

# Terrestrial exospheric dayside H-density profile at 3-15 $R_e$ from UVIS/HDAC and TWINS Lyman- $\alpha$ data combined

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## 1 Abstract.

2 Terrestrial ecliptic dayside observations of the exospheric Lyman- $\alpha$  column intensity between 3-  
3 15 Earth radii ( $R_e$ ) by UVIS/HDAC at CASSINI have been analysed to derive the neutral exospheric  
4 H-density profile at the Earth's ecliptic dayside in this radial range. The data were measured during  
5 CASSINIS's swing by manoeuvre at the Earth on 18 August 1999 and are published by (Werner  
6 et al., 2004). In this study the dayside HDAC Lyman- $\alpha$  observations published by (Werner et al.,  
7 2004) are compared to calculated Lyman- $\alpha$  intensities based on the 3D H-density model derived  
8 from TWINS Lyman- $\alpha$  observations between 2008-2010 (Zoennchen et al., 2015). It was found, that  
9 both Lyman- $\alpha$  profiles show a very similar radial dependence in particular between 3-8  $R_e$ . Between  
10 3.0-5.5  $R_e$  impact distance Lyman- $\alpha$  observations of both TWINS and UVIS/HDAC are existing at  
11 the ecliptic dayside. In this overlapping region the cross-calibration of the HDAC profile against  
12 the calculated TWINS profile was done, assuming, that the exosphere there was similar for both  
13 due to comparable space weather conditions. As result of the cross-calibration the conversion factor  
14 between counts/s and Rayleigh  $f_c=3.285$  [counts/s/R] is determined for these HDAC observations.  
15 Using this factor the radial H-density profile for the Earths ecliptic dayside was derived from the  
16 UVIS/HDAC observations, which constrained the neutral H-density there at 10  $R_e$  to a value of 35  
17  $cm^{-3}$ . Furthermore, a faster radial H-density decrease was found at distances above 8  $R_e$  ( $\approx r^{-3}$ )  
18 compared to the lower distances 3-7  $R_e$  ( $\approx r^{-2.37}$ ). This increased loss of neutral H above 8  $R_e$   
19 might indicate a higher rate of H ionization in the vicinity of the magnetopause at 9-11  $R_e$  (near sub  
20 solar point) and beyond, because of increasing charge exchange interactions of exospheric H atoms  
21 with solar wind ions outside the magnetosphere.

22 **Keywords.** Atmospheric composition and structure (airglow and aurora; pressure, density, and tem-  
23 perature) – meteorology and atmospheric dynamics (thermospheric dynamics)

24 **1 Introduction**

25 The Earth's exosphere is the outermost layer of our atmosphere that ranges from  $\approx$ 500km altitude  
26 to beyond the Moons orbit (Baliukin et al. 2019). Atomic hydrogen atom (H) becomes a dominant  
27 species above an altitude of  $\approx$ 1500km. The exosphere gains and loses hydrogen atoms as a result of  
28 the Sun - solar wind - magnetosphere - upper atmosphere interaction. Study of the exospheric density  
29 distribution and its response to dynamic space environments is key to understand the past, present,  
30 and future of the Earths atmosphere and to infer the evolution of other planetary atmospheres.

31 The typical geocorona emission, i.e., solar Lyman- $\alpha$  photons resonantly scattered by hydrogen  
32 atoms, has been a widely used dataset to derive a terrestrial exospheric neutral H-density. Sev-  
33 eral spacecraft missions like Thermosphere - Ionosphere - Mesosphere Energetics and Dynamics  
34 (TIMED; Kusnierzewicz, 1997), Two Wide-Angle Imaging Neutral- Atom Spectrometer (TWINS;  
35 Goldstein & McComas, 2018), and Solar and Heliospheric Observatory (SOHO; Domingo et al.,  
36 1995) have observed the geocorona from various vantage points, covering an optically thick, near-  
37 Earth exosphere below  $\approx$ 3  $R_e$  geocentric distance (e.g., Qin & Waldrop, 2016; Qin et al., 2017; Wal-  
38 drop et al., 2013) to an optically thin, far distant exosphere on top (e.g., Bailey & Gruntman, 2011;  
39 Cucho-Padin & Waldrop, 2019; Zoenchen et al., 2011, 2013). The exospheric density changes over  
40 various time scales such as solar cycle (Waldrop & Paxton, 2013; Zoenchen et al., 2015; Baliukin  
41 et al., 2019), solar rotation (Zoenchen et al., 2015), and geomagnetic storms (Bailey & Gruntmann,  
42 2013; Cucho-Padin & Waldrop, 2019; Qin et al., 2017; Zoenchen et al., 2017). This implies active  
43 response of our exosphere to a dynamic space environment through physical processes like thermal  
44 expansion, photoionization, and neutral charge exchanges as suggested in the previous theoretical  
45 studies (Chamberlain, 1963; Bishop, 1985; Hodges, 1994; and references therein). Also the possible  
46 contribution of non-thermal hydrogen to the exosphere is discussed (e.g., Qin & Waldrop, 2016;  
47 Fahr et al., 2018).

