



# Effect of Intermittent Structures on the Spectral Index of Magnetic field in the Slow Solar Wind

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**Abstract.** Intermittent structures are ubiquitous in the solar wind turbulence, and they can significantly affect the power spectral index of magnetic field fluctuations which reflects the cascading process of the turbulence. However, the relationship between intermittency magnitude and the spectral index has not been shown yet. Here we present the continuous variation of the magnetic spectral index in the inertial range as a function of the intermittency magnitude. By using the measurements from the WIND spacecraft, we find 42,272 intervals with different levels of intermittency magnitude and with duration of 5-6 minutes from 46 slow-wind streams between 2005 and 2013. Among them, each of the intermittent intervals is composed of one dominant intermittent structure and background turbulent fluctuations. For each interval, a spectral index  $\alpha_B$  is determined for the Fourier spectrum of magnetic field fluctuations in the inertial range between 0.01 Hz and 0.3 Hz. A parameter  $I_{max}$ , which corresponds to the maximum of the trace of partial variance increments of the intermittent structure, is introduced as an indicator of the intermittency magnitude. Our statistical result shows that as  $I_{max}$  increases from 0 to 20, the magnetic spectrum becomes steeper gradually and the spectral index  $\alpha_B$  decreases from  $-1.63$  to  $-2.01$ . Accordingly, an empirical relation is established between  $\alpha_B$  and  $I_{max}$ . The result will help us to know more details about the contributions of the intermittent structures on the power spectra, and further about the physical nature of the energy cascade taking place in the solar wind. It will also help to improve the turbulence theories that contains intermittent structures.

## 1 Introduction

Intermittent structures are ubiquitous in the solar wind turbulence. They correspond to the long tail of the non-Gaussian probability distribution functions of plasma or field fluctuations (Burlaga, 1991; Marsch and Tu, 1994, 1997). Previous studies have revealed that the intermittent structures are associated with current sheets and different types of discontinuities at small scales (tens of seconds) (Burlaga, 1969; Veltri and Mangeney, 1999; Servidio et al., 2012; Wang et al., 2013; Osman et al., 2014), and are associated with the boundary between two adjacent flux ropes at large scales (tens of minutes) (Bruno et al., 2001; Borovsky, 2008) in the solar wind turbulence. These structures play an important role in the turbulence cascading and dissipation processes (Tu and Marsch, 1995; Bruno and Carbone, 2013, and the references therein).



The intermittent structures with large-amplitude fluctuations make a substantial contribution to the shape and power level of magnetic-field spectra, which are directly related to the physical nature of the energy cascade taking place in the solar wind (Sari and Ness, 1969; Salem et al., 2007; Li et al., 2011; Borovsky, 2010). They often make the spectra become steeper (Siscoe et al., 1968; Burlaga, 1968; Salem et al., 2009). In previous studies, the time series of discontinuities were reported to produce  $f^{-2}$  energy spectrum (Sari and Ness, 1969; Roberts and Goldstein, 1987; Champeney, 1973; Dallas and Alexakis, 2013) in the inertial range. Later, people also found that the discontinuities can also produce the power spectra that are shallower than  $f^{-2}$ . Li et al. (2011) studied the effect of current sheets on the magnetic power spectrum from the Ulysses Observations. They found that the current-sheet-abundance periods and current-sheet-free periods show  $f^{-5/3}$  Kolmogorov scaling and  $f^{-3/2}$  Iroshnikov-Kraichnan scaling, respectively. Accordingly, they proposed that the current sheet is the cause of the Kolmogorov scaling. This finding was confirmed by Borovsky (2010), who created an artificial time series that preserves the timing and amplitudes of the discontinuities from the ACE spacecraft observations. The artificial time series produces a power-law spectrum with a slope near the Kolmogorov  $f^{-5/3}$  scaling in the inertial range. They emphasize that any interpretation of the dynamics or evolution of the solar wind turbulence should account for the contribution of strong discontinuities to the measurements. The intermittent structures can also lead to the anomalous (multifractal) scaling of structure functions (Veltri and Mangeney, 1999; Veltri, 1999; Salem et al., 2007, 2009).

The intermittent structures also influence the spectral anisotropy of the fluctuations in the solar wind turbulence. The spectral index of the magnetic field fluctuations was reported to be anisotropic with respect to the scale-dependent local mean field in the inertial range (Horbury et al., 2008; Podesta, 2009; Luo and Wu, 2010; Chen et al., 2011; Forman et al., 2011; Wicks et al., 2011). After removing the intermittency from the turbulence, Wang et al. (2014) found that the anisotropy of the spectral index turned out to nearly disappear. The magnetic spectrum in the parallel direction becomes shallower from  $f^{-2}$  to  $f^{-5/3}$ , which is close to the scaling in the perpendicular direction. They concluded that the observed spectral anisotropy could result from intermittency. The result was confirmed by Telloni et al. (2019). Wang et al. (2015) made a comparison between the spectral anisotropy of magnetic fluctuations with low amplitude and that with moderate amplitude. The statistical results showed that the anisotropy is only present in the moderate-amplitude situation, and is absent for the low-amplitude cases. Accordingly, they suggested that the spectral anisotropy is dependent on the fluctuation amplitude. Later, Wu et al. (2020) presented an analysis on the scaling anisotropy with a stationary background field and found the same isotropy for the moderate-amplitude fluctuations after removing those intermittent structures. Through numerical simulation in three-dimensional Magnetohydrodynamic turbulence, Yang et al. (2017) found the influence of intermittency on the quasi-perpendicular scaling of magnetic field and velocity fluctuations.

Recently, the magnitude and thickness of the current sheets are also found to have significant effect on the power level in the dissipation range and the frequency location of the spectral break (Borovsky and Podesta, 2015; Borovsky and Burkholder, 2020; Podesta and Borovsky, 2016). People have also studied the heating effect of the intermittent structures through both observations (Osman et al., 2011, 2012b, a; Borovsky and Denton, 2011; Wang et al., 2013; Liu et al., 2019; Zhou et al., 2022) and simulations (Parashar et al., 2009; Servidio et al., 2012; Wan et al., 2012; Zhang et al., 2015).



From the previous studies mentioned above, people have realized that the intermittent structure is an important part of the solar wind turbulence, and it can significantly affect the shape and power level of the magnetic power spectrum. However, no relation between the intermittency magnitude and the spectral index in the inertial range has been created so far. Here we will present the continuous variation of the magnetic spectral index as a function of the intermittency magnitude, by using the measurements of the WIND spacecraft in the slow solar wind between 2005 and 2013. More than 42,000 intervals with different levels of the intermittency magnitude are selected from 46 slow-wind streams. Our result shows that the power spectrum between 0.01 Hz and 0.3 Hz in the inertial range gets steeper from  $-1.63$  to  $-2.01$  as the intermittency magnitude increases from 0 to 20. It will help us to know more detail about the effect of the intermittency on the turbulence cascading process, and will also supply an empirical relation for the theoretical and numerical studies in the future.

The paper is organized as follows. In Section 2, we introduce the data used in this work and the methods applied to find the intermittent structures and to determine both the intermittency magnitude and the spectral index of magnetic fluctuations in the inertial range. In Section 3, we show our observations, including cases and statistical results. In Section 4, we summarize this work and discuss its consequences.

## 2 Data and Methods

We use magnetic field and plasma data measurements both with the time resolution  $\Delta T = 3$  s obtained respectively by Magnetic Field Investigation (Lepping et al., 1995) and 3D Plasma Analyzer (3DP, Lin et al., 1995) on board the WIND spacecraft between 2005 and 2013. During this period, the WIND spacecraft was located at the Lagrangian point L1 in the undisturbed solar wind. Here we focus on the slow-wind streams with proton bulk velocity  $V_{SW} \leq 450$  km s $^{-1}$ , and the data observed within the compression regions that are followed immediately by fast-wind streams are discarded. The compression region is much more complicated and dynamic than the typical slow wind of interest, and it is out of the scope of this work.

