To Dr. D. Buresova, Topical Editor

Each issue has been addressed in the Comment/Response format. These responses are highlighted in bold typeface in the revised manuscript.

Point-by-point replies to the comments raised by Referee #1 are given below.

**Comment 1:**
Is there any evidence for ionospheric potential variation?

**Response:**
Following paragraph is added to the revised version (Lines 44-51).

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Ionospheric potential may be observed in the global current circuit of the ionosphere-atmosphere-earth system. The currents in this circuit are generated in the atmosphere by charge separation processes in tropical convective storms. The current influenced by the ionospheric potential can be detected in this global circuit by monitoring vertical component (Bz) of the ground magnetometer data. Reduction of Bz on the ground correlates with decrease of atmospheric electric field on the ground [Minamoto and Kadokura, 2011]. Such correlation would occur in connection with the potential drop of the ionosphere above the ground station [Saka, 2021a].

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**Comment 2:**
Scenario is against common sense and observations.

**Response:**
The parallel electric fields of two types (transient and steady-state ones) develop sequentially with different time scales. Transient electric fields with short time scale (few seconds) develop first in the ionosphere. These transients yield charge separations along the field lines. Charge separations along the field lines produce steady-state parallel electric fields in the magnetosphere. Steady-state electric fields initiate auroral evolutions arising out of the onset arc (onset of substorm). Substorm subsides when charge separation along the field lines is neutralized. Because the flux tube contains parallel electric field pointing upward, neutralization may progress locally and intermittently accompanying auroral precipitation. This scenario is consistent with the referee’s comment that “during substorm, plasma sheet
particles refill the loss cone constantly."

For more details, please refer to Lines 56-142.

Comment 3:
Making the idea clearer, figures and sentences as well.
Response:
To clarify the ionospheric injection model, the parallel electric fields are divided into two types, one transient and the other steady-state. They arise sequentially. New figure (Figure 2) is added in the revised version to graphically show transient and steady-state electric fields. The revised manuscript is now more explicit with a step-by-step description of the distinct parallel electric fields.

For more details, please refer to Lines 56-142.

Specific comment 1:
What is "one direction"?
Response:
Instead of repeating description of electron and ion motions in the ionosphere as detailed in Saka (2021b), I added following paragraph in Lines 32-43.
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The ionosphere as generator has the capability to produce electrostatic potential itself, once the electric fields are transmitted along field lines into the auroral zone from the magnetosphere or produced therein by the local neutral winds [Saka, 2021b]. While these electric fields that have penetrated the E region may accumulate collisionless electrons at a leading edge of flow channels caused by the ExB drift, collisional ions cannot follow them. The negative potential thus produced at the leading edge of flow channels in the E region generates upward electric fields as an auroral driver. Although this conjunction is inconsistent with Gauss’s theorem, it can be understood if a positive space charge was generated immediately above the ionosphere. The above description is consistent with the formation of an incomplete Cowling channel [Baumjohann, 1980], except that upward field-aligned currents are created at the negatively charged southern border [Saka, 2021b].
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Specific comment 2:
Coordinate system
Response:
New figure (Figure 2) below is added.

Figure 2
Transient electric fields pointing into the ionosphere (downward) and steady-state electric fields out of the ionosphere (upward) are discussed in the ionospheric injection scenario. Negative charge sheet shown in red at polar ionosphere produced transient electric fields. Steady-state electric field was initiated by the transient electric field via Persson’s theorem (see text). Transient electric fields are shielded by the space charge deposited in association with the onset of steady-state electric fields.

Specific comment 3:
Persson’s scenario
Response:
Positive charges are generated by the Persson’s scenario (1963) immediately above the ionosphere. These positive charges and repelled electrons in the magnetosphere by the magnetic mirroring generate steady-state electric fields. These upward electric fields initiate substorms. Consequently, substorm conditions are not applied to Persson’s scenario.

For more details, please refer to Lines 56-142.
Specific comment 4:
Unclear definition, X₁ and X₂.
Response:
Removed as no related figures in the text.

Technical corrections:
Response:
We used c instead of α.

Point-by-point replies to the comments raised by Referee #2 are given below.