48 Recently, exospheric neutral H-density at 10  $R_e$  subsolar location becomes a particular interest  
49 due to two upcoming missions, the NASA Lunar Environment heliospheric X-ray Imager (LEXI;  
50 <http://sites.bu.edu/lexi>) and the joint ESA-China mission, Solar wind - Magnetosphere - Ionosphere  
51 Link Explorer (SMILE; Branduardi-Raymont et al., 2018) with expected launches in 2023 and 2024,  
52 respectively. Soft X-ray imagers on these spacecrafts will observe motion of the Earths magne-  
53 tosheath and cusps in soft X-ray with a primary goal of understanding the magnetopause reconne-  
54 cation modes under various solar wind conditions. Soft X-ray is emitted due to interaction between the  
55 exospheric neutrals and the highly charged solar wind ions like  $O^{7+}$  and  $O^{8+}$  (Sibeck et al., 2018;  
56 Connor et al., 2021). Neutral density is a key parameter that controls the strength of soft X-ray sig-

57 nals. Denser hydrogen increases their interaction probability with solar wind ions and thus enhance  
58 soft X-ray signals, which is preferable for the LEXI and SMILE missions.

59 The dayside geocoronal observations above  $8 R_e$  radial distance are very rare. For estimating an  
60 exospheric density at  $10 R_e$  subsolar location, Connor & Carter (2019) and Fuselier et al. (2010;  
61 2020) used alternative datasets: the soft X-ray observations from the X-ray Multi-Mirror Mission-  
62 Newton astrophysics mission (XMM; Jansen et al., 2001) and the Energetic Neutral Atom (ENA)  
63 observations from the Interstellar Boundary Explorer (IBEX; McComas et al., 2009), respectively.  
64 Their density estimates at  $10 R_e$  show a large discrepancy, ranging from  $4 \text{ cm}^{-3}$  to  $59 \text{ cm}^{-3}$  with a  
65 lower limit from the IBEX observations and an upper limit from the XMM observations. However,  
66 these studies analyzed only a handful of events. Additionally, inherent difference of the soft X-ray  
67 and ENA datasets leads to different density extraction techniques, possibly contributing to the neu-  
68 tral density discrepancy. To understand a true nature of this outer dayside exosphere, more statistical  
69 and cumulative approaches with various datasets are needed.

70 We estimate a dayside exospheric density in a radial distance of 3-15  $R_e$  using rare dayside geo-  
71 corona observations obtained from the CASSINI UVIS/HDAC Lyman- $\alpha$  instrument on 18 August  
72 1999. This paper is structured as follows. Section 2 introduces the CASSINI Lyman- $\alpha$  observations  
73 on 18 August 1999. Section 3 discusses the solar condition and interplanetary Lyman- $\alpha$  background  
74 during the observation period. Section 4 explains our density extraction approach. Section 5 esti-  
75 mates the conversion factor of the CASSINI UVIS/HDAC geocorona count rates to Rayleigh, and  
76 Section 6 derives the dayside exospheric density profiles from the converted geocoronal emission in  
77 Rayleigh. Finally, Section 7 discusses and concludes our results.