From the eight-year observations, we find 46 slow-wind streams. Each of the stream lasts about  $2 \sim 5$  days. Figure 1 shows one of the selected slow-wind streams observed 12:00:00 UT on 5 Dec 2007 to 00:00:00 UT on 9 Dec 2007. The top three panels are the time variations of the magnetic field (black) and proton velocity (blue) vectors in geocentric solar ecliptic (GSE) coordinates. Panel (d) shows the magnitude of the magnetic field. During the 3.5-day interval, the absolute value of the  $x$  component of the proton velocity shown in panel (a) decreases from  $\sim 360$  km s $^{-1}$  to  $\sim 300$  km s $^{-1}$ . So this interval is out of the compression region, and is not adjacent to fast wind.

A parameter named normalized partial variance of increments  $PVI$  is applied to quantitatively analyze the intermittency in the solar wind turbulence following previous studies (Marsch and Tu, 1994; Greco et al., 2008; Osman et al., 2011; Wang et al., 2013). For a component of the magnetic field vector in a given slow-wind stream, the time series of  $PVI$  is presented as:

$$PVI_i(t, \tau) = \frac{\delta B_i(t, \tau)}{\sqrt{\langle |\delta B_i(t, \tau)|^2 \rangle}} \quad (1)$$



where  $B_i(t)$  is time series of the  $i$  component of the magnetic field vector ( $i = x, y, z$ ),  $\delta B_i(t) = B_i(t + \tau) - B_i(t)$ , and  $\langle \dots \rangle$  denotes an ensemble average in the given stream. The time lag  $\tau$  is selected as 24 s following Wang et al. (2013), corresponding to a spatial separation within the inertial range. In the following we will refer to  $PVI_i(t, \tau)$  as  $PVI_i(t)$  for simplicity without  
90 further specification. Panel (e) of Figure 1 shows the time series of  $PVI_z(t)$  for the stream. Many spikes appear in the time series of  $PVI_z(t)$ , which correspond to large-amplitude fluctuations imbedded in the background turbulence.

In panels (f-h) of Figure 1, we demonstrate the probability distribution function (PDF, solid black curves) of  $PVI$  for the three components of the magnetic field, respectively. The dotted curves are standard Gaussian distribution, and they are plotted for easy comparison. The Gaussian distributions are located between the  $PVI$  range  $[-2, 2]$ . Beyond this range, the observed  
95 distribution curves exhibit long tails, and the tails extend even beyond the plotted range  $[-5, 5]$ . The  $PVI$  range  $[-2, 2]$  will then be used to select intermittent structures. Actually  $PVI_z$  can achieve  $\pm 10$  as shown in panel (e). So it is clear that the profiles of the PDF for the three components ( $PVI_x$ ,  $PVI_y$ , and  $PVI_z$ ) all deviate significantly from the Gaussian distribution, and have long tails when the absolute value of  $PVI_i$  increases. The long tails of the non-Gaussian PDF profiles indicate the existence of intermittent structures.

100 We calculate the flatness for each distribution as:  $F_i = \langle (PVI_i(t))^4 \rangle / \langle (PVI_i(t))^2 \rangle^2$ , where  $\langle \dots \rangle$  still denotes the ensemble average in the given stream. An empirical rule is that the minimum number  $N$  of data points in the time series to be used to accurately calculate moments of order  $M$  is  $N = 10^{M+1}$  (see Dudok de Wit (2004) for instance). In the case shown in Figure 1, the total number of samplings is 100,800. Since flatness (the fourth-order moment) is considered here, the total number of samplings meets the requirement, which is larger than the minimum number  $N = 10^5$ . The values of the flatness  
105 are marked in the bottom three panels, respectively, as  $F_x = 26.1$ ,  $F_y = 30.3$ , and  $F_z = 43.1$ . They are much larger than 3 (characteristic of a standard Gaussian distribution). It again indicates the fluctuations are highly intermittent.

The criterion  $|PVI_i(t)| > 2$  is applied for the basic identification of intermittent structures. First, we find the time instants that satisfy at least one of the conditions:  $|PVI_x(t)| > 2$ ,  $|PVI_y(t)| > 2$ , or  $|PVI_z(t)| > 2$ . Some of the instants are isolated, and some of them are clustered and continuous. Only if the number of the continuous instants is not smaller than 3, they are  
110 chosen for the following study. The rest instants are ignored. A continuous series of the intermittent instants is considered as an intermittent structure. Moreover, if the number of the instants between two adjacent structures is smaller than 3, the two structures and the data points between them are merged together and are seen as one "long-lived" structure. For a given structure, we use  $t_B$  and  $t_E$  to denote its beginning time and ending time, respectively, and use  $(t_E - t_B)/\Delta T$  as the width of the structure in the unit of data point. An interval between  $[t_B - 150 \text{ s}, t_E + 150 \text{ s}]$  is called intermittent interval. After the  
115 constrain of 10% data gap, we find 56,398 intermittent intervals from 46 slow-wind streams between 2005 and 2013.

Figure 2 shows a typical case of an intermittent interval observed by the WIND spacecraft on 2007 Feb 23. Panels (a-c) present the time variations of the three components of the magnetic field vector (black) and the proton velocity vector (gray). The magnetic field is transformed to Alfvén speed unit (i.e.,  $\mathbf{B}/\sqrt{\mu_0 \rho_0}$ , where  $\rho_0$  is the average proton density of this interval), so that the fluctuation amplitudes of the magnetic field and the velocity are comparable. Panel (d) shows the time variations of the magnetic field magnitude. Panel (e) shows the time series of  $PVI_x(t)$  (purple),  $PVI_y(t)$  (yellow), and  $PVI_z(t)$  (green), as  
120 well as the trace  $PVI$  ( $I = \sqrt{(PVI_x)^2 + (PVI_y)^2 + (PVI_z)^2}$ ) (black). The two vertical dotted lines mark the beginning time



( $t_B$ ) and ending time ( $t_E$ ) of the intermittent structure, respectively. We see that between the two vertical lines,  $|PVI_z|$  keeps larger than 2 for 15 s (5 data points), which satisfies our criteria of the intermittent structure selection. Accordingly, the width of this intermittent structure is recorded as 15 s (5 data points).

125 In the case shown in Figure 2, a very significant jump happens in the  $z$  component of the magnetic field between  $t_B$  and  $t_E$ . We also notice that in this case the fluctuation amplitude of the proton velocity is much smaller than the magnetic field (normalized residual energy  $\sigma_r = -0.91$ ), and the fluctuations between the velocity and the magnetic field are not well correlated (correlation coefficient  $cc = -0.11$ ). These characteristics indicate that this case may be associated with magnetic-field directional turning (Tu and Marsch, 1991; Wang et al., 2020). It is convected by the solar wind, and nearly has no velocity  
130 fluctuations. Hence it can lead to low normalized residual energy (close to  $-1$ ) and low correlation between  $\mathbf{B}$  and  $\mathbf{V}$  in the observations.

Next, we determine the intermittency magnitude for each interval. The trace of the normalized partial variance of increments is obtained from  $I = \sqrt{(PVI_x)^2 + (PVI_y)^2 + (PVI_z)^2}$ . If the maximum  $I$  ( $I_{max}$ ) during an intermittent structure (e.g., between the two vertical lines for the case shown in Figure 2) is also the maximum  $I$  during the corresponding intermittent  
135 interval (e.g., the whole interval for the case shown in Figure 2), this interval will be reserved, and  $I_{max}$  is recorded as the intermittency magnitude of this case. Otherwise, the case is eliminated since the energy of the fluctuations during the interval is not dominated by the intermittent structure of interest. In the case shown in Figure 2, we see that  $I_{max} = 4.10$  at 01:44:23 is also the maximum  $I$  within the plotted interval, so this case satisfies the condition well. In this way, 25,912 intermittent intervals are reserved for the following analysis.

