



Virtual sounding of solar-wind effects on the AU and AL indices based on an echo state network model

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Abstract. The properties of the auroral electrojets are examined on the basis of a trained machine learning model. The relationships between solar-wind parameters and the AU and AL indices are modeled with an echo state network (ESN), a kind of recurrent neural network. We can consider this trained ESN model to represent nonlinear effects of the solar-wind inputs on the auroral electrojets. To identify the properties of auroral electrojets, we obtain various synthetic AU and AL data by using various artificial inputs with the trained ESN. The analyses of various synthetic data show that the AU and AL indices are mainly controlled by the solar-wind speed in addition to B_z of the interplanetary magnetic field (IMF) as suggested by the literature. The results also indicate that the solar-wind density effect is emphasized when solar-wind speed is high and when IMF B_z is near zero. This suggests some nonlinear effects of the solar-wind density.

1 Introduction

The AU and AL indices (Davis and Sugiura, 1966; World Data Center for Geomagnetism, Kyoto et al., 2015) represent the strengths of eastward and westward electrojets, respectively, and are widely used for monitoring geomagnetic activity in the auroral region. It is widely accepted that the behavior of the westward electrojet is mostly controlled by the solar wind input into the magnetosphere, and there are various models for representing the relationship between the AU and AL indices and solar-wind parameters (e.g., Akasofu, 1981; Murayama, 1982; Newell et al., 2007). When modeling the temporal evolution of these indices, it is important to consider nonlinear processes of the auroral electrojets. To describe the complicated processes of the indices, Luo et al. (2013) constructed a parametric model with many parameters. Machine learning approaches are also used in many studies to describe the nonlinear evolution of the auroral electrojets. For example, Chen and Sharma (2006) employed the weighted nearest neighbors method for predicting the AL index during storm times. In particular, artificial neural networks are frequently used for modeling the AU , AL , and AE indices. It has been demonstrated that the AU , AL , and AE indices can be predicted well with feed-forward neural networks using time histories of solar-wind parameters as inputs (e.g., Gleisner and Lundstedt, 1997; Takalo and Timonen, 1997; Pallochia et al., 2008; Bala and Reiff, 2012). Recurrent types of neural networks are also useful for representing dynamical behaviors of the magnetosphere (Gleisner and Lundstedt, 2001).



Amariutei and Ganushkina (2012) predicted the AL index using a model which combines the autoregressive moving average with the exogenous inputs (ARMAX) model and a neural network.

25 While machine learning techniques tend to be used for predictions with high accuracy, the learned relationships between solar-wind inputs and auroral electrojets are of interest from the scientific perspective as well. As trained machine learning models can describe the nonlinear behaviors of the magnetospheric system, it is meaningful to analyze the input–output relationships of the trained models. Recently, Blunier et al. (2021) have identified solar-wind parameters which affect the value of geomagnetic indices by putting perturbed inputs into a trained neural network. This study takes a somewhat similar approach.
30 We employ an echo state network (ESN) model (Jaeger, 2001; Jaeger and Haas, 2004; Chattopadhyay et al., 2020), which is a kind of recurrent neural network, to describe the relationship between various solar-wind parameters and the auroral electrojet indices AU and AL . We then virtually sound the responses of the AU and AL indices to solar-wind inputs by putting various artificial inputs into the trained ESN model and identify the properties of the auroral electrojets.

2 Echo state network

35 We model the temporal evolution of AU and AL with the ESN model because it can be easily implemented to attain a satisfactory performance. The ESN is a kind of recurrent neural network with fixed random connections and weights between hidden state variables. Only the weights for the output layer are trained so that the target temporal pattern is well reproduced. We combine the state variables at the time t_k into a vector \mathbf{x}_k , where the i -th element of \mathbf{x}_k is denoted as $x_{k,i}$. The number of state variables m is set at 1200 in this study. At the time step k , we update $x_{k,i}$ as follows:

$$x_{k,i} = \alpha x_{k-1,i} + (1 - \alpha) \tanh(\mathbf{w}_i^T \mathbf{x}_{k-1} + \mathbf{u}_i^T \mathbf{z}_k + \eta_i) \quad (1)$$

40 where \mathbf{z}_k is a vector consisting of the input variables. The weights \mathbf{w}_i and \mathbf{u}_i determine the connection with the other state variables and input variables. The weights \mathbf{w}_i and the parameter η_i are given in advance and are fixed.

It is desirable that the weights are given so as to attain the so-called ‘echo state property’. The echo state property guarantees that the ESN forgets distant past inputs. Defining the weight matrix W as

$$W = (\mathbf{w}_1 \ \mathbf{w}_2 \ \cdots \ \mathbf{w}_m), \quad (2)$$

a sufficient condition for the echo state property is that the maximum singular value of W is less than 1. If a certain matrix W' is given and its maximum singular value λ' is computed, we can obtain the weight matrix W which satisfies this sufficient condition as follows:

$$W = \frac{\alpha}{\lambda'} W'. \quad (3)$$

We thus first determine W' randomly and obtain the weight W according to Eq. (3) with the parameter α set to 0.99. In this study, we set 90% of the elements of W' to be zero. Each of the remaining non-zero elements comprising 10% of W' is obtained randomly from a Laplace distribution for which the probability density function $p(x)$ is written as

$$p(x) = \frac{1}{2} \exp(-|x|). \quad (4)$$



50 Similarly to W' , 90% of the elements of \mathbf{u}_i are set to be zero and the other non-zero elements are given by the same Laplace distribution. The parameter η_i in Eq. (1) is obtained randomly from a normal distribution with mean 0 and standard deviation 0.3.