78

## 79 2 The UVIS/HDAC Lyman- $\alpha$ observations during CASSINI's swing by at the Earth

80 On its way to Saturn the CASSINI spacecraft performed a swing by manoeuvre at the Earth on 18  
81 August 1999. The UVIS/HDAC Lyman- $\alpha$  instrument ( $\text{FOV} \approx 3^\circ$ ) was switched on before and mea-  
82 sured then continuously Lyman- $\alpha$  intensities during the manoeuvre. When approaching the Earth the  
83 measured Lyman- $\alpha$  intensities were increasingly dominated by scattered Lyman- $\alpha$  emission from  
84 neutral H-atoms of the terrestrial exosphere. The intensity profile in [counts/s] (averaged over a  
85 1 min interval) from UVIS/HDAC is a rare observation of the exospheric dayside Lyman- $\alpha$  emis-  
86 sion near the Earth-Sun line up to  $15 R_e$  geocentric distance. It is a nearly perfect scan within the  
87 ecliptic plane during  $\approx 1.5$  hours and therefore nearly free from latitudinal and temporal variations.  
88 The profile was published by (Werner et al., 2004) and is shown in Figure 2 of their paper. From  
89 each measurement they had subtracted 4500 [counts/s] as correction for their estimate of the inter-  
90 planetary background intensity. For the geocentric distances 3-15  $R_e$  this corrected profile can be

91 numerically approximated by the following fit function:

92  $I_{corr}(r) = 282920.2 * (r + 2.0)^{-2.2}$  [counts/s] (1)

93 with the geocentric distance  $r$  in  $R_e$ . In Figure 1 is shown, that the fitted radial intensity function  
94 from Equation (1) (red line) approximates the profile from (Werner et al., 2004) (black line) very  
95 well. Values from Equation (1) need to be re-added with 4500 [counts/s] in order to retrieve the  
96 uncorrected intensities originally measured by UVIS/HDAC:

97  $I(r) = I_{corr}(r) + 4500$  [counts/s] (2)

98 The observational geometry (spacecraft position and viewing direction of UVIS/HDAC) during the  
99 swing by was also adopted from (Werner et al., 2004): On the Earth dayside CASSINI moved within  
100 the ecliptic plane towards Earth. CASSINI's dayside trajectory as shown in (Werner et al., 2004 -  
101 see Figure 1 there) is nearly linear within 3-15  $R_e$ . It can be numerically approximated as radial  
102 function of the GSE longitude:

103  $\phi_{GSE}(r) = 6.7 + 80.14/r$  [°] (3)

104 with the geocentric distance  $r$  in  $R_e$ . Following (Werner et al., 2004) in this trajectory segment the  
105 line of sight (LOS) of UVIS/HDAC pointed towards the positive GSE Y-axis away from Earth. **More**  
106 **UVIS/HDAC instrumental facts can be found in the "UVIS User's Guide" provided by NASA PDS-**  
107 **Website (see: [https://pds-atmospheres.nmsu.edu/data\\_and\\_services/atmospheres\\_data/Cassini/inst-uvvis.html](https://pds-atmospheres.nmsu.edu/data_and_services/atmospheres_data/Cassini/inst-uvvis.html))**

### 108 3 Solar conditions and the interplanetary Lyman- $\alpha$ background

109 The total solar Lyman- $\alpha$  flux and the solar  $F_{10,7cm}$ -radio flux are important indicators of the so-  
110 lar activity. The solar Lyman- $\alpha$  flux can vary from 3.5 (solar minimum) to 6.5 (solar maximum)  
111  $\cdot 10^{11}$  [photons/cm $^2$ /s]. The solar  $F_{10,7cm}$ -radio flux can vary from below 50 (solar minimum) to  
112 above 300 (solar maximum). On the swing by date 18 August 1999 the value of the total solar  
113 Lyman- $\alpha$  flux was 4.52 - a bit higher than the value of  $\approx 3.5$  during the TWINS LAD-observations  
114 in 2008 and 2010. It has been measured by TIMED SEE and SORCE SOLSTICE calibrated to UARS  
115 SOLSTICE level [Woods et al., 2000] (provided by LASP, Laboratory For Atmospheric And Space  
116 Physics, University of Boulder, Colorado). With the function given by (Emerich et. al., 2005), the  
117 line-center solar Lyman- $\alpha$  flux was calculated from this total solar Lyman- $\alpha$  flux for the derivation  
118 of the g-factor as used in Equation (4).