140 Then we perform Fast Fourier Transform (FFT) on the magnetic field fluctuations and obtain the spectral index of the Fourier spectrum in the inertial range. In this procedure, we use high-resolution magnetic field data with  $\Delta T = 1/11$  s, so that the spectral index could be more reliable. For a given intermittent interval, the time series of each component of the high-resolution magnetic field data is Fourier transformed using the FFT method. The trace of the spectral matrix gives the total power spectral density, and the spectrum is then three-point centered smoothed following Wang et al. (2015). In panel  
145 (f) of Figure 2, we plot the power spectral density (PSD) as a function of the spacecraft frequency ( $f$ ) in log-log space, i.e.,  $y = \log_{10}(PSD)$  versus  $x = \log_{10}(f)$ , as gray curve. We see that by using the high-resolution data, the spectrum can cover more three decades from  $3.3 \times 10^{-3}$  Hz to 5.5 Hz.

It is known that the points of the gray spectrum shown in Figure 2(f) are not uniformly distributed in the logarithm space of  $f$ . As mentioned in Podesta (2016), in this space the number of data points between two points ( $x$  and  $x + \Delta x$ ) increases  
150 exponentially with  $x$ . If a least-squares fit is performed, each point has equal weight. So the fit favors the points in the higher-frequency range since this range contains more points (Podesta, 2016; Borovsky and Burkholder, 2020). In order to avoid this issue, we linearly interpolate the spectral density onto a uniformly spaced grid with  $\Delta x = (f_{max} - f_{min})/100$  in the log-log space following Podesta (2016). In panel (f) of Figure 2, the black curve superposed on the original gray spectrum demonstrates the interpolated spectrum.

155 Then we perform the least squares fit to the interpolated spectrum to obtain the spectral index  $\alpha_B$  in the log-log space in the inertial range. The least squares fit is performed at the frequency range between 0.01 Hz and 0.3 Hz (between two vertical



dotted lines as shown in Figure 2(f)), and at this range the spectrum can be fitted well by a straight line with a slope of  $\alpha_B$ . The slope ( $\alpha_B$ ) and its corresponding error ( $\Delta_{\alpha_B}$ ) are obtained and both marked in panel (f) as  $\alpha_B = -1.84 \pm 0.04$ . We perform the same analysis on all the selected intervals. Then, the cases with the relative fitting error  $\Delta_{\alpha_B}/\alpha_B > 5\%$  are eliminated, since the magnetic spectra of them do not have a good power-law shape and cannot be well fitted by a straight line in the log-log space at the frequency range of interest. At last, 24,886 intermittent intervals are reserved for the following statistical analysis to explore the relation between the spectral index  $\alpha_B$  and the intermittency magnitude  $I_{max}$ .

### 3 Results: Variations of spectral index versus intermittency magnitude

For the selected 24,886 cases, we first present the joint distribution of their width and intermittency magnitude  $I_{max}$  in panel (a) of Figure 3. We see most of the cases have  $5 \leq Width < 7$  and  $3 \leq I_{max} < 6$ . As the width increases, the distribution of  $I_{max}$  extends to a wider range. This phenomenon makes the pattern of the joint distribution look like a triangle, which is consistent with Miao et al. (2011). They show in Figure 8 the triangle-like shape of the 2-D distribution in the  $\Delta\theta - \tau$  plane, where  $\Delta\theta$  and  $\tau$  are the deflection angle across current sheet and the width of current sheet, respectively. Panel (b) of Figure 3 shows the probability distribution of the width for the intermittent structures of interest. The width extends from 3 points (9 s) to 20 data points (60 s), and the most probable value is 5 data points (15 s). As the width increases, the probability distribution function first increases immediately and then decreases gradually. Panel (c) of Figure 3 shows the probability distribution of the intermittency magnitude  $I_{max}$ . The value of  $I_{max}$  extends from about 2 to 15, and the most probable value is 4.5. The profile of the distribution is similar to that of the width.

Another typical intermittent interval observed on 2010 Sep 12 is shown in Figure 4, but with high intermittency magnitude  $I_{max} = 11.8$ . This figure is plotted in the same format as Figure 2. The intermittent structure is marked by the two vertical dotted lines. Between the two vertical lines, the time instants all satisfy at least one of the conditions as mentioned above:  $|PVI_x| > 2$ ,  $|PVI_y| > 2$ , or  $|PVI_z| > 2$ . Between  $t_B$  and  $t_E$ , a large jump happens in both the  $x$  and  $z$  components of the magnetic field. The fluctuations of the proton velocity (in gray) are well correlated with the fluctuations of the magnetic field (correlation coefficient  $cc = 0.97$ ). However, the fluctuation amplitude of the proton velocity is much smaller than the magnetic field (normalized residual energy  $\sigma_r = -0.50$ ). It indicates that this may be a magnetic-velocity alignment structure (Wang et al., 2020; Wu et al., 2021). Magnetic-velocity alignment structure, of which the generation mechanism remains unclear, is a kind of magnetically dominated structure but with high correlation between magnetic-field fluctuations and velocity fluctuations. For these kinds of structures, the magnetic-field fluctuations are nearly aligned with the velocity fluctuations.

For the case shown in Figure 4, its intermittency magnitude  $I_{max}$  is recorded as 13.09, which corresponds to the value of  $I$  at 06:28:48. The right panel shows the power spectrum of magnetic field fluctuation obtained from performing FFT on the high-resolution magnetic field data. The original spectrum before interpolation is still plotted in gray, and the uniformly distributed spectrum after interpolation in black is superposed on the gray one. The least squares fit is performed on the interpolated spectrum at the frequency range between 0.01 Hz and 0.3 Hz. The spectral index is obtained as  $\alpha_B = -2.01 \pm 0.04$ . The small fitting error indicates that the spectrum has a good power-law shape. The spectral index obtained here is very close to  $-2$ . So



190 it is well consistent with previous theory and observations, which proposed that the discontinuities can produce  $f^{-2}$  energy spectrum in the inertial range (Sari and Ness, 1969; Roberts and Goldstein, 1987; Champeney, 1973; Dallas and Alexakis, 2013).

However, we have seen from the case shown in Figure 2 with  $\alpha_B = -1.84 \pm 0.04$  that the discontinuities are not always related with  $-2$  spectral index in the solar wind observations. The case shown in Figure 2 also have a typical discontinuity imbedded in the background turbulence, but its intermittency magnitude ( $I_{max} = 4.10$ ) is relatively smaller than that shown in 195 Figure 4 ( $I_{max} = 13.09$ ). Correspondingly, the magnetic spectrum of it is shallower. Therefore, it is clear that the intermittency magnitude can affect the spectral index of the magnetic field fluctuations in the inertial range significantly. It is necessary to know the relation between the intermittency magnitude and the spectral index.

In order to give the continuous variation of the spectral index as a function of the intermittency magnitude, we also select 200 some "quiet" intervals with  $|PVI_i| < 2$ . In this procedure, we first cut the data in the 46 slow-wind streams into short intervals with duration of 5 minutes. Then, in each interval we check the maximums of  $|PVI_x|$ ,  $|PVI_y|$ , and  $|PVI_z|$ , respectively. If the maximums of them are all smaller than 2, the interval is reserved as a "quiet" interval. During a given interval, the maximum of the trace  $I = \sqrt{(PVI_x)^2 + (PVI_y)^2 + (PVI_z)^2}$  is recorded as the "intermittency magnitude" ( $I_{max}$ ), although it may not be intermittent at all. The magnetic spectral indices of them are also obtained by using the method mentioned above. 205 Subsequently, we find 17,386 quiet cases for the following study.

Figure 5 shows a typical quiet interval with very low intermittency magnitude  $I_{max} = 1.44$  in the same format as Figure 2. The power spectrum is much shallower than that of the intermittent intervals with relatively higher intermittency magnitudes shown in Figure 2 and Figure 4. The spectral index comes out to be  $-1.65 \pm 0.04$ . It seems to be close to the Kolmogorov scaling  $f^{-5/3}$ .