The output for the time t_k , \mathbf{y}_k , is obtained from \mathbf{x}_k as follows:

$$\mathbf{y}_k = \beta^T \mathbf{x}_k. \quad (5)$$

The weight β in Eq. (5) is determined so that the objective function

$$J = \sum_{k=1}^K \|\mathbf{d}_k - \mathbf{y}_k\|^2 \quad (6)$$

55 is minimized, where \mathbf{d}_k is an observation vector consisting of the observed data. The present study aims to model the temporal pattern of the AU and AL indices. Accordingly, the output vector \mathbf{y}_k consists of two elements as follows

$$\mathbf{y}_k = \begin{pmatrix} y_{AU,k} \\ y_{AL,k} \end{pmatrix}, \quad (7)$$

where $y_{AU,k}$ and $y_{AL,k}$ are the predicted AU and AL values at t_k , respectively. In this study, 5-minute values (averages for 5 minutes) of AU and AL are used. We give the input vector \mathbf{z}_k as follows:

$$\mathbf{z}_k = \begin{pmatrix} B_{z,k} \\ B_{y,k} \\ V_{sw,k} \\ N_{sw,k} \\ \cos(2\pi H_k/24) \\ \sin(2\pi H_k/24) \\ \cos(2\pi D_k/364.24) \\ \sin(2\pi D_k/364.24) \\ y_{AU,k-1} \\ y_{AL,k-1} \end{pmatrix} \quad (8)$$

60 where $B_{z,k}$ and $B_{y,k}$ denote the z and y component of the interplanetary magnetic field in the geocentric solar magnetic (GSM) coordinates at time t_k , $V_{sw,k}$ is the $-x$ component of the solar wind velocity in the GSM coordinates, $N_{sw,k}$ is the solar wind density, H_k is universal time (UT) in hour, and D_k is the day from the end of 2000 ($D_k = 1$ on January 1, 2001). The variables H_k and D_k are included for considering UT dependence and seasonal dependence (e.g., Cliver et al., 2000). The feedback of the predicted AU and AL indices which can be obtained using Eq. (5) is also included in the input vector \mathbf{z}_k . The solar wind variables $B_{z,k}$, $B_{y,k}$, $V_{sw,k}$, and $N_{sw,k}$ are taken from the OMNI 5-minute data.

65 If \mathbf{z}_k does not contain the feedback of $y_{AU,k-1}$ and $y_{AL,k-1}$, the weight β can be determined through simple linear regression because \mathbf{x}_k at each time step would not depend on β in Eq. (5). However, since the feedback of $y_{AU,k-1}$ and $y_{AL,k-1}$ are



contained, the optimal β cannot be obtained by linear regression. We thus obtained β using the ensemble-based optimization method (Nakano, 2021).

3 Performance of ESN

70 We trained the ESN using data obtained over a period of ten years from 2005 to 2014. We used 5-minute values of the OMNI solar wind data and the AU and AL indices provided by Kyoto University. Since the ESN memorizes the history of the input data, the ESN output should be compared with the observation after referring to the input data for the preceding several time steps. We then start the comparison after spin-up of the ESN for 72 steps, which corresponds to 6 hours for the 5-minute values, from the initial time of the analysis. It should also be noted that solar wind data are sometimes incomplete. If more than half
75 of the data were missing for 1 hour, we stopped the prediction and spun up the ESN again for the subsequent 72 steps.

We then reproduced the AU and AL indices for the period from 1998 to 2004 and compared the outputs with the observed values. In Figure 1, the top panel shows the AU and AL reproduced by our ESN model in October 1999 with red lines and the observed AU and AL indices with gray lines for the same period. The second panel shows the three components of the IMF. The green, blue, and red lines indicate the x , y , and z components in (GSM) coordinates, respectively. The third panel shows
80 the solar wind speed and the fourth panel shows the solar wind density. The bottom panel shows the $SYM-H$ index (Iyemori, 1990; Iyemori and Rao, 1996) for the corresponding time period. High auroral activity was maintained for the period from 10 October to 17 October when high speed solar wind streams coincided with a continual southward IMF, as suggested by the literature (e.g., Tsurutani et al., 1990, 1995). The auroral activity was also enhanced during a magnetic storm from 21 October. The model outputs mostly reproduced the observed AU and AL values well for these events.

85 Table 1 shows the root-mean-square errors (RMSE) of the ESN prediction for each year of the period from 1998 to 2004. The RMSEs were less than 100 nT for the AL index and about 50 nT for the AU index except for 2003. The RMSEs of AU and AL were larger in 2003 than in other years likely because of high auroral activity during that year. Figure 2 shows the means of the $|AU|$ and $|AL|$ values for each month from 1998 to 2004. The mean of $|AL|$ exceeded 200 nT in most of the months in 2003, which indicates high activity of the westward auroral electrojet. The mean of $|AU|$ also tended to be larger in
90 2003 than in the other years. In the model of Luo et al. (2013), which predicted the 10-minute values of the AE indices from solar wind parameters, the RMSEs were 83.8, 125.5, and 102.0 nT in 2002, 2003, and 2004, respectively, for the AL index and 44.5, 58.7, and 47.7 nT in 2002, 2003, and 2004 for the AU index. Our ESN model thus achieves an accuracy comparable to the model of Luo et al.. While Luo et al. used 10-minute values, this study uses 5-minute values in the prediction. Considering that data with a higher time resolution tend to contain larger noise, we believe that the ESN meets a satisfactorily high accuracy
95 for the prediction of the AE indices.