119 The solar activity level as indicated by the solar  $F_{10,7cm}$ -radio flux starts to increase in summer  
120 1999 from the low values of the solar minimum until 1998. **With 130 the  $F_{10,7cm}$ -value during**  
121 **the UVIS/HDAC observations is also a bit higher compared to  $\approx 80$  during the TWINS LAD-**  
122 **observation in 2008 and 2010.**

123 When flying at the Earth dayside between 3-15  $R_e$ , the UVIS/HDAC LOS pointed to a region with

124 interplanetary Lyman- $\alpha$  background of about 1400  $R$ . This value was taken from the SOHO-SWAN  
125 all sky map of the Lyman- $\alpha$  background of 17 August 1999 (SOHO-SWAN images provided via Web  
126 by LATMOS-IPSL, Universit Versailles St-Quentin, CNRS, France: <http://swan.projet.latmos.ipsl.fr/images/>).

127 **4 Approach**

128 During the swing by at the Earth, the UVIS/HDAC instrument measured Lyman- $\alpha$  radiation reso-  
129 nantly backscattered from neutral hydrogen of the terrestrial exosphere and also from the interplan-  
130 etary medium. Due to their low velocities the contributing H-atoms can be considered as "cold".  
131 Therefore, this backscattered radiation contains wavelengths with a relatively narrow bandwidth  
132 around the Lyman- $\alpha$  line center. The sole contribution of the interplanetary hydrogen was quantified  
133 by the value taken from SOHO-SWAN as described in the previous section.

134 Within the exosphere the optical depth turns to be lower than 1 at geocentric distances  $> 3 R_e$ ,  
135 which allows for the assumption of single scattering. Under this assumption for a particular solar  
136 Lyman- $\alpha$  radiation (manifested in the g-factor) the exospheric H-density  $N(S)$  along a line of sight  
137  $S$  produces a Lyman- $\alpha$  scatter intensity  $I$  in [R]:

$$138 \quad I = \frac{g}{10^6} \int_0^{S_{max}} n(S) \epsilon(S) I_p(\alpha(S)) dS \quad (4)$$

139 with  $n(S)$  is the local H-density,  $\epsilon(S)$  the local correction term for geocoronal selfabsorption/re-  
140 emission and  $I_p(\alpha(S))$  the local intensity correction for the angular dependence of the scattering.

141 Additionally to the solar radiation the dayside Lyman- $\alpha$  observations above  $3R_e$  analysed in this  
142 study are illuminated by a secondary Lyman- $\alpha$  radiation from lower atmospheric shells of the Earth:  
143 At the dayside lower, optically thick exospheric shells are face-on illuminated by the Sun. The re-  
144 emission created there acts as a secondary source of Lyman- $\alpha$  besides the Sun. The relative effect  
145 increases with decreasing geocentric distance. With the  $\epsilon(S)$ -term in Equation (4) the Lyman- $\alpha$  in-  
146 tensity profile can be corrected from re-emission of solar Lyman- $\alpha$  from lower atmospheric shells of  
147 the Earth. The applied method in this study, all considered correction terms and the used  $\epsilon(r, \theta, \phi)$   
148 map (shown in Figure 2) are in detail described in (Zoennchen et al., 2015).

149 With usage of a given H-density distribution the Lyman- $\alpha$  column brightness can be calculated for  
150 any LOS and observing position within the optically thin regime based on the integral in Equation  
151 (4). The calculated values ([R]) can be converted into their observable intensities ([counts/s]) using  
152 a single instrumental factor ([counts/s/R]) - further referred as conversion factor  $f_c$ .

153 In this study two H-density models are used for comparison with UVIS/HDAC: the exospheric  
154  $H(r, \theta, \phi)$ -density model derived from TWINS Lyman- $\alpha$  observations from 2008 and 2010 (Zoen-  
155 nchen et al., 2015 - with parameters from Table 1 there) and a radial symmetric model as introduced  
156 by (Chamberlain, 1963) and frequently used for example by (Raideren et al., 1986), (Fuselier et al.,

157 2010, 2020) or (Connor & Carter, 2019):

$$158 n_H(r) = n_0 \cdot \left( \frac{10 R_e}{r} \right)^3 \quad (5)$$

159 with the geocentric distance  $r$  in  $R_e$ . The H-density at  $10 R_e$  subsolar point ( $n_0$ ) is set at  $40 \text{ cm}^{-3}$ ,  
160 which is within the reported range of Connor & Carter (2019) that derived  $n_0$  from the XMM soft  
161 X-ray emission.

162 The used TWINS model is an empirical 3D model of the neutral exospheric H-density with validity  
163 range 3-8  $R_e$ . It based on the inversion of Lyman- $\alpha$  LOS-observations of the TWINS satellites from  
164 the solar minimum in 2008 and 2010.

