



1    **Automatic calculation of the magnetometer zero offset using**  
2    **the interplanetary magnetic field based on the Wang-Pan**  
3    **method**

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12

13    **Abstract**

14        The space-borne fluxgate magnetometer (FGM) needs regular in-flight calibration to  
15        obtain its zero offset. Recently, a new method based on the properties of Alfvén waves  
16        for the zero offset calibration was developed by Wang and Pan (2021). They found that  
17        there exists an optimal offset line (OOL) in the offset cube for a pure Alfvén wave, and  
18        the zero offset can be determined by the intersection of at least two non-parallel OOLs.  
19        Since no pure Alfvén waves exist in the interplanetary magnetic field, the calculation  
20        of the zero offset relies on the selection of the highly Alfvénic fluctuation event. Here,  
21        we propose an automatic procedure to find highly Alfvénic fluctuations in the solar  
22        wind and calculate the zero offset. This procedure includes three parts: (1) selection of  
23        highly Alfvénic fluctuation events, (2) evaluation of the OOL of the selected fluctuation  
24        events, and (3) determination of the zero offset. We test our automatic procedure by  
25        applying it to the magnetic field data measured by the FGM onboard Venus Express.  
26        The tests reveal that our automatic procedure is able to achieve as good results as the  
27        Davis-Smith method. One advantage of our procedure is that the selection criteria and  
28        process for the highly Alfvénic fluctuation event are simpler. Our automatic procedure  
29        might also be applied to find fluctuation events for the Davis-Smith method after proper



30      modification.



## 1. Introduction

There are abundant dynamic processes in the space plasma environment, such as reconnections (Zhang et al., 2012; Lu et al., 2020), instabilities (Hellinger et al., 2017; Duan et al., 2018), turbulences (Huang et al., 2018; Xiao et al., 2020a, 2020b), linear magnetic holes (Ge et al., 2011; Wang et al., 2020, 2021a), and magnetohydrodynamic waves (Keiling, 2008; Wang et al., 2015, 2016, 2017). Some kinetic-scale processes or structures require the accurate measurement of the magnetic field (Burch et al., 2016; Wang et al., 2021b). Therefore, the high-precision magnetic field measurement is crucial to investigate the physical processes in space.

The fluxgate magnetometer (FGM) is one of the most widely used instruments for detecting the magnetic field in space (Acuña, 2002; Balogh, 2010; Burch et al., 2016; Liu et al., 2020). In order to accurately measure the magnetic field, the FGM needs to be calibrated before the launch of the spacecraft (Olsen et al., 2003; Risbo et al., 2003). Nevertheless, regular in-flight calibration is still needed to perform since its instrumental offset, the value measured in a null field environment, varies slowly with time (Balogh, 2010; Olsen et al., 2003). In addition, the slowly changing (or static) magnetic field generated by the spacecraft at the sensor position is generally not negligible, and it is difficult to distinguish the static magnetic field from the instrumental offset (Pope et al., 2011; Pudney et al., 2012). Thus, both the static magnetic field and the instrumental offset are regarded as the zero offset of the spaceborne FGM (Leinweber et al., 2008). Alfvén waves (Davis and Smith, 1968; Belcher, 1973; Hedgecock, 1975) as well as mirror mode structures (Plaschke and Narita, 2016; Plaschke et al., 2017; Plaschke, 2019; Schmid et al., 2020) can be used to calculate the zero offset.

Based on the properties of Alfvén waves, the Davis-Smith method (Davis and Smith, 1968), the Becher method (Belcher, 1973), and the Hedgecock method (Hedgecock, 1975) have been proposed to calculate the zero offset. Both the Becher method and



60 Hedgecock method require a long time interval (a few days or longer) of input data,  
61 which makes these two methods not suitable for the in-flight calibration of the  
62 spacecraft partially orbiting in the solar wind, such as Venus Express (Zhang et al., 2006)  
63 and the Magnetospheric Multiscale (MMS) mission (Russell et al., 2016). Leinweber  
64 et al. (2008) found that the Davis-Smith method is mathematically superior to the other  
65 two methods and needs a much shorter time interval of input data, and the accuracy of  
66 the zero offset calculation depends on the selection of the interplanetary magnetic field  
67 (IMF) fluctuations.

68

69 Recently, a new method has been proposed by Wang and Pan (2021) to calculate the  
70 zero offset of the FGM based on properties of the Alfvén wave. For the convenience of  
71 description, we refer to this new method as the Wang-Pan method. Wang and Pan (2021)  
72 found that the zero offset  $\mathbf{O}$  is on a straight line determined by an Alfvén wave event in  
73 the offset cube, and the authors defined this line as the optimal offset line (OOL). They  
74 also found that the intersection of at least two non-parallel OOLs determined by  
75 different Alfvén waves can be used to determine the zero offset. The Wang-Pan method  
76 can deal with the IMF fluctuation with a duration less than 1 minute, and it calculates  
77 the zero offset more intuitive. However, Wang and Pan (2021) did not provide a method  
78 or criterion to select the IMF fluctuation to perform the Wang-Pan method.