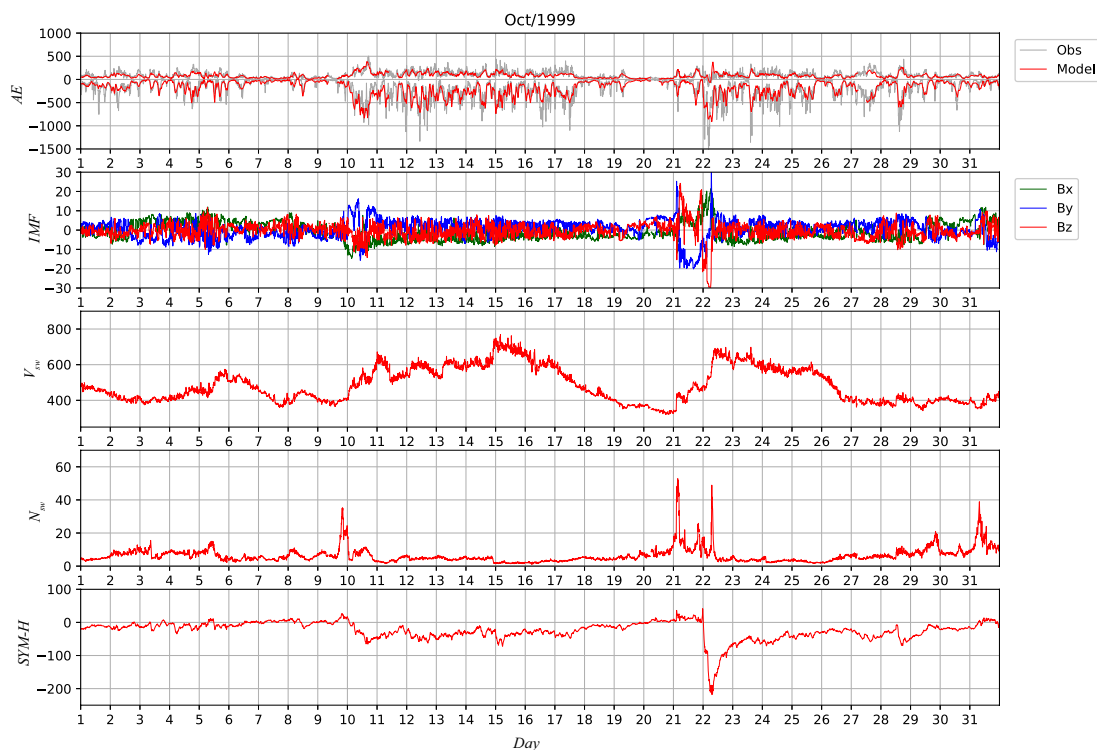


Figure 1. The top panel shows the AU and AL values for October 1999 reproduced with the ESN model (red) and the observed AU and AL indices (gray). The second panel shows the IMF B_x (green), B_y (blue), and B_z (red) in GSM coordinates. The third panel shows the solar wind speed, the fourth panel shows the solar wind density, and the bottom panel shows the $SYM-H$ index.

Table 1. The root-mean-square errors (in nT) for the AL and AU indices.

Year	RMSE (AL)	RMSE (AU)
1998	101.19	46.09
1999	88.04	47.08
2000	99.10	58.20
2001	96.75	53.36
2002	89.90	50.52
2003	118.62	63.50
2004	99.84	47.72

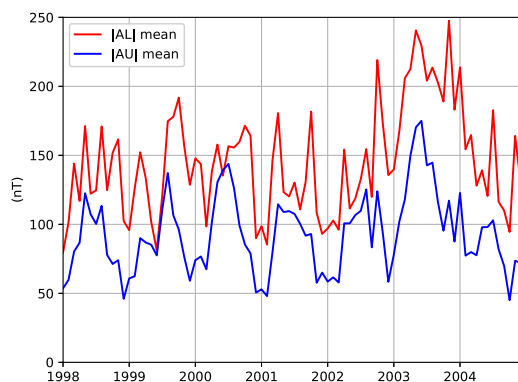


Figure 2. The means of $|AU|$ and $|AL|$ for each month from 1998 to 2004.

4 Responses to synthetic solar wind

Machine learning models including the ESN model can be regarded as nonlinear regression models for summarizing the relationship between an input and an output. Although there is a misfit between the ESN output and the observation, the ESN would learn the properties of the magnetospheric system which affect the auroral electrojets. As the ESN model is a ‘black-box’ model, we cannot directly extract the input-output relationships in a functional form. However, we can virtually sound the responses of the AU and AL indices to various solar-wind inputs. If we put artificial inputs into the trained ESN model, we obtain synthetic AU and AL indices as outputs of the model under the given inputs. We can then identify properties of the auroral electrojets by analyzing the synthetic indices obtained from various artificial inputs.

We obtained synthetic AU and AL indices by the ESN with an artificial input where the value of one of the solar-wind parameters was fixed. For example, we turned off the variation of IMF B_x by fixing it at a constant 0 nT and derived synthetic AU and AL indices where the B_x effect was excluded. We then compared the synthetic indices with the observed indices for each year to evaluate the impact of IMF B_x . Similarly, we obtained synthetic indices which exclude each of the effects of IMF B_y , solar-wind speed, solar-wind density, and solar-wind temperature, and evaluated the impact of each parameter for each year. The fixed values of IMF B_y , solar-wind speed, solar-wind density, and solar-wind temperature were 0 nT, 400 km/s, 1/cc, and 2×10^5 K, respectively. We did not consider the case where the IMF B_z effect was turned off because the RMSE becomes very large without an accurate IMF B_z input, as obviously expected from the results of many previous studies (e.g., Arnoldy, 1971; Akasofu, 1981; Murayama, 1982; Newell et al., 2007).

Figures 3 and 4 show the RMSE and mean deviation values in each year for the various synthetic AL indices where the effect of one of the solar-wind parameters was excluded. In each figure, the red lines show the RMSEs for the output of ESN using all the solar-wind parameters described in Eq. (8). The green and blue lines show the RMSEs when the effects of IMF B_x and B_y were excluded, respectively. The orange, light blue, and gray lines show the respective RMSEs when the effects



of solar-wind speed, density, and temperature were excluded. To evaluate the uncertainty, we prepared 10 data sets, each of which was obtained by leaving out the data for one of the ten years from 2005 to 2014 and calculated the weights β in Eq. (5) using each of the 10 data sets. We then obtained the synthetic AU and AL indices using the ESN with each of these different 10 weight values. The solid lines in Figure 3 and 4 show the mean values for the 10 synthetic AU and AL indices. The dashed lines indicate the maxima and minima among the 10 outputs. Among the six solar-wind parameters, the effect of solar-wind speed is prominent especially in 2003, when some severe magnetic storms were observed, presumably because it contributes to the efficiency of the coupling between the solar wind and the Earth's magnetosphere (e.g., Akasofu, 1981; Murayama, 1982; Newell et al., 2007). The mean deviation shown in Figure 4 indicates the bias of the ESN output, and the positive bias means that the ESN output tends to be larger than the observed AL value, which corresponds to an underestimation of $|AL|$. The large positive bias for the case without solar-wind speed variation in Figure 4 thus suggests that a low solar-wind speed results in a small $|AL|$. Conversely, a high solar-wind speed activates variations of AL . We can also observe a relatively small effect of IMF B_y , which would also contribute to the coupling between the solar wind and the magnetosphere. In addition, the effect of the solar-wind density can be seen for all of the years from 1998 to 2004. The large mean deviation suggests that the solar-wind density enhancement intensifies the westward electrojet as implied by some earlier studies (Newell et al., 2008; McPherron et al., 2015).