165 The other density model was introduced by [Chamberlain, 1963] as analytical approach, that based  
166 on 3 different H-atom populations in the exosphere (ballistic, satellite and escaping) with an initial  
167 Maxwellian distribution function at the exobase and the assumption of constant distribution func-  
168 tions on H-atoms trajectories (Liouville's theorem). The theoretical fundamentals are very good  
169 summarized in [Beth et al., 2016].

170 The comparison of the calculated profiles with the UVIS/HDAC profile was made for two reasons:  
171 First, to compare their radial dependency and second, to derive the conversion factor  $f_c$  of UVIS/HDAC  
172 by cross-calibrating it against the calculated profile from the TWINS H-density model in the radial  
173 range 3.0-5.5  $R_e$  (overlapping range). Dayside Lyman- $\alpha$  observations with impact distances inside  
174 this overlapping range are available by both - UVIS/HDAC and TWINS. This method for evalua-  
175 tion of  $f_c$  assumes, that the TWINS H-density model from 2008, 2010 also matches the exospheric  
176 H-density distribution on 18 August 1999 due to comparable space weather conditions. Both, the  
177 used TWINS and UVIS/HDAC observations were measured during quiet geomagnetic conditions  
178 (minimum Dst index  $\approx -30 \text{ nT}$ ; provided by the website of the WDC for Geomagnetism, Kyoto) and  
179 low solar activity (Solar 10,7 cm  $\leq 130$ ).  
180 Nevertheless, it is known from other studies, that the terrestrial exosphere show H-density variations  
181 of about 10-20% caused by geomagnetic storms (i.e. Bailey & Gruntman, 2013; Zoenenchen et al.,  
182 2017; Cucho-Padin & Waldrop, 2018). Therefore we expect an error of the conversion factor by this  
183 variations up to 20%.

## 184 5 Comparison of the observed UVIS/HDAC profile with calculated profiles

185 The observed dayside Lyman- $\alpha$  profile (column intensity) by UVIS/HDAC (approximated in Equa-  
186 tion (2)) was compared to the calculated Lyman- $\alpha$  profiles (column brightness) from two exospheric  
187 H-density models described in the previous section. CASSINI's trajectory at the dayside between  
188 3-15  $R_e$ , the LOS of HDAC, the interplanetary background and the solar conditions of the swing by  
189 day 18 August 1999 were considered by the calculation.

190 Figure (3A) shows the uncorrected observed Lyman- $\alpha$  profile by UVIS/HDAC from Equation (2)  
191 in [counts/s] (black line) together with the calculated column brightness profiles in [R] based on the

192 TWINS 3D H-density model (inside its validity range 3-8  $R_e$  = red line) and the  $1/R^3$  model (blue  
193 line) - all including interplanetary Lyman- $\alpha$  background. It is obvious from that figure, that between  
194 3-8  $R_e$  the radial dependence of the calculated profile using the TWINS 3D H-density model corre-  
195 sponds well to the UVIS/HDAC observed profile. The radial dependency of the  $1/R^3$ -profile (blue  
196 line) deviates from the HDAC profile in this particular range.

197 Figure (3B) shows the ratios of the observed and the calculated profiles: In the overlapping range  
198 (3.0-5.5  $R_e$ ) the averaged ratio between the UVIS/HDAC observations and the TWINS 3D H-density  
199 model (red line) is nearly constant with only slight variations between -2.1% and +1.2%. It is equiv-  
200 alent to the averaged conversion factor and was found to be  $f_c=3.285$  [counts/s/R].

201 For the  $1/R^3$  model (blue line) the ratio shows significant deviations from a constant value for lower  
202 radial distances  $<8R_e$ . But for distances above 9  $R_e$  the profile of this model turned also into a  
203 nearly constant ratio to the UVIS/HDAC data (average = 3.145 [counts/s/R]).