210 The lower panel of Figure 6 shows the joint distribution of  $I_{max}$  and  $\alpha_B$  for the selected 42,272 intervals. The  $x$  axis corresponding to the intermittency magnitude  $I_{max}$  in the range  $[0, 20]$  is divided into 20 bins. The  $y$  axis corresponding to the magnetic spectral index  $\alpha_B$  in the range  $[-2.5, -1.2]$  is divided into 13 bins. For a given pixel, the color denotes the number of the cases normalized by the maximum number of the pixels among the corresponding  $I_{max}$  bin. Thus, in each column, the pixel with the largest amount of cases is colored in red, corresponding to 1. The maximum number of each column versus 215  $I_{max}$  is also shown in the upper panel of Figure 6. In order to guarantee that there are enough cases used for statistics, the pixels containing no more than 10 cases are ignored. So the pixels in black contains the smallest amount of cases, but the number of the cases is still larger than 10. If we focus on the pixels in red, we notice that when the intermittency magnitude  $I_{max}$  increases, the spectral index  $\alpha_B$  has a very clear decreasing trend from  $\sim -1.6$  to  $\sim -2$ . The gray solid circles show the average  $\alpha_B$  in each  $I_{max}$  bin as a function of  $I_{max}$ , and the dotted gray lines represent the upper/lower quartiles. It is found 220 that as  $I_{max}$  increases from 0.5 to 3.5, the magnetic power spectrum gets steeper quickly from  $f^{-1.63_{-0.12}^{+0.09}}$  to  $f^{-1.84_{-0.11}^{+0.14}}$ . When  $I_{max}$  increases from 4.5 to 15.5, the magnetic power spectrum gets steeper slowly from  $f^{-1.86_{-0.11}^{+0.14}}$  to  $f^{-1.99_{-0.11}^{+0.09}}$ . As  $I_{max} > 16$ , the spectral index keeps close to  $-2$ .

The observed variation of the spectral index  $\alpha_B$  versus the intermittency magnitude  $I_{max}$  can be well fitted by an exponential function. In Figure 6, the black curve corresponding to  $\alpha_B = 0.4 \exp(-I_{max}/5) - 2.02$  shows the fitting result. This empirical



225 relation supplies the continuous variation of the spectral index  $\alpha_B$  of magnetic field in the inertial range as a function of the  
intermittency magnitude  $I_{max}$ . The empirical relation tells us that when  $I_{max}$  is small, and the fluctuations of the magnetic  
field could be considered as randomly distributed, the magnetic spectral index in the inertial range will be close to  $-1.6$ . As  
the fluctuations get intermittent, the magnetic spectrum becomes steeper gradually until  $\sim f^{-2}$ .

#### 4 Discussion

230 Our result confirms the idea that the intermittent structures have significant influence on the magnetic spectral index and often  
make the spectra become steeper (Siscoe et al., 1968; Burlaga, 1968; Salem et al., 2007, 2009). It is generally acknowledged that  
the time series of discontinuities produce  $f^{-2}$  energy spectrum in the inertial range. Later, people found that the discontinuities  
can also produce shallower spectra (Li et al., 2011; Borovsky, 2010). Here, we find from the continuous relation that the  $f^{-2}$   
scaling could be produced if the intermittency magnitude of the structure imbedded in the turbulence is high enough, i.e.,  
235  $I_{max} > 15$  for the cases studied in this work.

Our result is also consistent with the radial evolution trend of intermittency and magnetic spectral index in the solar wind.  
The evolution of intermittency with distance from the Sun can be explained on the basis of the interplay between coherent  
(intermittent) structures and Alfvénic fluctuations. Intermittent events advected by the wind are increasingly exposed as the  
Alfvénic fluctuations are depleted with the heliocentric distance (see, for instance, Bruno et al. (2003)). By using the observa-  
240 tions from Parker Solar Probe, people also found that there is a clear transition for the magnetic spectral index in the inertial  
range as the radial distance from the Sun increases (Chen et al., 2020). When  $r \approx 0.17$  au, the spectral index is close to  $-3/2$ .  
When  $r \approx 0.6$  au, the magnetic spectrum becomes steeper as  $\alpha \approx -5/3$ . These observational results indicate that when  $r$  in-  
creases, the solar wind turbulence becomes more intermittent, and the magnetic spectrum gets steeper. The variation trend of  
the magnetic spectral index versus the intermittency is confirmed by our observations.

245 We also notice that for the cases with very low intermittency magnitude  $0 < I_{max} < 1$ , the magnetic spectral index of the  
intervals is between  $-1.62$  and  $-1.69$ , which is close to the Kolmogorov scaling. This is different from Li et al. (2011), who  
found that the current-sheet free periods show  $f^{-3/2}$  Iroshnikov-Kraichnan scaling. We see from Figure 6 that some of the  
low-intermittency-magnitude cases can also produce the  $f^{-3/2}$  scaling, but the number of the cases with  $-1.6 < \alpha_B < -1.4$   
only account for 20% of all the cases with  $I_{max} < 1$ . The differences between this work and Li et al. (2011) include: they focus  
250 on the  $\sim 1$ -day Ulysses data at about 5 AU, while we use the 5-minute WIND data at about 1 AU. In addition, the frequency  
range for the fittings is  $[10^{-3}, 10^{-1}]$  Hz in Li et al. (2011) and  $[0.01, 0.3]$  Hz here.

The  $f^{-2}$  scaling has been reported for parallel-sampling magnetic fluctuations in many previous studies associated with  
spectral anisotropy (Horbury et al., 2008; Podesta, 2009; Luo and Wu, 2010; Chen et al., 2011; Forman et al., 2011; Wicks  
et al., 2011). Wang et al. (2014) found that after removing the intermittency, the magnetic spectrum in the parallel direction  
255 becomes shallower from  $f^{-2}$  to  $f^{-5/3}$ . However, the question about how the intermittency affect the anisotropy of the spectral  
index remains unclear. In the future, we might try to check the intermittency magnitude of the parallel-sampling data to see if  
the steep spectrum in the parallel direction is related to high intermittency magnitude or not.





The intermittency in many theoretical models are also found to steepen the inertial-range power spectrum of turbulence. For example, a multi-fractal model developed by She and Leveque (1994) (SL model) gave intermittency correction to the Kolmogorov law (Kolmogorov, 1941), and predicted an energy spectrum  $E(k) \approx k^{-5/3-0.03}$  for fluids. Carbone (1993) presented a magnetohydrodynamic (MHD) cascade model and found the intermittency modification to the Kraichnan theory. Politano and Pouquet (1995) extended the SL model to the MHD case, and the energy spectrum was obtained as  $E(k) \approx k^{-3/2-0.04}$ . Boldyrev et al. (2002) predicted for the velocity spectrum  $E(k) \approx k^{-1.74}$  from an analytical study of driven supersonic MHD turbulence. Recently, Chandran et al. (2015) found that when considering scale-dependent dynamic alignment, the power spectrum of the intermittent turbulence flattens. However, there seems no conclusion about which model is the most appropriate one to describe the solar wind turbulence. According to the observational result shown in this work in the slow-wind streams, we obtain the empirical relation between the magnetic spectral index  $\alpha_B$  and the intermittency magnitude  $I_{max}$ . The relation will supply observational basis for theoretical studies of the intermittent turbulence, and will help improve the turbulence theory related to the slow solar wind.

Besides the intermittency, the magnetic spectral index has been reported to also depend on the level of magnetic compressibility. The magnetic compressibility was defined as the ratio between the variance of the magnetic field magnitude fluctuations and the variance matrix trace of the fluctuations, i.e.,  $c_b = \sigma_{|B|}^2 / \sum_{i=x,y,z} \sigma_{B_i}^2$  (Bavassano et al., 1982; Telloni et al., 2019; Wang et al., 2020). Here, in order to take into account of the influence of the magnetic compressibility on the shape of the magnetic spectrum, we also calculate the magnetic compressibility of all the 24,886 intermittent intervals and 17,386 quiet intervals in the 46 slow-wind streams.