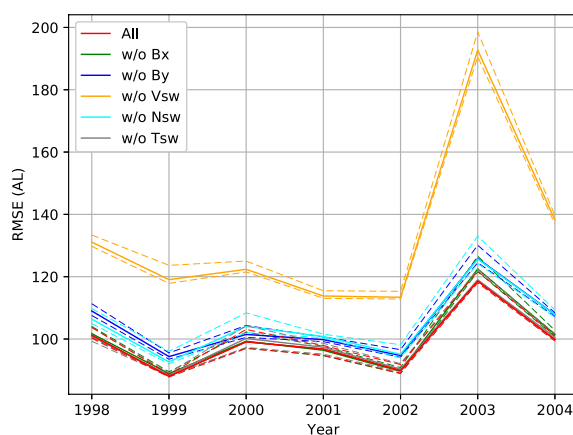


Figure 3. RMSE in each year for the various synthetic AL indices where the effect of one of the solar-wind parameters was excluded.

Figures 5 and 6 show the RMSE and the mean deviation values for the various synthetic AU indices. Each color indicates the result with the same input as the corresponding color in Figure 3. The solar-wind speed effect is again prominent. The large negative bias for the case without solar-wind speed variation in Figure 6 suggests a low solar-wind speed underestimates the AU value. In contrast with AL , AU is likely to be strongly controlled by IMF B_y and the solar-wind density. In particular, the mean deviation is largely negative for the case without density variation, which suggests an important effect of solar-wind density on the AU index, as discussed by Blunier et al. (2021).

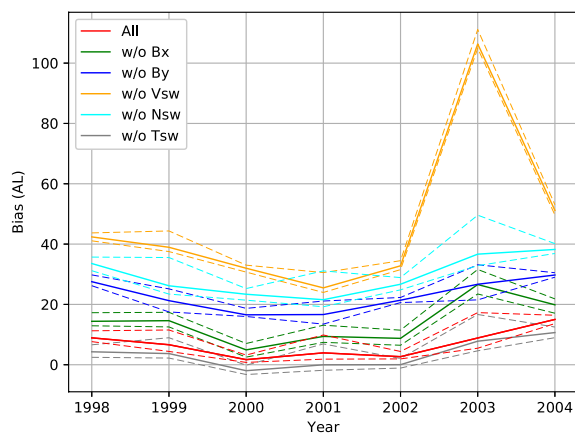


Figure 4. Mean deviation in each year for the various synthetic AL indices where the effect of one of the solar-wind parameters was excluded.

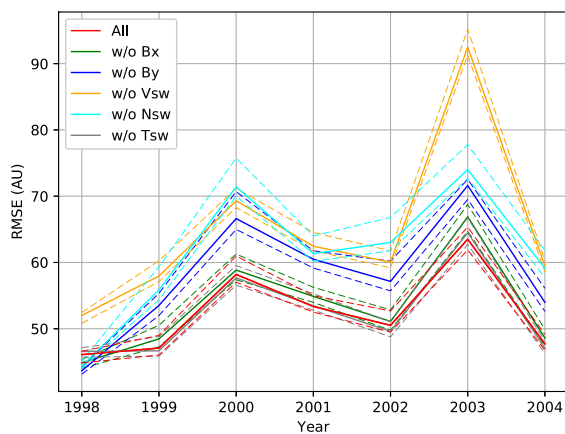


Figure 5. RMSE in each year for the various synthetic AU indices where the effect of one of the solar-wind parameters was excluded.

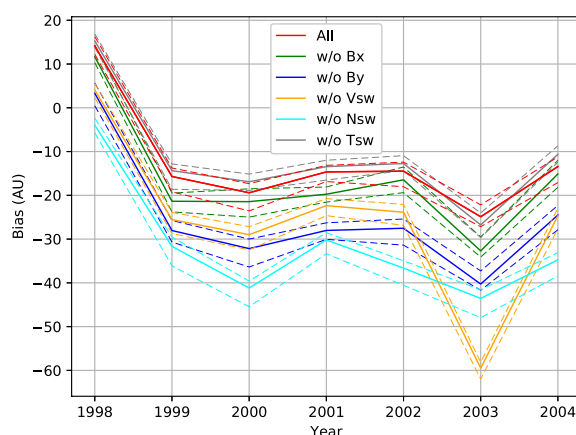


Figure 6. Mean deviation in each year for the various synthetic AU indices where the effect of one of the solar-wind parameters was excluded.

The top panel in Figure 7 shows some of the synthetic AU and AL indices from 21 October to 25 October in 1999. The red lines indicate the output where all of the parameters in Eq. (8) were used. The green and blue lines indicate the synthetic values where solar-wind speed and density was turned off, respectively. The gray lines show the observed actual AU and AL indices for reference. The other panels in this figure are the same as those in Figure 1. Although the ESN output is much smoother than the observation, especially in some impulsive events which would be related to substorms, the red line reproduces the observed AU and AL indices well. In contrast, when the solar-wind speed was set to be low at 400 km/s, the ESN model clearly underpredicted the strength of AL . This suggests that a high-speed solar wind makes an important contribution to enhancing the westward electrojet. When the density effect was turned off, the ESN tended to slightly underpredict $|AL|$ although the density effect was likely to be minor in this event.

Figure 8 shows the result for another event from 26 July to 30 July in 2000. In this event, since the solar-wind speed was maintained at around 400 km/s, which we set as the base level of the solar-wind speed, the green line was similar to the red line. On the other hand, the solar-wind density effect is visible. If the density is fixed at $1/cc$, the ESN tended to underpredict $|AU|$ and $|AL|$. However, the relationships with the solar-wind density learned by the ESN seemed to not be linear. For example, the difference between the red and blue lines tended to be larger on 29 July than on 28 July while the solar-wind density was more enhanced on 28 July than on 29 July. This might suggest some compound effects of the solar-wind density and other parameters.