204

205 Besides the cross-calibration method there is another independent way to approximate  $f_c$ : (Werner  
206 et al, 2004) estimated the interplanetary Lyman- $\alpha$  background in the UVIS/HDAC observations with  
207 4500 [counts/s]. To be not contaminated with exospheric emission, this value had to be measured  
208 far enough outside the exosphere. The interplanetary Lyman- $\alpha$  radiation is also created by resonant  
209 backscattering and is therefore comparable in its physical properties to exospheric emission. Using  
210 the Lyman- $\alpha$  background emission value from SOHO-SWAN in [R] for the UVIS/HDAC LOS, the  
211 conversion factor  $f_c$  can be approximated on this separate way to:

$$212 f_c = \frac{4500 \text{ counts/s}}{1400 \text{ R}} = 3.215 \text{ [counts/s/R]} \quad (6)$$

213 The two results for  $f_c$  with  $f_c=3.285$  from the profile comparison using the TWINS H-density model  
214 and  $f_c=3.215$  from the background estimation by (Werner et al., 2004) are relatively close together.

## 215 **6 H-density profile derived from the UVIS/HDAC observations**

216 We applied the determined conversion factor  $f_c=3.285$  [counts/s/R] to convert the observed dayside  
217 Lyman- $\alpha$  profile by UVIS/HDAC from intensities [counts/s] into column brightness [R] between  
218 3-15  $R_e$ . Inverse usage of Equation (4) with known column brightnesses I(S) allows to fit the H-  
219 density profile. The H-density profile inverted from the UVIS/HDAC observations was fitted into  
220 the radial symmetric function:

$$221 n_H(r) = 370520 * (r + 2.47)^{-3.67} \text{ [cm}^{-3}] \quad (7)$$

222 with geocentric distance  $r$  in  $R_e$ . Figure (4) shows the fitted H-density profile (black squares). From  
223 the  $n_H(r)$ -profile the UVIS/HDAC observations can be calculated very precisely over the entire  
224 radial range 3-15  $R_e$  within  $\pm 2\%$  error.

225 Obvious in Figure (4) is a change in the radial dependency of the profile in the radial region above

226  $8 R_e$ . At distances lower  $8 R_e$  the H-density profile seems to fall with distance with a power law  $\approx$   
227  $r^{-2.37}$  (red line in Figure (4)). It was fitted in the distance range  $3-7 R_e$  to:

228  $n_H(r) = 10198 * r^{-2.375} [cm^{-3}]$  (8)

229 where the geocentric distance  $r$  is in  $R_e$ . The black and red lines are in very good agreement at  
230  $3-7 R_e$ . Above  $>8 R_e$  the situation has changed and the H-density falls with about  $\approx r^{-3}$ , what  
231 is indicated by the very good agreement of the cyan with the **black squares** there. The fit of the  
232 H-density profile between  $9-15 R_e$  delivers a  $r^{-3}$  fall:

233  $n_H(r) = 35.17 * \left(\frac{10 R_e}{r}\right)^{3.02} [cm^{-3}]$  (9)

234 From theory an enhanced loss of neutral H atoms near the magnetopause and outside the magne-  
235 tosphere can be expected due to sharply increased interactions with solar wind ions in this region  
236 that produces soft X-ray photons and ENAs. The faster decrease with  $r^{-3}$  in the H-density profile  
237 above  $8 R_e$  might indicate the higher ionization of cold exospheric neutrals near the magnetopause  
238 (located at  $9-11 R_e$  in the vicinity of the sub solar point) and beyond.

239 From the fitted H-density profile of Equation (7) the exospheric H-density at  $10 R_e$  was found to be  
240  $35 cm^{-3}$  at the ecliptic dayside. From known variations of the neutral exosphere due to geomagnetic  
241 storms up to 20 % [Zoennchen et al., 2017] and with the summarized error from other contributions  
242 (i.e. from background, solar Lyman- $\alpha$  flux and so on) there is a total error in the H-density of about  
243 25 % expectable. Nevertheless, from several facts we assume, that the found value of  $35 cm^{-3}$  at  
244  $10 R_e$  is more likely to be a lower limit: First, between  $3-10 R_e$  the neutral exospheric response to  
245 geomagnetic storms is so far known as an increase and not as a decrease of neutral density (Bailey &  
246 Gruntman 2013, Zoennchen et al., 2017, Cucho-Padin & Waldrop 2018). Second, there are indica-  
247 tions, that an increasing solar activity also corresponds to an increase of neutral density in this radial  
248 range, either weak (Fuselier et al., 2020) or somewhat stronger (Zoennchen et al., 2015). The H-  
249 density model from TWINS used here based on observations in 2008 and 2010 near solar minimum  
250 during quiet days without storms. Therefore it represents likely an exosphere with neutral densities  
251 close to their lowest values.