The lower panel of Figure 7 shows the joint distribution of the magnetic compressibility  $c_b$  and  $\alpha_B$  for the selected 24,886 intermittent intervals in the same format as Figure 6. The  $x$  axis corresponding to the magnetic compressibility  $c_b$  in the range  $[0, 0.5]$  is divided into 20 bins. The  $y$  axis corresponding to the magnetic spectral index  $\alpha_B$  in the range  $[-2.5, -1.2]$  is still divided into 13 bins. For a given pixel, the color also denotes the number of the cases normalized by the maximum number of the pixels among the corresponding  $c_b$  bin. The maximum number of each column versus  $c_b$  is also shown in the upper panel of Figure 7. The pixels containing no more than 10 cases are ignored. When we focus on the pixels in red, we notice that when  $c_b$  increases, the spectral index  $\alpha_B$  keeps nearly constant. The gray solid circles show the average  $\alpha_B$  in each  $c_b$  bin, and the two dotted gray lines represent the upper and lower quartiles, respectively. It is found that for the selected intermittent intervals, as the magnetic compressibility  $c_b$  increases from 0 to 0.5, the average slope of the magnetic spectrum in the inertial range varies between  $[-1.90, -1.80]$ , and there is no systematic trend. This result could indicate that for the intermittent cases, the magnetic compressibility does not have significant influence on the magnetic spectral index in the slow-wind streams of interest.

The same analysis is performed on the selected 17,386 quiet intervals. The result is shown in Figure 8. Figure 8 is plotted in the same format as Figure 7. When we focus on the most probably value of  $\alpha_B$  in each  $c_b$  bin, i.e., the pixels in red, we can find that no clear trend appears, neither. The gray solid circles and the two dotted gray lines represent the average  $\alpha_B$  in each  $c_b$  bin and the upper/lower quartiles, respectively. When  $c_b$  increases from 0 to 0.5, the magnetic spectral index changes slightly from  $-1.76 \pm 0.14$  to  $-1.70 \pm 0.10$ . The result indicates that for the quiet cases in the slow-wind streams of interest, the magnetic compressibility does not significantly affect the magnetic spectral index, neither.



## 5 Conclusions

In this paper, we first present the continuous relation between the magnetic spectral index  $\alpha_B$  in the inertial range and the  
295 intermittency magnitude  $I_{max}$  at the time scale of  $\tau = 24$  s in the slow solar wind. The data from the WIND spacecraft obser-  
vations between 2005 and 2013 are used for analysis. We select 24,886 intermittent intervals and 17,386 quiet intervals from  
46 slow-wind streams. Each intermittent interval lasts about 5 ~ 6 minutes with a dominant intermittent structure imbedded in  
the center of it. The maximum  $I$  ( $I_{max}$ ) of an intermittent structure is recorded as the intermittency magnitude of the corre-  
sponding interval. The magnetic trace power spectrum of each interval is obtained by performing FFT on the high-resolution  
300 magnetic field data with  $\Delta T = 1/11$  s, and is then linearly interpolated onto a uniformly spaced grid in the log-log space. The  
spectral index  $\alpha_B$  is obtained by performing the least squares fit on the interpolated spectrum between 0.01 Hz and 0.3 Hz in  
the inertial range. The selected intervals all have relatively low fitting errors ( $\Delta_{\alpha_B}/\alpha_B \leq 5\%$ ), indicating that the magnetic  
power spectra of them have good power-law shape.

The observed variation of the averaged spectral index  $\alpha_B$  as a function of the intermittency magnitude  $I_{max}$  is presented  
305 in the lower panel of Figure 6 as gray solid circles. When  $I_{max}$  increases from 0.5 to 15.5, the magnetic power spectrum  
gets steeper, and the averaged spectral index  $\alpha_B$  decreases from  $-1.63^{+0.09}_{-0.12}$  to  $-1.99^{+0.09}_{-0.11}$ . We also find that the averaged  
spectral index  $\alpha_B$  changes more quickly at  $I_{max} \leq 3.5$  than at  $3.5 < I_{max} \leq 15.5$ . When  $I_{max}$  gets larger, the spectral index  
stops decreasing and keeps nearly constant at  $\alpha_B \approx -2$ . However, the dependence of the spectral index on the magnetic  
compressibility seems to be not significant as shown in Figure 7 and Figure 8.

310 According to the observational result, an empirical relation is built up between the magnetic spectral index  $\alpha_B$  and the inter-  
mittency magnitude  $I_{max}$  as  $\alpha_B = 0.4 \exp(-I_{max}/5) - 2.02$ . The empirical relation is illustrated as black curve in the lower  
panel of Figure 6. It gives the continuous variation of the magnetic spectral index  $\alpha_B$  as a function of the intermittency mag-  
nitude  $I_{max}$ . This relation will help people to easily estimate the contribution of the intermittency magnitude on the magnetic  
spectral index, which implies the nature of the cascading process happening in the turbulence. It also supplies observational  
315 constraint for numerical studies related to the intermittency and spectral analysis about the solar wind turbulence. From the  
aspect of theoretical study, the relation will also help improve the turbulence theory that contains intermittent structures.

Moreover, Sari and Ness (1969) has mentioned that "The only change in the spectra for intervals containing a different  
number of discontinuities, or of discontinuities of differing magnitude, should be in the power levels, and not in the general  
spectral shape." Based on the high-resolution data and sufficient samples observed by the WIND spacecraft, our result here  
320 provide the observational evidence that the magnetic spectral shape (i.e., the spectral index in the inertial range) actually  
changes when the intermittency magnitude of interval is different. So, when people try to study the cascading process and  
evolution of the solar wind turbulence, it is very necessary to consider the effect of the intermittency magnitude. In the future,  
we will also investigate the influence of the number of intermittent structures on the spectral shape. Additionally, it will be  
also interesting to know the physical nature of these intermittent structures found in the slow-wind streams, and to compare the  
325 result with that in the fast-wind streams (Wang et al., 2013).



*Data availability.* WIND data are downloaded from SPDF (<http://spdf.gsfc.nasa.gov>). The magnetic field data used in this work include 3s-resolution (WI\_H0\_MFI) and high-resolution (WI\_H2\_MFI) data measured by Magnetic Fields Investigation between 2005 and 2013. The plasma data used here include 3s-resolution ion moments (WI\_PM\_3DP) measured by 3D Plasma Analyzer between 2005 and 2013.

*Author contributions.* XW had the main responsibility of the data analysis and writing of the article. XHF also participated in the data analysis. YXW, HHW and LZ participated in the discussion and interpretation of the results, as well as editing of the manuscript text.