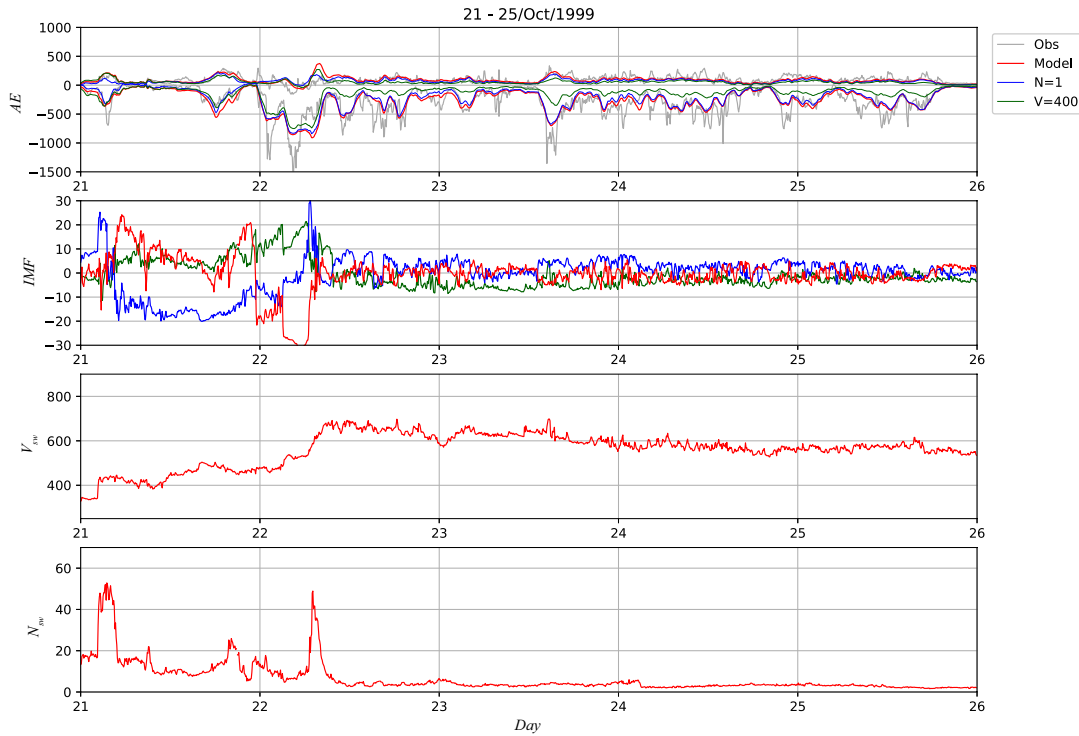


Figure 7. Comparison of some ESN outputs during the period from 21 October to 25 October 1999. The top panel shows the ESN output with all the parameters (red), the synthetic indices where the solar-wind speed effect was turned off (green), those where the solar-wind density effect was turned off (blue), and the observed AU and AL indices (gray). The second panel shows the IMF B_x (green), B_y (blue), and B_z (red) in GSM coordinates. The third panel shows the solar wind speed, the fourth panel shows the solar wind density, and the bottom panel shows the $SYM-H$ index.

We closely examined the density effects learned by the ESN by computing other synthetic indices $AU(N = 20)$ and $AL(N = 20)$, obtained by fixing the solar-wind density input of the ESN at $20 / \text{cc}$. We then obtained the differences

$$\Delta AU_{N_{\text{eff}}} = AU(N = 20) - AU(N = 1),$$

$$\Delta AL_{N_{\text{eff}}} = AL(N = 20) - AL(N = 1)$$

where $AU(N = 1)$ and $AL(N = 1)$ are the synthetic AU and AL indices obtained by fixing the solar-wind density at $1 / \text{cc}$. We then used $\Delta AU_{N_{\text{eff}}}$ and $\Delta AL_{N_{\text{eff}}}$ as proxies of the solar-wind density effect as a function of time. Figure 9 is a 2-dimensional histogram to compare $\Delta AU_{N_{\text{eff}}}$ and $\Delta AL_{N_{\text{eff}}}$ with the solar-wind speed. As the solar-wind speed increases, $\Delta AU_{N_{\text{eff}}}$ increases and $\Delta AL_{N_{\text{eff}}}$ decreases. This suggests that the solar-wind density effect on the auroral electrojets is not independent of the solar-wind speed effect but that the solar-wind density contributes to the auroral electrojet intensity more effectively under high solar-wind speed conditions. The solar-wind density effect is likely to be small when the solar-wind



speed is low. Figure 10 is a 2-dimensional histogram to compare $\Delta AU_{N_{\text{eff}}}$ and $\Delta AL_{N_{\text{eff}}}$ with IMF B_z . The solar-wind density effect gets large when IMF B_z is near zero. The density effect is small on average when $|B_z|$ is large. The ESN model therefore suggests that the solar-wind density effect is most important when IMF B_z is small.

