially faster. The orbital dynamics of
419 interplanetary particles have been very well summarized in section 2.2 of (Koschny et al., 2019). For the
420 reasons above, the meteor radiant distribution of mass could deviate from the radiant distribution of
421 occurrence. Therefore, the meteor input rates as shown in the blue curves of Figure 6 could be different
422 from those derived from the meteor radiant distribution of mass since they were derived from the
423 meteor radiant distribution by occurrence.

424 In the sodium chemistry model presented in this work, the MIF is the sole source of sodium, while the
425 sodium sink comprises NaHCO_3 dimerization and smoke uptake. The MIF(s) is determined by matching
426 the sink rate of the sodium atoms with the rate of sodium injection. In other words, MIF(s) represents
427 the amount of sodium injection needed to keep the sodium concentration equal to the reference
428 sodium profiles. If the chemical lifetime of sodium in the MLT is short, then the seasonal variation of
429 both the MIF and sodium concentration in the MLT should be similar. After examining Figures 3, 5, and
430 6, it can be observed that the averaged seasonal variation of sodium over the years at both sites (ALO
431 and CSU) does not correspond to the trend of the MIF(m) at their respective latitudes. This may indicate
432 that the chemical lifetime of sodium in the MLT should be relatively long, as there is no immediate effect
433 of MIF(m) on the sodium concentration. The MIF displays a sinusoidal pattern which peaks in March at
434 the ALO's latitude and in August at the CSU's latitude, whereas the sodium layer shows dual peaks in the
435 CSU's lidar observations and one peak in June in the ALO's lidar observations.

436 In this study, the MIF(s) derived from the NaChem simulation, based on the CSU lidar measurements
437 with uptake turned on, was able to match the amplitude of MIF(m) obtained from the meteor radiant
438 distribution. Although the model does not directly incorporate any dynamical processes, the vertical
439 transport by diffusion is implicitly included. The model forces the sodium layer to be the same as the
440 data, which are averaged by the observations of many years, in which the diffusions are inherently
441 embedded. The combination of observational data with the numerical chemistry model in this paper is a
442 relatively straightforward application of data assimilation (Bouttier & Courtier 2002). The lidar data of
443 both sites (CSU and ALO) indicate that the sodium column density consistently increases by about 20%
444 from 22:00 to 4:00 LT the next day. This can be attributed to the fact that, during nighttime, the large
445 deposits of Na^+ formed by daytime reactions slowly neutralized to Na. As a result, the sodium column
446 density consistently increases throughout the night. The same effect can be reproduced in the NaChem
447 simulation, albeit with a smaller amplitude. The simulation shows the increase to be about 8%. The
448 value is obtained by maintaining a constant total number of sodium-bearing species through the
449 deactivation of the sodium sink.

450 While meridional transport or atmospheric dynamics both contribute to the seasonal variation of the
451 sodium layer in the MLT, the diurnal sodium profile is the mean of observations of thousands of days, of
452 which the variation by atmospheric dynamics should be much less prominent. The lack of explicit
453 dynamics in the model may be one of the sources of inconsistency when compared to the observations.
454 Further, the WACCM 6, which supplied the background species to the NaChem, is an older version that
455 does not fully incorporate the dynamics of each ion species. Despite our results showing good
456 agreement between the MIF(s) and the MIF(m), there might be several plausible factors that could lead
457 to potential errors. For example, the Na sink by NaHCO_3 dimerization varies by the diffusion rate or the
458 vertical transport of sodium atoms in the chemistry model (Plane, 2004). Likewise, the MIF(m) may also
459 differ if the meteoroid mass input differs from the radiant source distribution by the occurrence of
460 meteors, as discussed in the aforementioned paragraph.

461 **5. Conclusion**

462 This work introduced a new sodium chemistry model that simulates the time evolution of all sodium-
463 bearing species using the continuity equation without making any steady-state assumption. The model
464 employs an exponential integrator and runs in high-time resolution to maintain numerical stability. The
465 model is simple to maintain in such a configuration and can be scaled up to include additional

466 capabilities more easily. The model is highly optimized for processing efficiency and benefits from the
467 use of an exponential integrator. Therefore, within an acceptable total CPU time, the NaChem can afford
468 a time resolution of up to milliseconds, several orders of magnitude smaller than those used in other Na
469 models. During our testing, the CPU time to simulated real-time ratio is about 1 to 1000 using a 0.1
470 second time step.

471 The model simulation was able to reproduce the seasonal variation of the sodium layer in the MLT by
472 simulations of chemical reactions. The simulation results at the CSU's latitude capture the general trend
473 of the seasonal variation at the location. The MIF(s) based on the ALO data exhibited less conformity
474 with the corresponding MIF(m), which could be attributed to inadequate statistics of the observational
475 data. Comparably, the CSU dataset is more reliable as the insufficient lidar hours in the ALO dataset may
476 lead to inaccurate statistics. In the simulation, when forcing the sodium layer to be the observation-
477 based reference profile, the inferred MIF is estimated to be $83 \pm 28 \text{ t d}^{-1}$ at ALO and $53 \pm 23 \text{ t d}^{-1}$ at CSU.
478 The numerical simulation by NaChem could reproduce the general trend of diurnal and seasonal
479 variation of the sodium layer compared to the observations by the CSU Lidar. There are some
480 inconsistencies in MIF(m) and MIF(s) based on data obtained from ALO Lidar. These inconsistencies may
481 have originated from poor statistics resulting from insufficient observation hours.

482 In summary, a new sodium chemistry model has been developed in this work to investigate the
483 relationship between MIF and the sodium layer. We also compared the MIF(m) derived from radar
484 meteor observation to the MIF(s) derived from the chemistry model and lidar observations. Our results
485 indicate that the uptake of sodium species onto meteoric smoke particles removes approximately three
486 times more sodium than the dimerization of NaHCO_3 . Our future work will focus on incorporating the
487 plausible factors that may lead to potential errors discussed above into the chemistry model.

488

489

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496 Sodium LIDAR facility and the Andes Lidar Observatory.

497

498 Code/Data availability

499 The CSU lidar data is available through Utah State University data service (Yuan, 2023). The ALO data is
500 available through the ALO online database (ALO, 2023). The WACCM data used in this work are available
501 through Penn State Scholarsphere (Li, 2023b).

502

503 Author contribution

504 Conceptualization, Yanlin L., Tai-Yin H. and Julio U.; methodology, Yanlin L.; software, Yanlin L.;
505 validation, Yanlin L., Tai-Yin H., Fabio V., Julio U. and Wuhu F.; formal analysis, Yanlin L., Tai-Yin H. and
506 Julio U.; investigation, Yanlin L., Tai-Yin H., Julio U. and Wuhu F.; resources, Tai-Yin H., Julio U., Fabio V.,
507 and Wuhu F.; data curation, Yanlin L.; writing---original draft preparation, Yanlin L.; writing---review and
508 editing, Yanlin L., Tai-Yin H., Julio U., Fabio V., and Wuhu F.; visualization, Yanlin L.; supervision, Julio U.
509 and Tai-Yin H.; project administration, Julio U. and Tai-Yin H.; funding acquisition, Julio U. and Tai-Yin H.
510 All authors have read and agreed to the published version of the manuscript.

511

512 Competing interests

513 The authors declare no competing interests.

514

515 Reference

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