Comment 1:
The argumentation is circular.
Response:
To avoid circular argumentation, we distinguish parallel (vertical) electric fields of two types (transient and steady-state ones) developing sequentially with different time scales. First, vertical electric fields with short time scale (few seconds) develop in the ionosphere. These transients yield space charges along the field lines according to Persson’s theorem (1963). Space charges along the field lines produce steady-state parallel electric fields in the magnetosphere. The transients were shielded quickly by the space charges emerged. Steady-state electric fields initiate auroral evolutions arising out of the onset arc (onset of substorm).

For more details, please refer to Lines 56-142.

Comment 2 (1):
Equations and use of quantity α.
Response:
All equations are numbered. The second equation, \( \sin^2 \alpha = \frac{B}{B_R} \) is a key equation in the ionospheric driver scenario. This equation, applicable in the absence of parallel electric fields, shows the pitch-angle of particle at any point B relates to magnitude \( B_R \) at the reflection point. In the presence of the parallel electric fields, the above relation is modified to move the
pitch-angle at any point of B to higher altitudes. If this happened to electrons in limited altitude range, positive charges would be yielded locally there. These are evaluated numerically by integrating velocity distributions over the phase space (equation 3).

**Comment 2 (2):**
Is phase space density empty in loss cone?

**Response:**
Charge separations along the magnetic fields constitute steady-state solutions of the parallel electric fields [Alfven and Falthammar, 1963; Persson, 1966]. Steady-state electric fields may persist until charge separation along field lines is neutralized. Because flux tube contains parallel electric fields pointing upward, neutralization may occur locally and intermittently accompanying auroral precipitation. We then assumed that loss cone electrons are removed by the downward acceleration before the start of following auroral evolutions. “C=0” may not be an unreasonable assumption prior to the substorm onset.

For more details, please refer to Lines 56-142.

**Comment 3:**
Discussion of prior work and meaning of “local breakdown” and “injection”.

**Response:**
Following points of view are included in the section of introduction.
Generators that build up parallel electric fields supposedly exist in the distant magnetosphere. Magnetospheric generator is constituted by Poynting flux of the fields and particle momentum from the plasma sheet, plasma flows in the flux tube, charge separations across the nightside magnetosphere. In addition, a generator exists in the polar ionosphere as a modified Cowling channel.

For more details, please refer to Lines 22-43.

Local breakdown”: Breakdown of the charge neutrality is initiated by the transverse electric field in the E layer. The breakdown creates negative charge sheet in the ionosphere and generates transient electric fields pointing into the ionosphere (downward).

“Injection”: Injections are triggered by the steady-state electric fields pointing out of the ionosphere (upward). Steady-state electric fields inject ions out of the ionosphere to avoid complete neutralization of the polar ionosphere.
Parallel electric fields produced by the ionospheric injection

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Abstract

It is well known that there exists a thin layer in the lower boundary of the ionosphere between altitudes of 80 km and 140 km in which collisional ions and collisionless electrons mix. Local breakdown of charge neutrality may be initiated in this layer by electric fields from the magnetosphere as well as by electric fields generated there by the local neutral winds. The breakdown may be momentarily canceled by the Pedersen currents, but a complete neutralization is prevented because some ionospheric plasmas are released as outflows by parallel electric fields. Those parallel electric fields are produced by inherent plasma processes in the polar ionosphere and act as auroral drivers. New scenario creating parallel potential gradients is proposed.

1. Introduction

The Poynting flux of the fields and particle momentum carried by double layer or electrostatic shock generate parallel electric fields in the magnetosphere [Block, 1977; Goertz and Boswell, 1979]. Field-aligned plasma flows in converging field geometry
are mechanical energies that excite parallel electric fields by the charge separations along the field lines due to the magnetic mirroring of electrons and ions [Sato, 1982; Schriver and Ashour-Abdalla, 1993]. Open fields interacting with the solar wind and a charge separation across the nightside magnetosphere due to the plasma convections in the magnetosphere create parallel electric fields [Lyons, 1980; Stern, 1981]. These parallel potentials associated with the magnetospheric generators are used to infer FAC in the magnetosphere [Knight, 1973; Chiu and Schulz, 1978].