79

80 In this study, we develop an automatic procedure to search out the highly Alfvénic  
81 IMF fluctuation and then calculate the zero offset based on the Wang-Pan method. We  
82 first briefly introduce the Wang-Pan method in section 2. Then, we give the details of  
83 the automatic procedure in section 3. In section 4, we apply this automatic procedure  
84 to perform the in-flight calibration of the FGM onboard the Venus Express spacecraft.  
85 Section 5 presents the summary of our work.

86

## 87 2. Wang-Pan method

88 Alfvén waves do not change the magnetic field strength (Keiling, 2008). Based on



such a property of Alfvén waves, Wang and Pan (2021) found that there exists an OOL with good linearity in the offset cube, and this line passes through the real zero offset. The range of each side of the offset cube can be set according to the possible range of the IMF strength, which is typically less than 20 nT. The intersection of at least two non-parallel OOLs resulting from different Alfvén waves is expected to be the zero offset.

## 2.1 Optimal offset line

Now we introduce the definition of the OOL and how to obtain the OOL of an Alfvén wave in the offset cube (Wang and Pan, 2021). We assume that the sensitivities and non-orthogonality angles of the FGM have been calibrated except for the zero offset  $\mathbf{O}$  ( $= (O_X, O_Y, O_Z)$ ), thereby the magnetic field data  $\mathbf{B}_M$  ( $= (B_{M_X}, B_{M_Y}, B_{M_Z})$ ) is only composed of the natural magnetic field  $\mathbf{B}_A$  ( $= (B_{A_X}, B_{A_Y}, B_{A_Z})$ ) and  $\mathbf{O}$ , or  $\mathbf{B}_M = \mathbf{B}_A + \mathbf{O}$ . Since the typical value of the IMF strength is  $< 20$  nT, the three components of  $\mathbf{O}$  are expected to be in the range of  $(\langle B_{M_X} \rangle - 20, \langle B_{M_X} \rangle + 20)$ ,  $(\langle B_{M_Y} \rangle - 20, \langle B_{M_Y} \rangle + 20)$  and  $(\langle B_{M_Z} \rangle - 20, \langle B_{M_Z} \rangle + 20)$  nT, respectively, where  $\langle B_{M_X} \rangle$ ,  $\langle B_{M_Y} \rangle$  and  $\langle B_{M_Z} \rangle$  are the average values of the three components of  $\mathbf{B}_M$ . Thus, an offset cube in the same coordinate system of  $\mathbf{B}_M$  can be built and the three axes of this offset cube are in the ranges of  $(\langle B_{M_X} \rangle - 20, \langle B_{M_X} \rangle + 20)$ ,  $(\langle B_{M_Y} \rangle - 20, \langle B_{M_Y} \rangle + 20)$  and  $(\langle B_{M_Z} \rangle - 20, \langle B_{M_Z} \rangle + 20)$  nT, respectively. One can find that the zero offset is a certain point in this offset cube.

The magnetic field data are modified to be  $\mathbf{B}'_M = \mathbf{B}_A + \mathbf{O} - \mathbf{O}'$  at the point  $\mathbf{O}'$  in the offset cube. To find out which point in the offset cube is the zero offset, Wang and Pan (2021) tried to find the point which is most likely to be the zero offset in each parallel plane. For a pure Alfvén wave, the standard deviation  $\delta$  of  $\mathbf{B}'_M$  is zero when  $\mathbf{O} = \mathbf{O}'$ , and  $\delta$  is non-zero when  $\mathbf{O} \neq \mathbf{O}'$ . Therefore, Wang and Pan (2021) optimized the point in each parallel plane that is most likely to be the zero offset by minimizing the value of  $\delta$  in the corresponding plane. And they find that these points in the corresponding parallel



118 planes are approximately on a straight line, which is defined as the OOL, because any  
119 point on this line could be the zero offset. Furthermore, the OOL is parallel to the vector  
120  $(\langle B_{A_X} \rangle, \langle B_{A_Y} \rangle, \langle B_{A_Z} \rangle)$ , where  $\langle B_{A_X} \rangle$ ,  $\langle B_{A_Y} \rangle$  and  $\langle B_{A_Z} \rangle$  are the averages of the  
121 three components of  $\mathbf{B}_A$ , respectively.