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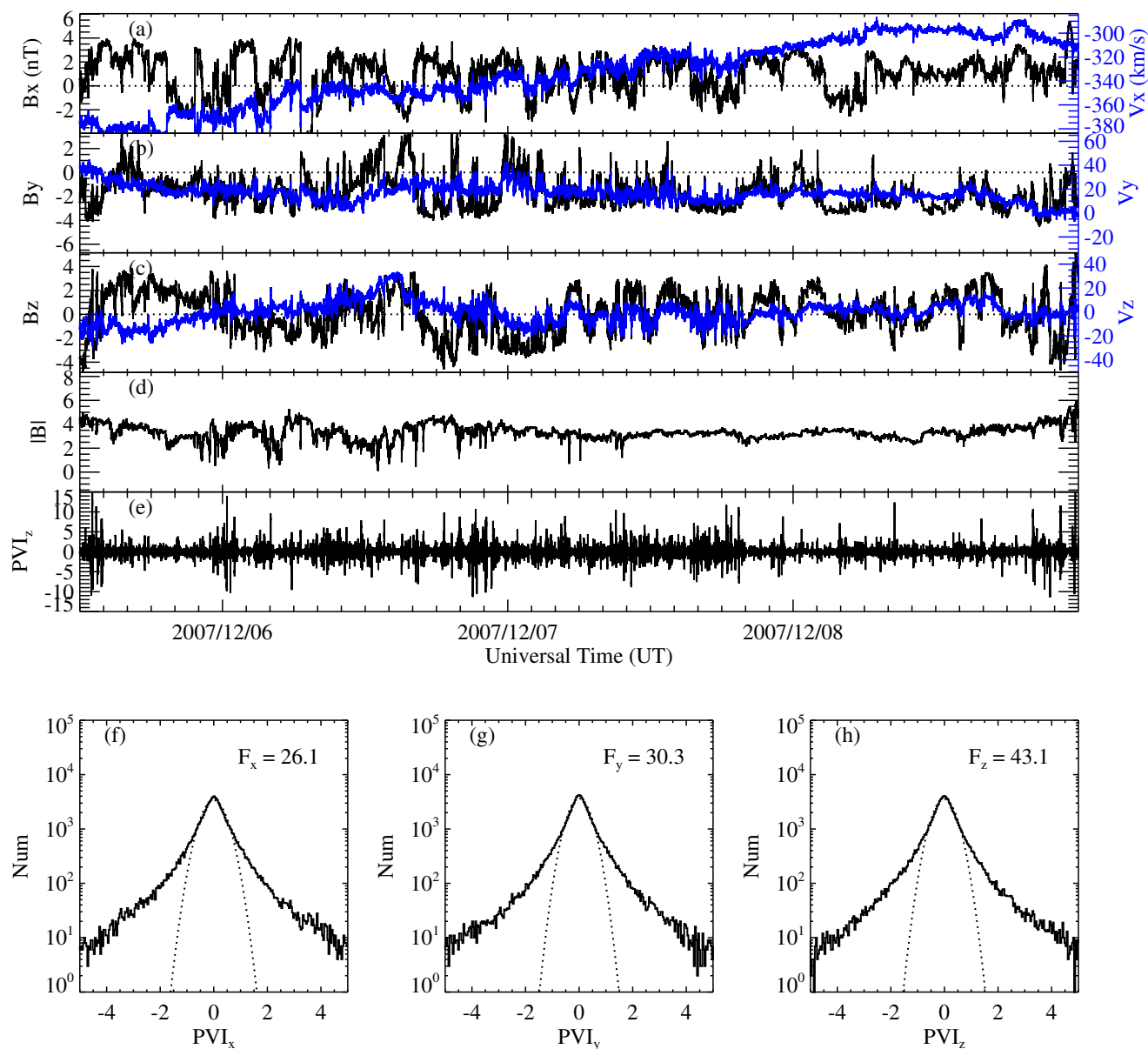
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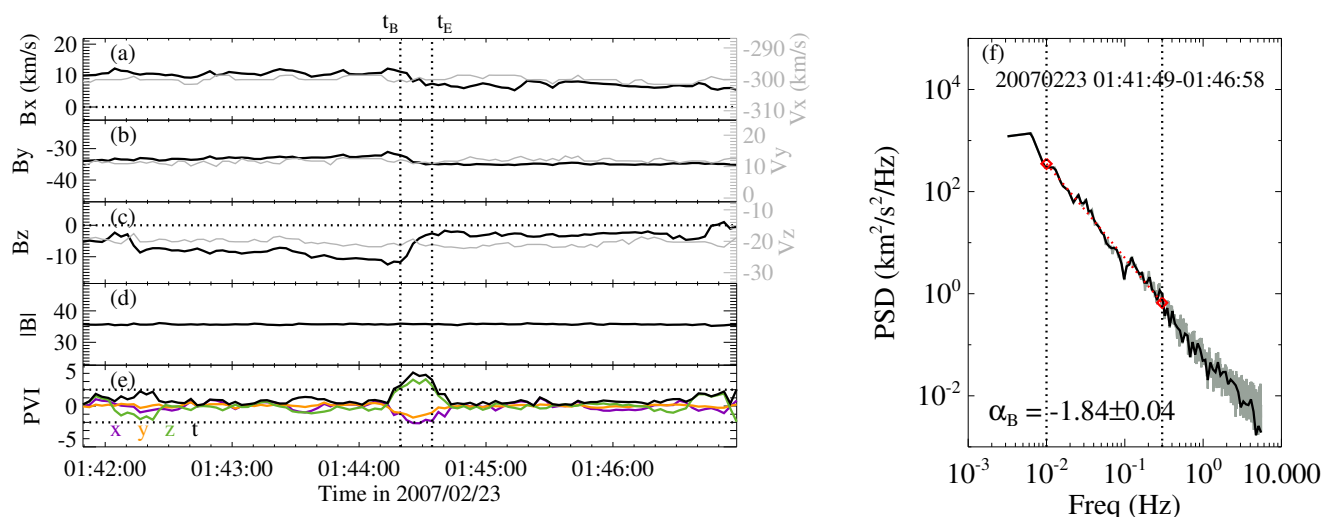


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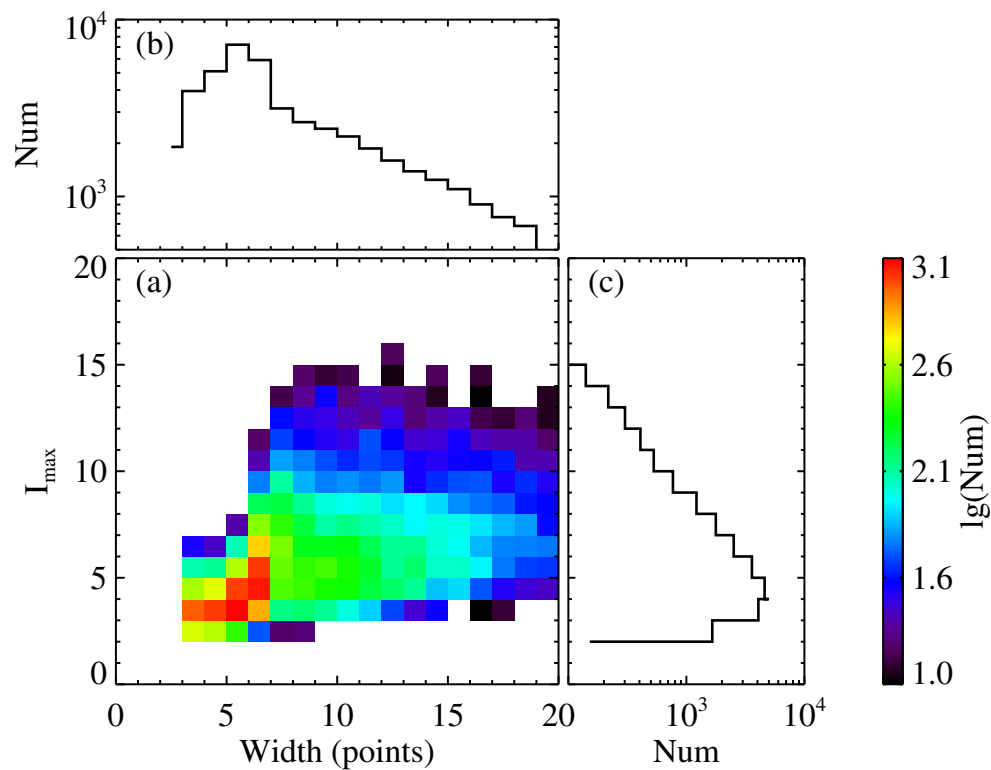


**Figure 1.** A typical slow-wind stream observed from 12:00:00 UT on 5 Dec 2007 to 00:00:00 UT on 9 Dec 2007 by the WIND spacecraft at the L1 point. (a-c) Time variations of the three components of magnetic field vector (black) and proton velocity vector (blue) in the GSE coordinates. Horizontal dotted lines correspond to 0 nT. (d) Magnetic field magnitude. (e) Normalized partial variance of increments ( $PVI$ ) for the  $z$  component of the magnetic field vector at the time scale of  $\tau = 24$  s. (f-h) Probability distribution function (PDF, solid black curves) of  $PVI$  for the three components of magnetic field, respectively. Flatness  $F_i$  ( $i = x, y, z$ ) of each distribution is marked in each panel. Dotted curves denote standard Gaussian distribution.