The ionosphere as generator has the capability to produce electrostatic potential itself, once the electric fields are transmitted along field lines into the auroral zone from the magnetosphere or produced there by the local neutral winds [Saka, 2021b]. While these electric fields that have penetrated the E region may accumulate collisionless electrons at a leading edge of flow channels caused by the ExB drift, collisional ions cannot follow them. The negative potential thus produced at the leading edge of flow channels in the E region generates upward electric fields as an auroral driver. Although this conjunction is inconsistent with Gauss's theorem, it can be understood if a positive space charge was generated immediately above the ionosphere. The above description is consistent with the formation of an incomplete Cowling channel [Baumjohann, 1980], except that upward field-aligned currents are created at the negatively charged southern border [Saka, 2021b].

Ionospheric potential may be observed in the global current circuit of the ionosphere-atmosphere-earth system. The currents in this circuit are generated in the atmosphere by charge separation processes in tropical convective storms. The current influenced by the ionospheric potential can be detected in this global circuit by monitoring vertical component (Bz) of the ground magnetometer data. Reduction
of $B_z$ on the ground correlates with decrease of atmospheric electric field on the ground [Minamoto and Kadokura, 2011]. Such correlation would occur in connection with the potential drop of the ionosphere above the ground station [Saka, 2021a].

The proposed new scenario referred to as ionospheric injection is summarized in Sect. 2. Summary and discussion are presented in Sect. 3.

2. Ionospheric injection

Distribution of the pitch angle along the field lines can be expressed using constant of the motion,

$$\mu = \frac{m_q v^2 \sin^2 \alpha}{2B}$$  \hspace{1cm} (1)

Here, $\alpha$ denotes pitch angle at the magnetic field $B$, and $m_q v^2 / 2$ is kinetic energy of particle $q$. Substituting $B_r$ at the mirror height ($\sin^2 \alpha = 1$), altitude profiles of the pitch angle in the absence of the parallel electric fields can be given as,

$$\sin^2 \alpha = \frac{B}{B_r}$$  \hspace{1cm} (2)

Figure 1 shows altitude profile of $\sin^2 \alpha$ along $L=6$ of the dipole fields from the ionosphere (100 km) to 10,520 km above it.

Pitch angle curve along the field lines shown in Figure 1 could be modified by the presence of the parallel electric fields. Two types of the parallel electric fields are discussed, one being transient and the other steady-state. Direction of the transient electric field is downward into the ionosphere and that of the steady-state electric field is upward out of the ionosphere (Figure 2).

2.1 Excitation of transient electric fields
We assume negative potential regions are produced by the local breakdown of the charge neutrality. This breakdown occurred in a thin layer located at boundaries between mesosphere and thermosphere where collisional ions and collisionless electrons mix [Rishbeth and Garriot, 1969]. The thin layer extends between altitude of 80 km to 140 km and is hereafter referred to as the ionosphere.

We assume that the negative charge sheet (1280 km in longitudes and 128 km in latitudes) was developed in the ionosphere. The thickness of the sheet is assumed to be equivalent to the same 60 km thickness of the ionosphere. Emerged charge density is assumed to be $5 \times 10^2 m^{-3}$ in the sheet. Vertical electric fields generated by the negative charge sheet are directed down into the ionosphere (Figure 2). Altitude profiles of the downward electric fields through the center of the sheet are colored red in Figure 3-1. For comparison, magnetic mirror force in mV/m is presented in black, assuming $\mu = 0.16 eV / nT$, corresponding to $\frac{mv^2}{2} = 1 keV$ at $X=1Re$ (6240 nT). Force arising from electrostatic fields exceeds the magnetic mirror force below 3,643 km in altitudes. When the spatial scale of the negative charge sheet decreased to 640 km x 64 km, the crossover altitudes of two forces decreased to 1,830 km (Figure 4-1).