122

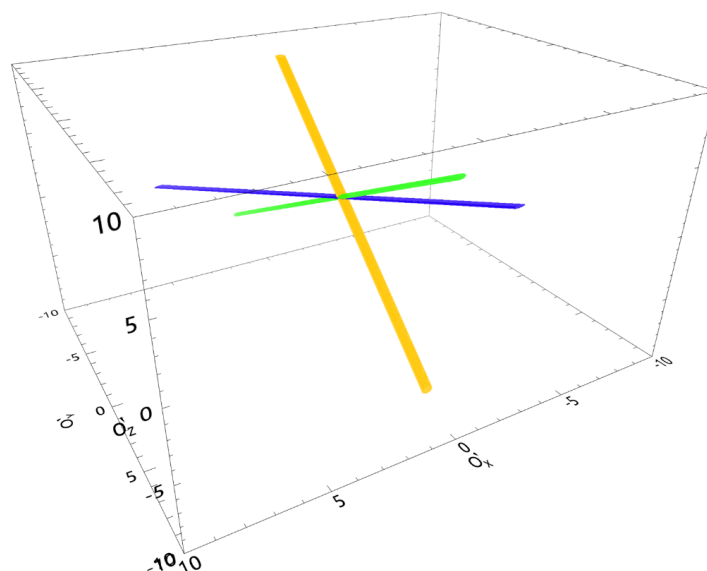
123 The physical meaning of the OOL can be better understood in the mean field-aligned  
124 (MFA) coordinate system. In this coordinate system, the z-axis is parallel to the ambient  
125 magnetic field, and the fluctuation of the Alfvén wave is only in the x-y plane. Thus,  
126 the strength of the magnetic field in the x-y plane  $\sqrt{B_x^2 + B_y^2}$  is a constant (Keiling,  
127 2008; Wang et al., 2015). In the offset cube, the non-constant value of the modified  
128 magnetic field strength in the x-y plane is expected to be caused by the x and y  
129 components of  $\mathbf{O} - \mathbf{O}'$ . Thus, in the offset cube, we can obtain the x and y components  
130 of zero offset in MFA. However, the z component of the zero offset could be any value.  
131 Thus, we cannot determine the zero offset just based on a single Alfvén wave. The most  
132 likely values of the zero offset in MFA form a straight line parallel to the z-axis, and  
133 this line is the so-called OOL.

134

## 135 2.2 Determination of the zero offset

136 To find out the zero offset  $\mathbf{O}$ , at least two non-parallel OOLs are necessary. As shown  
137 in Figure 1, the intersection of the three non-parallel OOLs is the zero offset, since all  
138 the OOLs pass through the point  $\mathbf{O}$  in the offset cube.

139



**Figure 1.** Schematic of the zero offset determined by three non-parallel OOLs in the offset cube.

Due to the influence of the compressional wave and the magnetic field noise, even if the corresponding IMF fluctuation event has a highly Alfvénic nature, the OOL is usually not a straight line. Anyway, the point that minimize  $\delta$  in each plane can be fitted into a straight line, which is called the fitted optimal offset line (FOOL). The FOOL usually does not pass the zero offset point, resulting in no common intersection for the non-parallel FOOLs in the offset cube. Therefore, Wang and Pan (2021) optimized the zero offset so that the sum of the distances from the point in the offset cube to all the FOOLs determined by different IMF fluctuation events is smallest.

### 3. Automatic procedure

For the Wang-Pan method, the process of determining the zero offset can be simplified as finding the point in the offset cube that minimizes the sum of the distances from this point to all the non-parallel FOOLs (Wang and Pan, 2021). It is easy to obtain the zero offset based on the Wang-Pan method when we obtain the IMF fluctuation events with a highly Alfvénic nature. Therefore, finding such IMF fluctuation events



158 automatically is the key to achieve automatic calculation of the zero offset. Here, we  
159 develop an automatic procedure to calculate the zero offset using the IMF fluctuations  
160 based on the Wang-Pan method. This automatic procedure consists of three parts: (1)  
161 selection of the highly Alfvénic fluctuation events, (2) evaluation of the OOL for each  
162 event, and (3) calculation of the zero offset.

163

164 The magnetic field data measured by the FGM onboard the Venus Express (VEX)  
165 spacecraft is used to illustrate the implementation of our automatic procedure. The VEX  
166 spacecraft, launched on 9 November 2005, is a three-axis stabilized spacecraft (Titov  
167 et al., 2006). VEX is the first mission of Europe to Venus, and one of its main scientific  
168 objectives is to study the solar wind interaction with Venus (Zhang et al., 2006). The  
169 VEX FGM measured the magnetic field with a sampling rate up to 128 Hz using two  
170 triaxial fluxgate sensors. The ambient natural magnetic field and the dynamic field  
171 generated by the spacecraft can be separated based on the dual-sensor configuration  
172 (Zhang et al., 2006; Pope et al., 2011). In this study, we use the 1 Hz data of VEX FGM  
173 in the spacecraft coordinate system to calculate the zero offset. Except for the zero offset,  
174 the sensitivities and non-orthogonal angles of the FGM have been calibrated, so the  
175 data we used are called partially calibrated data.

176

### 177 **3.1 Selection of the highly Alfvénic fluctuation event**

178 There are rich of magnetic field fluctuations and structures in the solar wind, such as  
179 Alfvén waves (Li et al., 2016; Wu et al., 2016), mirror mode structures (Volwerk et al.,  
180 2021; Wang et al., 2021a), and discontinuities (Artemyev et al., 2019; Neukirch et al.,  
181 2020). We need to select the magnetic field fluctuation with a highly Alfvénic nature  
182 from the partially calibrated data.