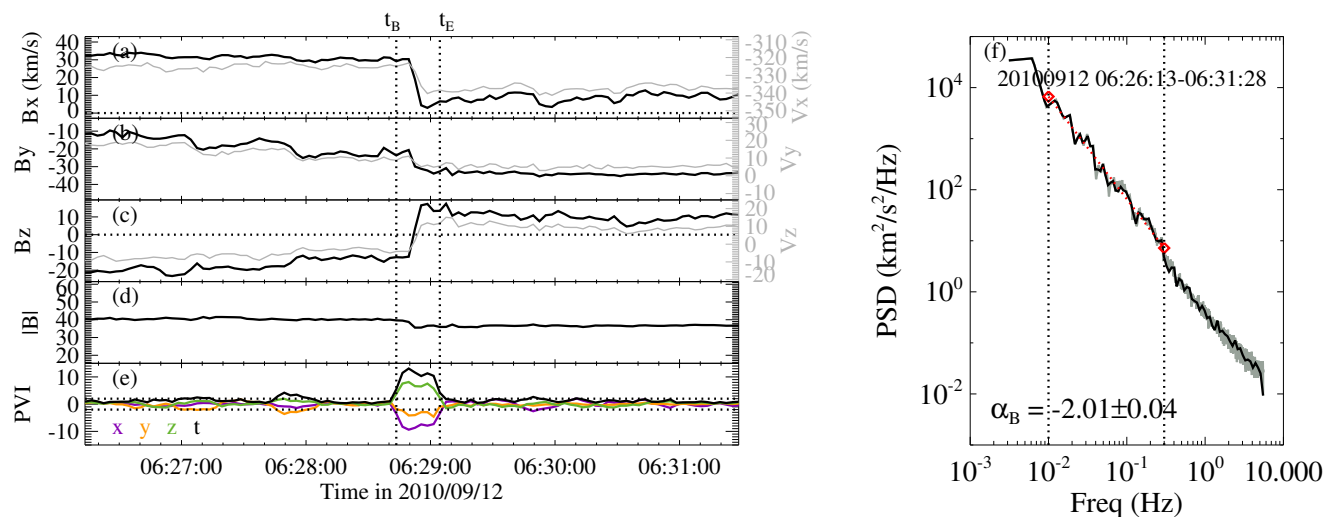




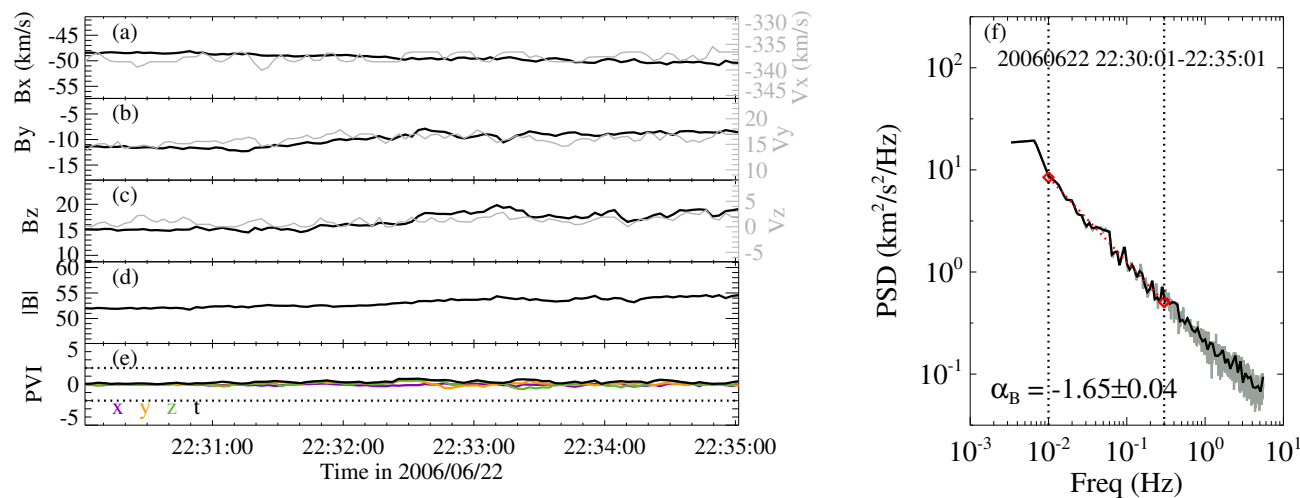
**Figure 2.** A typical case of intermittent interval observed by the WIND spacecraft at 01:41:49–01:46:58 on 2007 Feb 23. (a–c) Time variations of the magnetic field vector (black) and the proton velocity vector (gray) in the GSE coordinates. The magnetic field is plotted in the Alfvén speed unit. (d) Magnetic field magnitude in the Alfvén speed unit. (e) Normalized partial variance of increments ( $PVI$ ) for the magnetic field vector at the time scale of  $\tau = 24$  s, with  $PVI_x$  in purple,  $PVI_y$  in orange,  $PVI_z$  in green, and matrix trace of  $PVI$  in black. The two horizontal lines correspond to  $|PVI| = 2$  that used to search for the intermittent structure. The two vertical dotted lines mark the beginning time ( $t_B$ ) and the ending time ( $t_E$ ) of the intermittent structure, respectively. (f) Spacecraft-frame trace power spectra of magnetic field. The gray curve corresponds to the power spectrum obtain from performing FFT on the high-resolution magnetic field data with  $\Delta T = 1/11$  s. The black curve superposed on the gray one corresponds to the uniformly distributed spectrum after interpolation. The spectral index and its uncertainty shown are obtained from applying a least-squares fit to the interpolated spectrum, resulting in the straight line (red dotted line) over the frequency range from 0.01 Hz to 0.3 Hz (between the two vertical dotted lines).



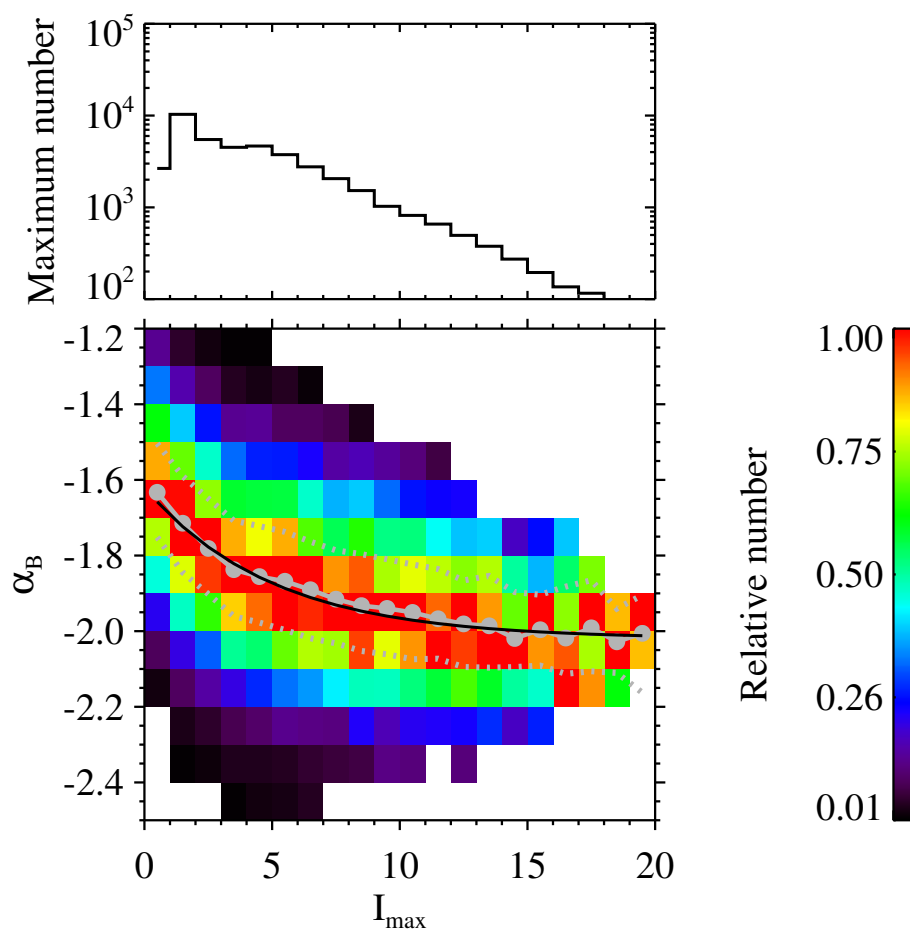
**Figure 3.** (a) Joint distribution of intermittency magnitude ( $I_{max}$ ) and width for the selected intermittent structures. The pixels containing no more than 10 cases are ignored. (b) Probability distribution of the width. (c) Probability distribution of the intermittency magnitude ( $I_{max}$ ).