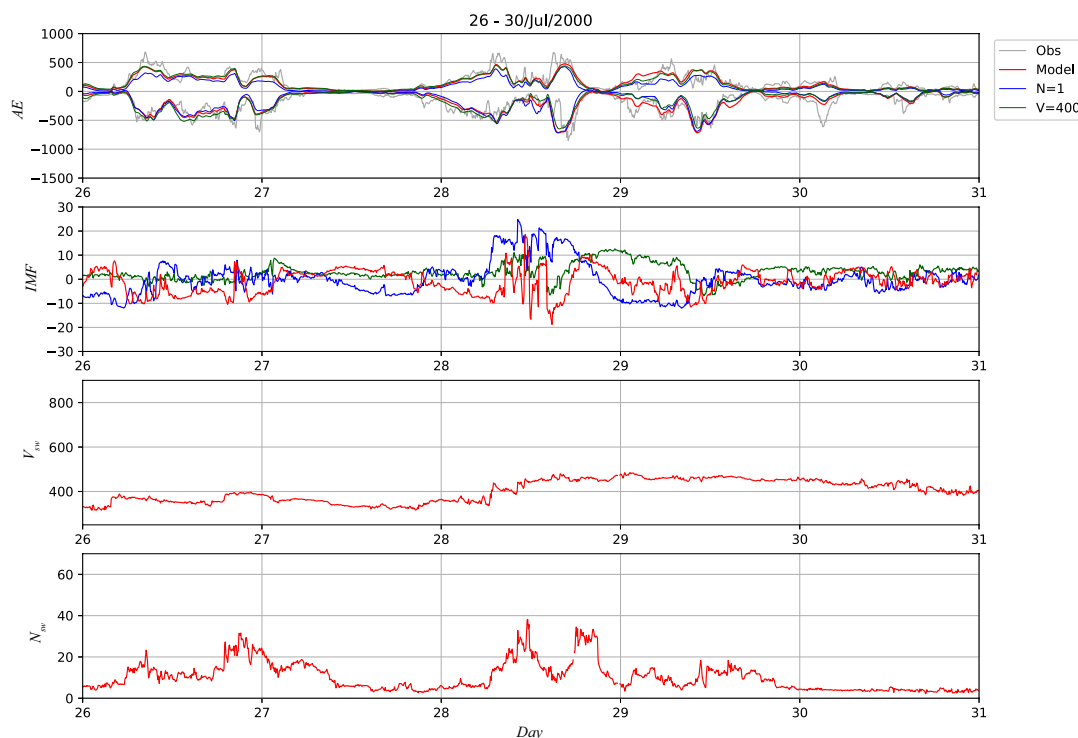


Figure 8. Comparison of ESN outputs during the period from 26 July to 30 July 2000 in the same format as Figure 7.

165 5 Discussion

It is widely accepted that auroral electrojets are mainly controlled by IMF and the solar-wind speed (e.g., Akasofu, 1981; Murayama, 1982; Newell et al., 2007). In particular, IMF B_z has an essential effect on auroral activity. When IMF is directed southward, DP2 type electrojets (e.g., Kamide and Kokubun, 1996) are enhanced and contribute to both AU and AL . The substorm current wedge, which contains a westward electrojet contributing to the AL index, would also be controlled by IMF (e.g., Kepko et al., 2015). As illustrated in Figure 1, the solar-wind speed also has an important effect.

Although the solar-wind density effect is sometimes ignored when modeling the AU and AL indices, Gleisner and Lundstedt (1997) reported that the performance of a neural network for modeling the AE index is improved by considering the solar-wind density effect. McPherron et al. (2015) also suggested a contribution from the solar wind density to the AL index. Blunier et al. (2021) deduced the solar-wind parameters contributing to changes in the geomagnetic indices by using neural networks, and

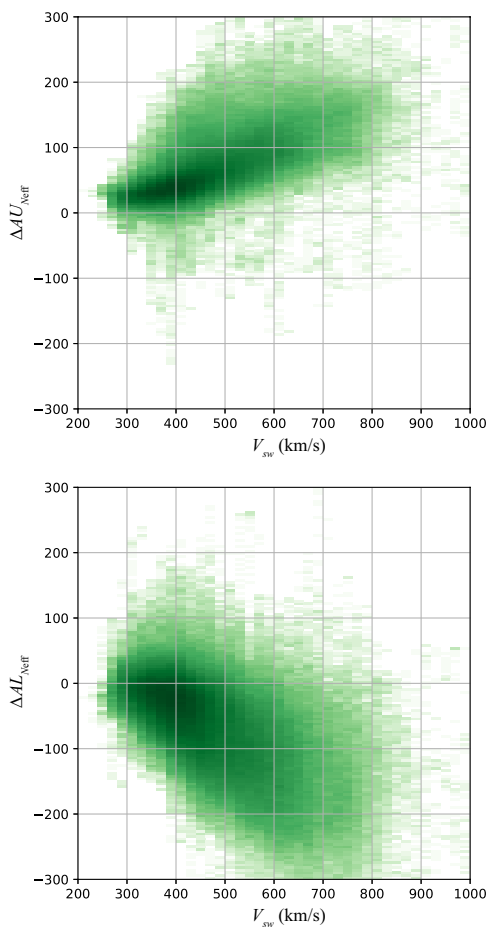


Figure 9. 2-dimensional histogram indicating the dependence of the solar-wind density effect on the solar-wind speed.

175 suggested that the solar-wind density has a more visible effect on AU than on AL . The stronger effect on AU suggested by Blunier et al. agrees with our result shown in Figure 5. Ebihara et al. (2019) conducted simulation experiments to examine the impact of various solar-wind parameters on the SML index (Newell and Gjerloev, 2011), which is an extension of the AL index calculated with data from a larger number of observatories. According to their result, the SML index depends on the solar-wind density when IMF B_z is weak, while it is not clearly affected by the solar-wind density when IMF B_z is directed strongly southward. This simulation result is consistent with our result in Figure 10. Figure 10 may thus be regarded as
180 statistical evidence of the compound effect between IMF B_z and the solar-wind density.