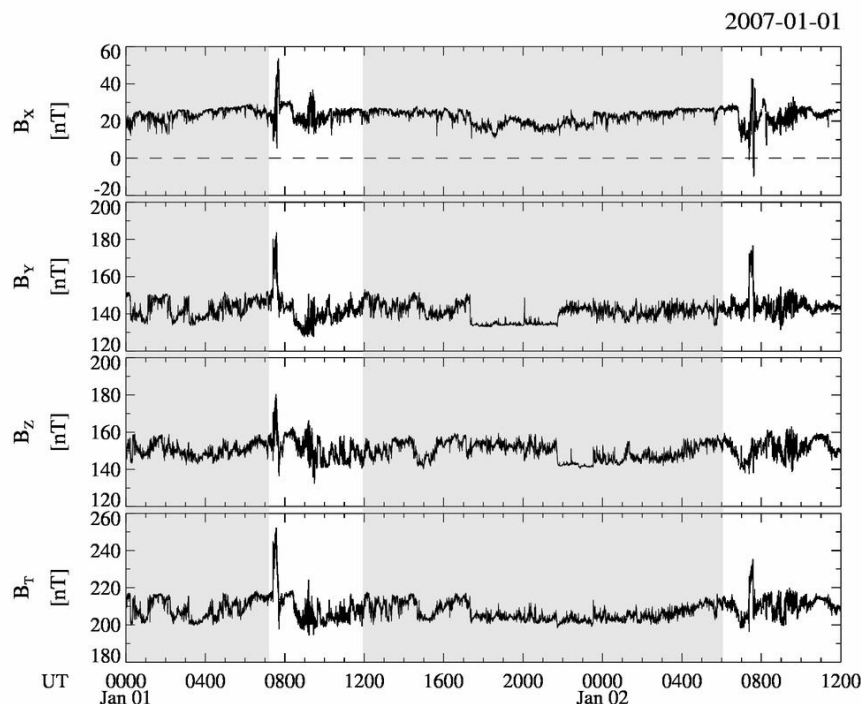
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184 Figure 2 shows the partially calibrated magnetic field data in the spacecraft  
185 coordinate system between 00:00 UT on 1 January and 12:00 UT on 2 January 2007.  
186 Based on the bow shock model (Shan et al., 2015) and the location of the VEX





187 spacecraft, the VEX spacecraft is confirmed to be in the solar wind as shown in the gray  
 188 area of Figure 2. The magnetic field fluctuations have the following characteristics: (1)  
 189 they do not have a fixed period, and the periods of the fluctuations vary from a few  
 190 seconds to several hundred seconds; (2) the amplitude is dominant in different  
 191 components of the magnetic field during different intervals; (3) after removing the zero  
 192 offset, the transverse component of the magnetic field fluctuations dominates in some  
 193 intervals, while the compressional component dominates in other intervals.



194  
 195 **Figure 2.** The partially calibrated magnetic field data of VEX in the spacecraft coordinate system  
 196 and its strength between 00:00 UT on 1 January 2007 and 12:00 UT on 2 January 2007. The gray  
 197 area denotes the VEX spacecraft is in the solar wind.

198  
 199 The selection of the highly Alfvénic fluctuation event can be divided into two steps:  
 200 first, selection of the start and end moments of the event, and second, evaluation of the  
 201 event’s Alfvénic nature. Since the IMF has strong variations with periods typically less  
 202 than 5 minutes as shown in Figure 2, we only select the IMF fluctuation events with



203 periods within 5 minutes. To find the start and end time of a fluctuation event, the  
204 following procedures are executed in parallel on the three components of magnetic field  
205 data:

206 (i). To reduce the effect of the high-frequency noise of the data, the 10 s boxcar filter  
207 is used to smooth the data of each component, and the result is marked as  $B_{i\_sm1}$  (the  
208 index  $i$  represents the component X, Y, or Z of FGM in this procedure). To obtain the  
209 ambient magnetic field, the 200 s boxcar filter is used to smooth the data of each  
210 component, and marked as  $B_{i\_sm2}$ .

211 (ii). We find all the moments when the value of  $B_{i\_sm1} - B_{i\_sm2}$  is 0, and the collection  
212 of these moments is marked as  $T_i$ . The first moment in  $T_i$ , marked as  $T_{i\_0}$ , is regarded  
213 as the start time of the fluctuation event. The end moment  $T_{i\_1}$  of this fluctuation event  
214 is also in the collection of  $T_i$  determined according to the following criteria: a)  $30\text{ s} <$   
215  $T_{i\_1} - T_{i\_0} < 10\text{ min}$ , and b) the number of the elements in  $T_i$  is in the range of 2 – 5.  
216 When the above two criteria are met at the same time, the number of  $T_i$  should be as  
217 large as possible.