Downward electric fields change pitch-angle trajectories of electrons approaching the ionosphere from the magnetosphere by decelerating the parallel velocities. Mirror height moved to 1,407 km (Figure 3-2). For the smaller scale charge sheet, new mirror height is 590 km (Figure 4-2). For purposes of reference, pitch-angle trajectories in the absence of the parallel electric fields ($\sin^2 \alpha$ vs $X$) are plotted in black. Pitch-angle trajectories of electrons bend clockwise with new mirror height. These are shown in Figure 3-2 and Figure 4-2 in red. Ions may not change pitch-angle trajectories in a bounce time of electrons (few seconds) because of the mass ratio.
As a result, there appeared three regions designated as A, B, C in the pitch-angle plane (Figure 3-2 and Figure 4-2). In (A), electrons and ions are in loss cone, in (B), ions are trapped but electrons from loss cone decelerated by downward electric fields filled this region due to magnetic mirroring, and in (C), electrons and ions are trapped. Pitch-angle discrepancy appears only in region (B): electrons are loss cone populations while ions are trapped populations.

According to Persson (1963), the number densities of hot plasmas are calculated substituting isotropic Maxwellian distribution of temperature $T_q$,

$$f_{\text{trap}}(v_{\|}, v_{\perp}) = \left( \frac{m_q}{2\pi kT_q} \right)^{3/2} \exp \left( -\frac{m_q}{2kT_q} (v_{\|}^2 + v_{\perp}^2) \right) \quad \text{out of the loss cone, and}$$

$$f_{\text{loss}}(v_{\|}, v_{\perp}) = c f_{\text{trap}}(v_{\|}, v_{\perp}) \quad \text{in the loss cone}$$

into

$$\frac{n_i}{n_0} = 2\pi \left[ \int f_{\text{trap}}(v_{\|}, v_{\perp}) + f_{\text{loss}}(v_{\|}, v_{\perp}) \right] v_{\perp} dv_{\perp} dv_{\|} \quad (3)$$

Here, $q$ is applicable to either electrons or ions. We assume that loss cone particles are removed from the flux tubes and are empty ($c = 0$) prior to the auroral evolutions arising out of the onset arc, or before the following auroral onset.

Normalized density difference, $(n_i - n_e) / n_0$, before the auroral onset ($c = 0$) is shown in Figure 3-3 (Figure 4-3). When we choose $c = 0.5$, normalized density difference shown in Figure 3-3 (Figure 4-3) was reduced by half. Positive charges emerged immediately above the ionosphere. The excess electrons repelled from both hemispheres due to magnetic mirroring would create the electron rich regions in the magnetosphere.
2.2 Steady-state solution of parallel electric fields

In the one-dimensional model, parallel electric fields at $s_1$ are calculated by integrating the density difference along field lines $s$,

$$E_{ij}(s_1) = \int_{s_0}^{s_1} \frac{e(n_i - n_e)}{\varepsilon_0} ds$$

(4)

Here $s_0$ denotes ionospheric altitude where integration starts.

These are plotted in Figure 3-4 (Figure 4-4) starting from the ionosphere (0 km) to a point 10,520 km. At this altitude, the upward electric fields are not vanished, because electron rich region may be located far up in the magnetosphere. To plot profiles of the parallel electric fields, geometrical factor ($\sqrt{B_x/B_y}$) was multiplied to $E_{ij}(s_1)$ for adjusting the diverging geometry of the dipole configuration. $E_{ij}(s_1)$ is linearly proportional to the background hot plasma density supplied from the tail. In this plot, hot plasma density $n_0 = 10^3 m^{-3}$ was assumed.

These parallel electric fields are generated by charge separations along the diverging magnetic fields, with positive charges immediately above the ionosphere and negative charges in the magnetosphere constituting steady-state solutions of the flux tubes [Alfven and Falthammar, 1963; Persson, 1966]. Generation of upward electric fields above the negative charge sheet resembles battery connected in series to the negative electrode in the ionosphere. Transient electric fields of opposite polarity would be shielded by the space charge built up along the field line. The lifetime of the transient electric fields is few seconds, a time required for building up the space charge or bounce time of electrons. Steady-state electric fields may persist until charge separation along field lines is neutralized. Because flux tube contains parallel
electric fields pointing upward, neutralization may occur locally and intermittently accompanying auroral precipitation. We assume that loss cone electrons are removed by the downward acceleration before the start of following auroral evolutions.