Figure 9 shows the compound effect between the solar wind density and velocity. One plausible explanation is the effect of the solar wind dynamic pressure which is proportional to $N_{sw} V_{sw}^2$. As some studies have suggested that field-aligned currents around the auroral latitudes are influenced by the solar-wind dynamic pressure (Iijima and Potemra, 1982; Wang et al., 2006; Nakano et al., 2009; Korth et al., 2010), it is possible that the enhancement of the field-aligned currents increases the auroral
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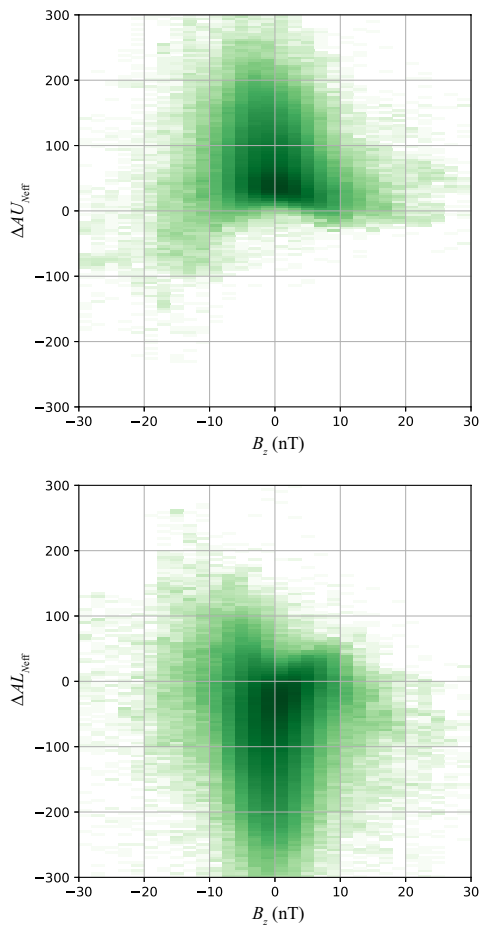


Figure 10. 2-dimensional histogram indicating the dependence of the solar-wind density effect on IMF B_z .

electrojets. In Figure 9, however, the density effect disappears when the solar wind velocity is around 300 km/s, which does not seem to be explained by the solar-wind dynamic pressure effect. This problem might be solved by considering the contribution of the plasma sheet condition. Sergeev et al. (2014, 2015) suggests that the plasma sheet temperature and density may affect the ionospheric conductivity in the region of the westward electrojet which the AL index represents. It has been suggested that
190 the plasma sheet temperature and density depend on the solar-wind velocity and density, respectively (Terasawa et al., 1997; Nagata et al., 2007). The plasma sheet effect can thus partially contribute to the relationship between AL and the solar-wind density.



6 Summary

This study modeled the temporal pattern of the AU and AL indices using ESN. Although the ESN model is relatively simple, it
195 mostly accurately reproduces the variations of the AU and AL indices. We virtually sound the properties of the magnetospheric
system by putting artificial inputs into the trained ESN model. Our virtual sounding results show a strong impact of the solar-
wind speed which was previously observed in the literature. It is also suggested that IMF B_y and the solar-wind density have
significant effects, especially on the AU index. These results are consistent with other studies. In addition, an analysis of the
synthetic AU and AL indices obtained from the artificial inputs suggests that the solar-wind density does not have a simple
200 linear effect on AU and AL , but rather that some compound processes exist. According to the results, the solar-wind density
contributes to the auroral electrojet intensity more effectively under high solar-wind speed conditions and the solar-wind density
effect becomes small under low solar-wind speed conditions. The solar-wind density effect tends to be important when IMF
 B_z is near zero. The density effect is small on average when $|B_z|$ is large.

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References

- Akasofu, S.-I.: Energy coupling between the solar wind and the magnetosphere, *Space Sci. Rev.*, 28, 121–190, 1981.
- Amariutei, O. A. and Ganushkina, N. Y.: On the prediction of the auroral westward electrojet index, *Ann. Geophys.*, 30, 841–847,
210 <https://doi.org/10.5194/angeo-30-841-2012>, 2012.
- Arnoldy, R. L.: Signature in the interplanetary medium for substorms, *J. Geophys. Res.*, 76, 5189–5201, 1971.
- Bala, R. and Reiff, P.: Improvements in short-term forecasting of geomagnetic activity, *Space Weather*, 10, S06001,
<https://doi.org/10.1029/2012SW000799>, 2012.
- Blunier, S., Toledo, B., Rogan, J., and Valdivia, J. A.: A nonlinear system science approach to find the robust solar wind drivers of the
215 multivariate magnetosphere, *Space Weather*, 19, e2020SW002634, <https://doi.org/10.1029/2020SW002634>, 2021.
- Chattopadhyay, A., Hassanzadeh, P., and Subramanian, D.: Data-driven predictions of a multiscale Lorenz 96 chaotic system using machine-
learning methods: reservoir computing, artificial neural network, and long short-term memory network, *Nonlin. Processes Geophys.*, 27,
373–389, <https://doi.org/10.5194/npg-27-373-2020>, 2020.
- Chen, J. and Sharma, S.: Modeling and prediction of the magnetospheric dynamics during intense geospace storms, *J. Geophys. Res.*, 111,
225 A4209, <https://doi.org/10.1029/2005JA011359>, 2006.
- Cliwer, E. W., Kamide, Y., and Ling, A. G.: Mountain and valleys: Semiannual variation of geomagnetic activity, *J. Geophys. Res.*, 105,
2413, 2000.
- Davis, T. N. and Sugiura, M.: Auroral electrojet activity index *AE* and its universal time variations, *J. Geophys. Res.*, 71, 785–801, 1966.
- Ebihara, Y., Tanaka, T., and Kamiyoshikawa, N.: New diagnosis for energy flow from solar wind to ionosphere during substorm: Global
225 MHD simulation, *J. Geophys. Res.*, 124, 360–378, <https://doi.org/10.1029/2018JA026177>, 2019.
- Gleisner, H. and Lundstedt, H.: Response of the auroral electrojets to the solar wind modded with neural networks, *J. Geophys. Res.*, 102,
14 269–14 278, 1997.
- Gleisner, H. and Lundstedt, H.: Auroral electrojet predictions with dynamic neural networks, *J. Geophys. Res.*, 106, 24 514–24 549, 2001.
- Iijima, T. and Potemra, T. A.: The relationship between interplanetary quantities and Birkeland current densities, *Geophys. Res. Lett.*, 9, 442,
230 1982.
- Iyemori, T.: Storm-time magnetospheric currents inferred from mid-latitude geomagnetic field variations, *J. Geomag. Geoelectr.*, 42, 1249,
1990.
- Iyemori, T. and Rao, D. R. K.: Decay of the Dst field of geomagnetic disturbance after substorm onset and its implication to storm-substorm
relation, *Ann. Geophys.*, 14, 608, 1996.
- 235 Jaeger, H.: The “echo state” approach to analysing and training recurrent neural networks, in: GMD Report 148, German National Research
Center for Information Technology, 2001.
- Jaeger, H. and Haas, H.: Harnessing nonlinearity: Predicting chaotic systems and saving energy in wireless communication, *Science*, 304,
78–80, <https://doi.org/10.1126/science.1091277>, 2004.
- Kamide, Y. and Kokubun, S.: Two-component auroral electrojet: Importance for substorm studies, *J. Geophys. Res.*, 101, 13 027, 1996.
- 240 Kepko, L., McPherron, R. L., Amm, O., Apatenkov, S., Baumjohann, W., Birn, J., Lester, M., Nakamura, R., Pulkkinen, T. I., and Sergeev,
V.: Substorm Current Wedge Revisited, *Space Sci. Rev.*, 190, 1–46, <https://doi.org/10.1007/s11214-014-0124-0>, 2015.
- Korth, H., Anderson, B. J., and Waters, C. L.: Statistical analysis of the dependence of large-scale Birkeland currents on solar wind param-
eters, *Ann. Geophys.*, 28, 51500 530, <https://doi.org/10.5194/angeo-28-515-2010>, 2010.