218 (iii). Calculate the standard deviation  $\delta_i$  of each magnetic field component in the  
219 period determined by start time  $T_{i\_0}$  and end time  $T_{i\_1}$ .

220 (iv). We can obtain three periods after the above steps. The period corresponding to  
221 the maximum standard deviation  $\delta_i$  is determined as the period of the fluctuation event  
222 eventually.

223 (iv). The end time of this event is selected as the start time of the next event. We  
224 repeat the steps (i) ~ (iv) until we get the start and end time of all fluctuation events in  
225 the solar wind in each VEX orbit.

226

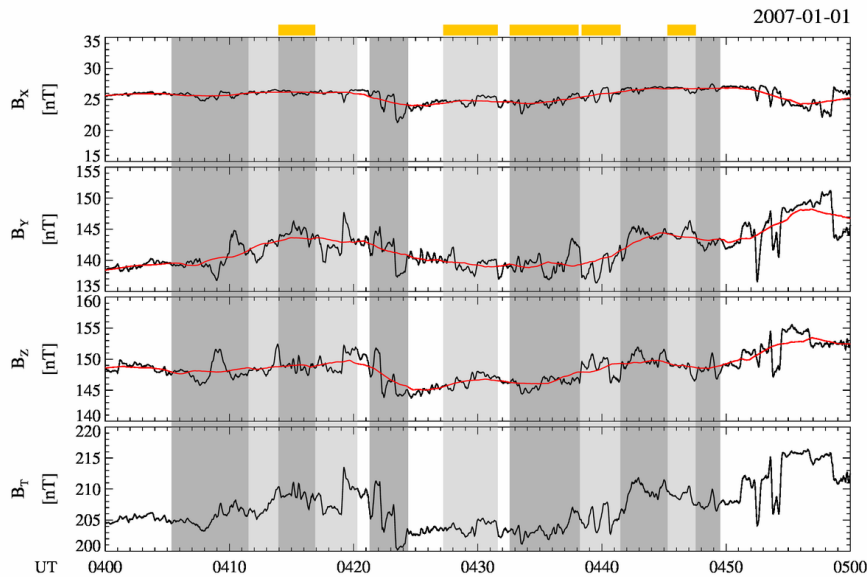
227 According to the Wang-Pan method (Wang et al., 2021) introduced in section 2, we  
228 first build an offset cube in the same coordinate system as  $\mathbf{B}_M$ , and the three axes of the  
229 offset cube are in the range of  $(\langle B_{A\_X} \rangle - 20, \langle B_{A\_X} \rangle + 20)$ ,  $(\langle B_{A\_Y} \rangle - 20, \langle B_{A\_Y} \rangle + 20)$   
230 and  $(\langle B_{A\_Z} \rangle - 20, \langle B_{A\_Z} \rangle + 20)$  nT, respectively. At the point  $\mathbf{O}'$  in the offset cube, the  
231 magnetic field is modified as  $\mathbf{B}'_A = \mathbf{B}_M - \mathbf{O}'$ . For a fluctuation event with a highly



232 Alfvénic nature, the standard deviation of the total field strength is generally very small.  
 233 Thus, the standard deviation  $\delta_{B_T'}$  of  $|\mathbf{B}_A'|$  is expected to be very small at a certain  
 234 point in the offset cube when the real ambient magnetic field  $\mathbf{B}_A$  is a fluctuation event  
 235 with a highly Alfvénic nature. We calculate the values of  $\delta_{B_T'}$  in the offset cube with a  
 236 step length of 0.1 nT along each axis. If the minimum value of  $\delta_{B_T'}$  is  $< \xi_1$  (here,  $\xi_1$  is  
 237 set to be 0.1 nT) in the offset cube, we identify the fluctuation event as a highly Alfvénic  
 238 fluctuation event.

239  
 240 Figure 3 shows an example of selecting the fluctuation event using the partially  
 241 calibrated data of the VEX spacecraft between 04:00 and 05:00 UT on 1 January 2007.  
 242 The red curves indicate the three components of the ambient magnetic field. The gray  
 243 areas in Figure 3 indicate the automatically selected highly Alfvénic fluctuation events  
 244 with different periods. One can find that our above procedures can obtain the interval  
 245 of a fluctuation event with different temporal scales.

246



247  
 248 **Figure 3.** The VEX partially calibrated magnetic field data between 04:00 and 05:00 UT on 1  
 249 January 2007. The red curve denotes the ambient magnetic field  $\mathbf{B}_{A\_sm2}$ . The gray area denotes the



250 interval of the selected fluctuation event, and the yellow tag denotes the interval of the selected  
 251 highly Alfvénic fluctuation event.