3. Summary and Discussion

Vertical electric fields develop transiently in the ionosphere and produce different angular distributions of ions and electrons in the magnetosphere. These transients yield charge separations along the field lines. Charge separations along the field lines produce steady-state parallel electric fields in the magnetosphere.

The transients are usually triggered by the transverse electric fields transmitted from the magnetosphere during the dipolarization onset. We also consider the cases where breakdown of the charge neutrality was initiated in the polar ionosphere by the neutral winds. Neutral wind generates positive charge in the leading edge of wind channel and negative charge in the trailing edge; the ExB drift (E is polarization electric fields in the wind channel) generates negative charge to one side and positive to the other side of the wind channel. Auroras are produced in the negative charge region. If wind velocity is weaker than ExB drift, breakdown of the charge neutrality may not happen because polarization drift of ions suppressed the charging up of the ionosphere. Wind velocities of the order of $10^3 \text{m/s}$ are necessary to produce substorm auroras by the neutral wind. This scenario may be reminiscent of auroras among gas planets in the solar system such as weather-driven auroras in Saturn [Chowdhury et al., 2021].
4. Data availability

No data sets were used in this article.

5. Competing interest

The author declares that there is no conflict of interest.

References


Lyons, L.R.: Generation of large-scale regions of auroral currents, electric potentials, and precipitation by the divergence of the convection electric field, J. Geophys. Res., 85, 17-24, 1980.


Persson, H.: Electric field parallel to the magnetic field in a low-density plasma, Physics Fluids, 9, 1090-1098, 1966.


Figure 1
Altitude profiles of $\sin^2 \alpha = B/B_R$ in dipole geometry of $L=6$. $X$ (Re) denotes equatorial projection of the altitudes, from the ionosphere ($X=0.42$ Re) to 10,520 km above it ($X=1.70$ Re). $B_R$ represents field magnitudes at the ionosphere. Trapped particles filled area C. Loss cone particles filled A. This curve can be given in the absence of the parallel electric fields.
Figure 2

Transient electric fields pointing into the ionosphere (downward) and steady-state electric fields out of the ionosphere (upward) are discussed in the ionospheric injection scenario. Negative charge sheet shown in red at polar ionosphere produced transient electric fields. Steady-state electric field was initiated by the transient electric field via the Persson’s theorem (see text). Transient electric fields are shielded by the space charge deposited in association with the onset of steady-state electric fields.
Negative charge sheet extending 1,280km in longitudes and 128km in latitudes are generated in the polar ionosphere.
(1) Equatorial projection of altitude profiles of magnetic mirror force (black) and vertical electric fields (red). X (Re) denotes equatorial projection of the altitudes, from the ionosphere (X=0.42 Re) to 10,520 km above it (X=1.70 Re). It is assumed that \( \mu = 0.16 \text{eV} / \text{nT} \). Vertical electric fields exceed the magnetic mirror force below 3,643 km. Note that amplitudes are presented in mV/m.

(2) Pitch-angle curve, \( \sin^2 \alpha = B / B_r \), for electrons in the absence of the parallel electric fields (black) and those modified by the vertical electric fields (red). Electrons affected by the vertical electric fields moved their mirror point to higher altitudes at 1,407 km above the ionosphere. There are three regions in pitch-angle profiles, namely (A), (B), and (C) (see text).

(3) Difference of number density \( n_i - n_e \) normalized by \( n_0 \). Number densities of ions \( n_i \) and electrons \( n_e \) are calculated by integrating Maxwellian distribution over velocity space. Plasma density in loss cone is empty (see text). The plot along L=6 started from the ionosphere (X=0.42 Re) to 10,520 km above it (X=1.70 Re). Real density is given by multiplying \( n_0 \). Density gap at X=0.54 Re is caused by discontinuous change of \( \sin^2 \alpha \).

(4) Altitude profiles of steady-state electric fields \( E_{//} \) (upward, \( \mu \text{V} / \text{m} \)) along field lines. Horizontal axis is altitudes in km of the field lines along L=6. Note that the ionosphere is at 0 km.
Figure 4

Same as Figure 3 but for half-sized negative charge sheet (640km in longitudes and 64km in latitudes).