- Luo, B., Li, X., Temerin, M., and Liu, S.: Prediction of the *AU*, *AL*, and *AE* indices using solar wind parameters, *J. Geophys. Res.*, 118, 7683–7694, <https://doi.org/10.1002/2013JA019188>, 2013.
- McPherron, R. L., Hsu, T.-S., and Chu, X.: An optimum solar wind coupling function for the *AL* index, *J. Geophys. Res.*, 120, 2494–2515, <https://doi.org/10.1002/2014JA020619>, 2015.
- Murayama, T.: Coupling function between solar wind parameters and geomagnetic indices, *Rev. Geophys. Space Phys.*, 20, 623–629, 1982.
- Nagata, D., Machida, S., Ohtani, S., Saito, Y., and Mukai, T.: Solar wind control of plasma number density in the near-Earth plasma sheet, *J. Geophys. Res.*, 112, A09 204, <https://doi.org/10.1029/2007JA012284>, 2007.
- Nakano, S.: Behavior of the iterative ensemble-based variational method in nonlinear problems, *Nonlin. Processes Geophys.*, 28, 93–109, <https://doi.org/10.5194/npg-28-93-2021>, 2021.
- Nakano, S., Ueno, G., Ohtani, S., and Higuchi, T.: Impact of the solar wind dynamic pressure on the Region 2 field-aligned currents, *J. Geophys. Res.*, 114, A02 221, <https://doi.org/10.1029/2008JA013674>, 2009.
- Newell, P. T. and Gjerloev, J. W.: Evaluation of SuperMAG auroral electrojet indices as indicators of substorms and auroral power, *J. Geophys. Res.*, 116, A12 211, <https://doi.org/10.1029/2011JA016779>, 2011.
- Newell, P. T., Sotirelis, T., Liou, K., Meng, C.-I., and Rich, F. J.: A nearly universal solar wind–magnetosphere coupling function inferred from 10 magnetospheric state variables, *J. Geophys. Res.*, 112, A01 206, <https://doi.org/10.1029/2006JA012015>, 2007.
- Newell, P. T., Sotirelis, T., Liou, K., and Rich, F. J.: Pairs of solar wind–magnetosphere coupling functions: Combining a merging term with a viscous term works best, *J. Geophys. Res.*, 113, A04 218, <https://doi.org/10.1029/2007JA012825>, 2008.
- Pallochia, G., Amata, E., Consolini, G., Marcucci, M. F., and Bertello, I.: AE index forecast at different time scales through an ANN algorithm based on L1 IMF and plasma measurements, *J. Atmos. Sol. Terres. Phys.*, 70, 663–668, 2008.
- Sergeev, V. A., Sormakov, D. A., and Angelopoulos, V.: A missing variable in solar wind–magnetosphere–ionosphere coupling studies, *Geophys. Res. Lett.*, 41, 8215–8220, <https://doi.org/10.1002/2014GL062271>, 2014.
- Sergeev, V. A., Dmitrieva, N. P., Stepanov, N. A., Sormakov, D. A., Angelopoulos, V., and Runov, V.: On the plasma sheet dependence on solar wind and substorms and its role in magnetosphere–ionosphere coupling, *Earth Planets Space*, 67, 133, <https://doi.org/10.1186/s40623-015-0296-x>, 2015.
- Takalo, J. and Timonen, J.: Neural network prediction of AE data, *Geophys. Res. Lett.*, 24, 2403–2406, 1997.
- Terasawa, T., Fujimoto, M., Mukai, T., Shinohara, I., Saito, Y., Yamamoto, T., Machida, S., Kokubun, S., Lazarus, A. J., Steinberg, J. T., and Lepping, R. P.: Solar wind control of density and temperature in the near-Earth plasma sheet: WIND/GEOTAIL collaboration, *Geophys. Res. Lett.*, 24, 935, 1997.
- Tsurutani, B. T., Goldstein, B. E., Smith, E. J., Gonzalez, W. D., Tang, F., Akasofu, S. I., and Anderson, R. R.: The interplanetary and solar causes of geomagnetic activity, *Planet. Space Sci.*, 38, 109–126, 1990.
- Tsurutani, B. T., Gonzalez, W. D., Gonzalez, A. L. C., Tang, F., Arballo, J. K., and Okada, M.: Interplanetary origin of geomagnetic activity in the declining phase of the solar cycle, *J. Geophys. Res.*, 100, 21 717, 1995.
- Wang, H., Lühr, H., Ma, S. Y., Weygand, J., Skoug, R. M., and Yin, F.: Field-aligned currents observed by CHAMP during the intense 2003 geomagnetic storm events, *Ann. Geophys.*, 24, 311, 2006.
- World Data Center for Geomagnetism, Kyoto, Nosé, M., Iyemori, T., Sugiura, M., and Kamei, T.: Geomagnetic *AE* index, Data Analysis Center for Geomagnetism and Space Magnetism, Graduate School of Science, Kyoto University, <https://doi.org/10.17593/15031-54800>, 2015.