252

### 253 3.2 Evaluation of the OOL for each event

254 After obtaining the highly Alfvénic fluctuation events, we then need to determine the  
 255 OOLs of these events. The OOL is expected to be a straight line for a pure Alfvén wave  
 256 (Wang and Pan, 2021). Due to the effect of the compressional fluctuation, the OOL is  
 257 usually not a straight line even for a highly Alfvénic fluctuation event (Wang and Pan,  
 258 2021). Besides, the OOL with a high linearity cannot be obtained if the normal direction  
 259 of the plane is not selected properly for some events. Since we cannot know in advance  
 260 which axis is the best choice to be the normal direction of the reference plane to obtain  
 261 the minimum  $\delta_{B'_T}$ , we use the following steps to obtain the OOL:

262 (i). We find the points of  $P_{OX}$  ( $= [P_{OX\_X}, P_{OX\_Y}, P_{OX\_Z}]$ ) which are the minima of  $\delta_{B'_T}$   
 263 in the planes perpendicular to the  $O'_X$  axis with a step of  $\Delta O'_X = 1$  nT. Note that the  
 264  $P_{OX}$  cannot be located at the boundary of the plane. We require that the number of  $P_{OX}$   
 265 is not less than 10. Then we calculate the correlation coefficients between  $P_{OX\_X}$  and  
 266  $P_{OX\_Y}$ ,  $P_{OX\_X}$  and  $P_{OX\_Z}$ , and  $P_{OX\_Y}$  and  $P_{OX\_Z}$  respectively. The maximum absolute  
 267 value among these coefficients is noted as  $R_{OX}$ . Similarly, we can obtain the sets of  
 268 points  $P_{OY}$  and  $P_{OZ}$ , and their corresponding correlation coefficients  $R_{OY}$  and  $R_{OZ}$ .

269 (ii). If  $R_{OX}$  is larger than  $R_{OY}$  and  $R_{OZ}$ , and  $R_{OX}$  is  $> r$  (here,  $r = 0.9$ ), then  $P_{OX}$  is  
 270 selected to be the OOL. Similarly,  $P_{OY}$  or  $P_{OZ}$  can also be selected as the OOL when the  
 271  $R_{OY}$  or  $R_{OZ}$  is the maximum of the three correlation coefficients and is  $> r$ . If  $R_{OX}$ ,  $R_{OY}$ ,  
 272 and  $R_{OZ}$  are all  $< 0.9$ , the corresponding event will not be selected to calculate the zero  
 273 offset.

274 (iii). We then obtain the FOOL of the OOL determined in step (ii).

275 (iv). Repeat the steps (i) ~ (iv) until we get the FOOLs of all the selected highly  
 276 Alfvénic fluctuation events which meet the requirements in the (i) and (ii) steps.

277

278 Figure 3 displays 8 highly Alfvénic fluctuation events as shown in the gray areas. We



279 use the above procedure to further select the events whose OOLs have good linearity.  
 280 As the yellow tags shown in Figure 3, only 3 out of 8 events meet the above criteria for  
 281 good linearity.

282

### 283 **3.3 Calculation of zero offset**

284 The FOOL is expected to be parallel to the ambient magnetic field and passes through  
 285 the zero offset in the offset cube for a pure Alfvén wave (Wang and Pan, 2021). Due to  
 286 the effect of the compressional fluctuation, the FOOL does not pass through the zero  
 287 offset. Therefore, Wang and Pan (2021) optimize the zero offset so that the sum of the  
 288 distances from the point to all the FOOLs is the smallest. We use the following steps to  
 289 determine the zero offset:

290 (i). In the section 3.2, we obtain the FOOLs in the time period during which the FGM  
 291 needs in-flight calibration. We select N adjacent FOOLs to determine the zero offset.  
 292 Here, the number N is set to be 16. We require that all these FOOLs are within 1 day.

293 (ii). We obtain the distance L from the point O' to the FOOL in the offset cube. In  
 294 order to reduce the influence of a certain FOOL deviating far from the estimated zero  
 295 offset, we convert the distance L to be a probability  $f(L)$ , and  $f(L) = \frac{1}{\sqrt{2\pi}\delta} \exp\left(-\frac{L^2}{2\delta^2}\right)$ .  
 296 Here, we set the standard deviation  $\delta = 3$  nT. We determine the zero offset to be the  
 297 point in the offset cube so that the sum of the values of  $f(L)$  resulting from all the FOOLs  
 298 is the largest. The average time of these FOOLs are considered to be the time of the  
 299 estimated zero offset.