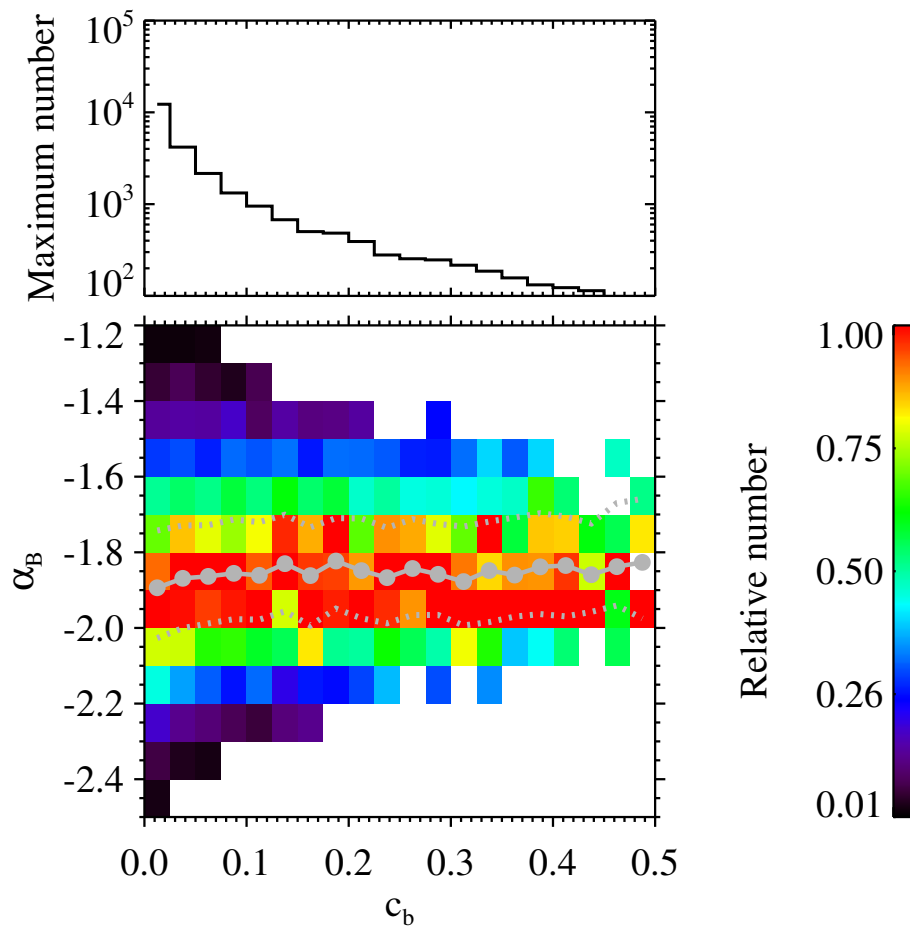
**Figure 4.** A typical case of intermittent interval observed by the WIND spacecraft at 06:26:13–06:31:28 on 2010 Sep 12 in the same format as Figure 2.



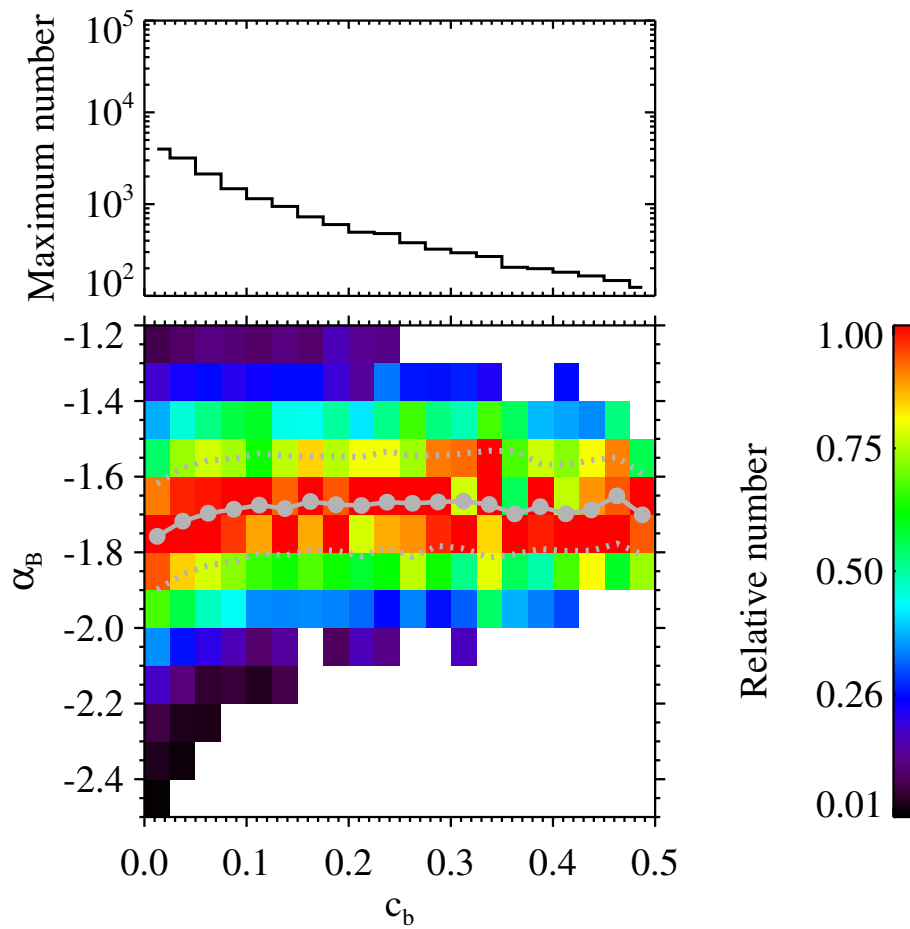
**Figure 5.** A typical case of quiet interval observed by the WIND spacecraft at 22:30:01–22:35:01 on 2006 Jun 22 in the same format as Figure 2. The fluctuation amplitude of the proton velocity (gray curves in panels (a)(b)(c)) is very close to the instrument noise level ( $2 \text{ km s}^{-1}$ ) in the 3DP velocity observations (Wicks et al., 2013a). Thus, the variations of the proton velocity look noisy here.



**Figure 6.** Joint distribution of intermittency magnitude  $I_{max}$  and spectral index  $\alpha_B$  for the selected 42,272 intervals. The bin width of  $I_{max}$  is 1, and the bin width of  $\alpha_B$  is 0.1. For a given pixel, the color denotes relative number, which is the number of the cases normalized by the maximum number among the corresponding column ( $I_{max}$  bin). The pixels containing no more than 10 cases are ignored. The gray solid circles represent the average  $\alpha_B$  in each  $I_{max}$  bin. The dotted gray lines represent the upper/lower quartiles. The black curve, corresponding to the exponential function  $\alpha_B = 0.4 \exp(-I_{max}/5) - 2.02$ , represents the fitting result to the gray solid circles.



**Figure 7.** Joint distribution of magnetic compressibility  $c_b$  and spectral index  $\alpha_B$  for the selected 24,886 intermittent intervals in the same format as Figure 6.



**Figure 8.** Joint distribution of magnetic compressibility  $c_b$  and spectral index  $\alpha_B$  for the selected 17,386 quiet intervals in the same format as Figure 6.