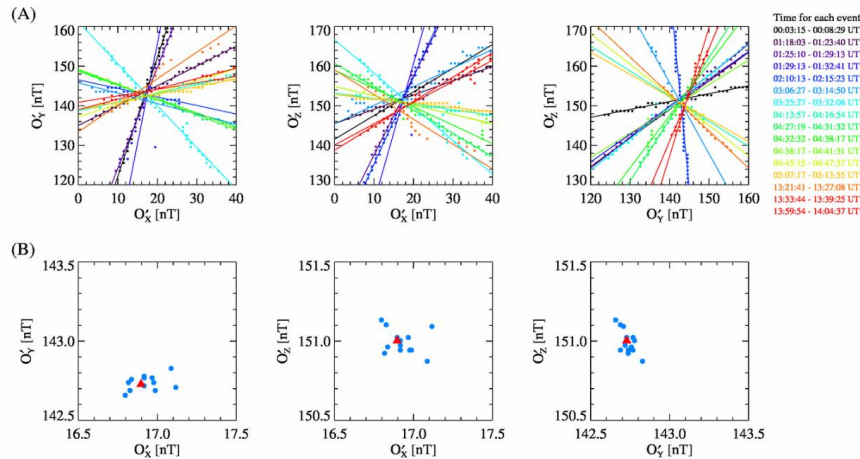
300 (iii). We use any  $N - 1$  out of the N FOOLs to determine the zero offset using the  
 301 method described in the step (ii), then we can obtain N estimated zero offsets. The  
 302 maximum and minimum of these N zero offsets can be used to evaluate the calculation  
 303 error of the zero offset determined by the N FOOLs.

304 (iv). We repeat the steps (i) ~ (iii) to determine the zero offset of the next N FOOLs  
 305 whose sequence number is shifted by M until all the FOOLs have been used to  
 306 determine the zero offset. Here, M is set to be 1.

307



Figure 4 shows an example of the calculation of the zero offset using 16 highly  
 Alfvénic fluctuation events observed by VEX on 1 January 2007. Figure 4A shows the  
 FOOLs of the 16 events as well as their time intervals. As shown by the dots, one can  
 find that the linearity of the OOL is high for each event. The red triangle in Figure 4B  
 denotes the zero offset  $\mathbf{O}_1$  ( $= [16.88, 142.73, 151]$  nT) determined by the automatic  
 procedure introduced in this section, and the blue dot denotes the zero offset  $\mathbf{O}_2$   
 determined by any 15 out of the 16 events. The X, Y, and Z components of  $\mathbf{O}_2$  are in  
 the ranges of  $[16.8, 17.11]$ ,  $[142.66, 142.83]$ , and  $[150.87, 151.13]$  nT, respectively. The  
 minimum and maximum of  $\mathbf{O}_2$  can be used to evaluate the calculation error of  $\mathbf{O}_1$ .



**Figure 4.** (A) The FOOLs (solid lines) for the 16 highly Alfvénic fluctuation events observed by VEX on 1 January 2007. Each dot denotes the position of the minimum  $\delta_{B_T}$  in the corresponding plane for a certain event. The time intervals of the 16 events are also given. (B) The zero offset determined by the FOOLs. The red triangle denotes the zero offset determined by the 16 events. The blue dot denotes the zero offset determined by any 15 out of 16 events.

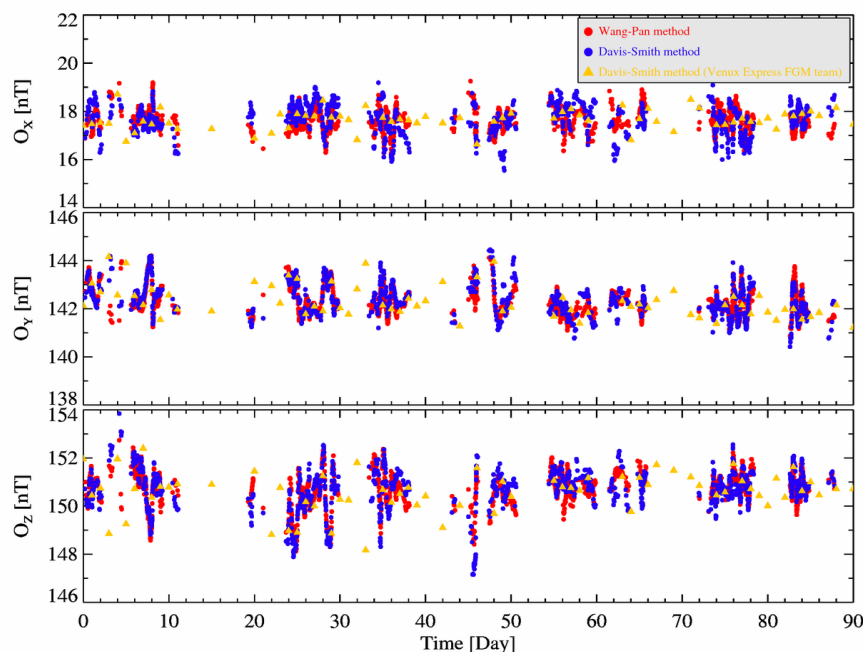
#### 4. Application to VEX

We apply our automatic procedure to the partially calibrated data of VEX from January 1, 2007 to March 31, 2007. Based on the location of the VEX spacecraft and the model of the Venusian bow shock (Shan et al., 2015), we first find the time intervals during which the VEX spacecraft was in the solar wind. Then, the data are used to



330 determine the zero offset based on the automatic procedure described in section 3. The  
 331 zero offsets determined by our procedure are shown by the red dots in Figure 5. We also  
 332 determine the zero offset using the Davis-Smith method with the same fluctuation  
 333 events, and the results are shown by the blue dots in Figure 5. For comparison, Figure  
 334 5 also displays the zero offset provided by the VEX FGM team as shown by the orange  
 335 triangles, and each day has one estimated zero offset. One can find that the profiles of  
 336 the red, blue dots, and orange triangles are very similar, suggesting that our automatic  
 337 procedure is successful to get a reliable results of zero offset.

338



339

340 **Figure 5.** The zero offset for the VEX partially calibrated magnetic field data from 1 January 2007  
 341 to 31 March 2007. The red (blue) dot denotes the zero offset determined by the Wang-Pan (Davis-  
 342 Smith) method. The orange triangle denotes the zero offset provided by the MAG team of the VEX  
 343 spacecraft.

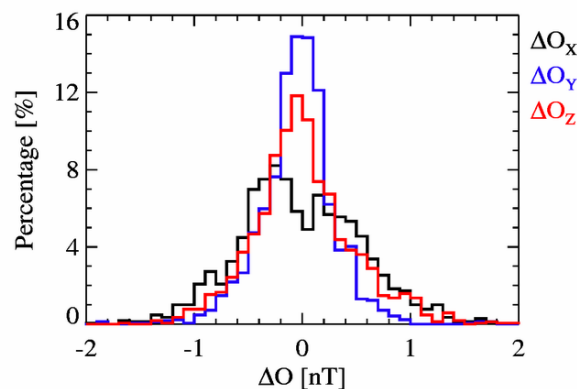
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345 Figure shows the difference between the zero offsets determined by the Wang-Pan  
 346 method and the Davis-Smith method using the highly Alfvénic fluctuation events



347 selected by our automatic procedure.  $\Delta O$  is marked as the difference of the zero offsets  
 348 determined by the two methods. About 64.2% values of  $\Delta O_x$  are within  $[-0.5, 0.5]$  nT,  
 349 and the corresponding probabilities of  $\Delta O_y$  and  $\Delta O_z$  are 87.2% and 73.9%. It suggests  
 350 that the calculation results of the Wang-Pan method are very close to those of the Davis-  
 351 Smith method when using the same fluctuation events selected by our automatic  
 352 procedure.

353



354  
 355 **Figure 6.** The distribution of the difference between the zero offsets determined by the Wang-Pan  
 356 method and the Davis-Smith method.

357

## 358 5. Summary

359 In order to make the application of the Wang-Pan method more convenient, we  
 360 develop an automatic procedure to automatically find the fluctuation events of highly  
 361 Alfvénic nature in the solar wind and determine the zero offset of the FGM. This  
 362 automatic procedure consists of three parts: (1) selection of the highly Alfvénic  
 363 fluctuation event, (2) obtaining the OOL with good linearity for the fluctuation event,  
 364 and (3) determination of the zero offset using at least two non-parallel OOLs. We test  
 365 our automatic procedure by using three months of the partially calibrated data measured  
 366 by VEX FGM, and find that our automatic procedure is successful to achieve as good  
 367 results as the Davis-Smith method.

368





369 Since both the Wang-Pan method and the Davis-Smith method are based on the  
370 properties of Alfvén waves (Davis and Smith, 1968; Wang and Pan, 2021), the selection  
371 of fluctuation events with a highly Alfvénic nature is critical for both methods. Thereby,  
372 Leinweber et al. (2008) provided the following three selection criteria for the  
373 application of the Davis-Smith method: (1) the first criterion is designed to require the  
374 fluctuation in each data window to lie at least within a single plane; (2) the second  
375 criterion requires that the magnetic field has a low level of compression after being  
376 calibrated; (3) the third criterion requires that each magnetic field component has no  
377 strong correlation with the recalculated magnetic field strength. For the Wang-Pan  
378 method, we also need to select the highly Alfvénic fluctuation events, and the criteria  
379 for selecting highly Alfvénic fluctuation events can be summarized into the following  
380 two simple criteria: (1) the minimum of the standard deviations of the modified  
381 magnetic field strength in the offset cube should be small enough; (2) the OOL should  
382 have good linearity. One can find that these two selection criteria are more intuitive.

383

384 Our automatic procedure is developed based on the two criteria of the Wang-Pan  
385 method, and consists of three parts: selection of the potentially high Alfvénic  
386 fluctuation events, evaluation of the OOLs, and determination of the zero offset. The  
387 purpose of the first two parts is to select the highly Alfvénic fluctuation event. After the  
388 highly Alfvénic fluctuation events have been selected, we can choose either the Wang-  
389 Pan method or the Davis-Smith method to calculate the zero offset (Leinweber et al.,  
390 2008; Wang and Pan, 2021). As shown in Figure 5, these two methods can achieve very  
391 similar results. Therefore, our automatic procedure can also be used to automatically  
392 calculate the zero offset based on the Davis-Smith method after a slight modification.



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