252 **7 Discussion**

253 Ecliptic dayside Lyman- $\alpha$  observations of the terrestrial H-exosphere between  $3-15 R_e$  by UVIS/HDAC  
254 onboard CASSINI were compared to calculated Lyman- $\alpha$  brightnesses using two different H-density  
255 models: First, the H-density model based on TWINS Lyman- $\alpha$  observations from 2008, 2010 and  
256 second, the  $1/R^3$ -model introduced by (Chamberlain et al., 1963). The calculations considered the  
257 HDAC Lyman- $\alpha$  observations, CASSINI's trajectory and the HDAC LOS published by (Werner et  
258 al., 2004).

259 As first result it was found, that the radial dependence of the HDAC observations and the calculated

260 profile from the TWINS model are very similar in the radial range 3-8  $R_e$ . The  $1/R^3$ -model shows  
261 significant deviations from the observed profile in this lower range.

262 To be able to convert the HDAC observations from [counts/s] into physical units [R] the averaged  
263 conversion factor  $f_c=3.285$  [counts/s/R] was derived in the radial range 3.0-5.5  $R_e$  (overlapping re-  
264 gion) from the ratio between the HDAC observations and the calculated Lyman- $\alpha$  brightnesses from  
265 the TWINS model. Dayside LOSs with impact distances in the overlapping region are available  
266 from both instruments - HDAC and TWINS LAD. Additionally a second independent way was used  
267 to quantify the conversion factor  $f_c=3.215$  [counts/s/R] by calculating the ratio between the esti-  
268 mated background value given by (Werner et al., 2004) and the corresponding value taken from the  
269 SOHO/SWAN map. Both values found for  $f_c$  are very close together.

270 With usage of  $f_c=3.285$  the HDAC observations are inverted into a radial symmetric H-density pro-  
271 file of the ecliptic dayside between 3-15  $R_e$ . The derived density profile determined a H-density  
272 value of  $35 \text{ cm}^{-3}$  at  $10 R_e$  in the vicinity of the sub-solar point. The error is expected with 25 %.  
273 Nevertheless, from different mentioned reasons it is more likely, that this value is closer to the lower  
274 limit.

275 Also found was a faster decrease of the H-density for distances above  $8 R_e$  ( $r^{-3}$ ) compared to the  
276 lower region  $3-7 R_e$  ( $r^{-2.37}$ ). This is consistent with an enhanced depletion of neutral H in the far-  
277 upsun direction beyond  $8 R_e$  reported by (Carruthers et al, 1976) based on Lyman- $\alpha$  images from  
278 the Moon by Apollo 16 and also with observations of Mariner 5 (Wallace et al., 1970).

279 The faster H-density decrease above  $8 R_e$  in the up-sun direction as quantified in this study may  
280 indicate an enhanced ionization rate near the magnetopause and beyond, respectively, due to sharply  
281 increased interactions there of neutral H atoms with solar wind ions.

282 The regions near the sub solar point (close to the magnetopause) and the connected magnetosheath  
283 are identified as sources of observable strong enhanced ENA production (see e.g. Fuselier et al.,  
284 2010, 2020) and of Soft X-ray radiation (see Connor & Carter, 2019).

285 The ENA's are produced by charge exchange between energized solar wind  $H^+$ -ions and cold geo-  
286 coronal neutral H. The result is a slow  $H^+$ -ion (bound to the terrestrial magnetic field) and a fast  
287 neutral H-atom (ENA), which mainly escapes from this region into space.

288 The Soft X-ray radiation is (also) produced by charge exchange - between highly charged solar wind  
289 oxygen ions ( $O^{7+}$  or  $O^{8+}$ ) and geocoronal neutral H, which donates an electron to the ions (referred  
290 as solar wind charge process SWCX).

291 Inside the magnetopause there is a protection against the solar wind ions due to the terrestrial mag-  
292 netic field. This situation changes from the magnetopause towards the connected magnetosheats:  
293 There, the named ENA- and Soft X-ray production sharply increase, since the solar wind ions can  
294 penetrate this regions.

295 In both processes cold neutral H-atoms are lost by conversion into ions. This might be a possible  
296 reason for a faster decrease of the neutral geocoronal H-density in the named regions of ENA / Soft

297 **X-ray production.**

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## Figure Captions

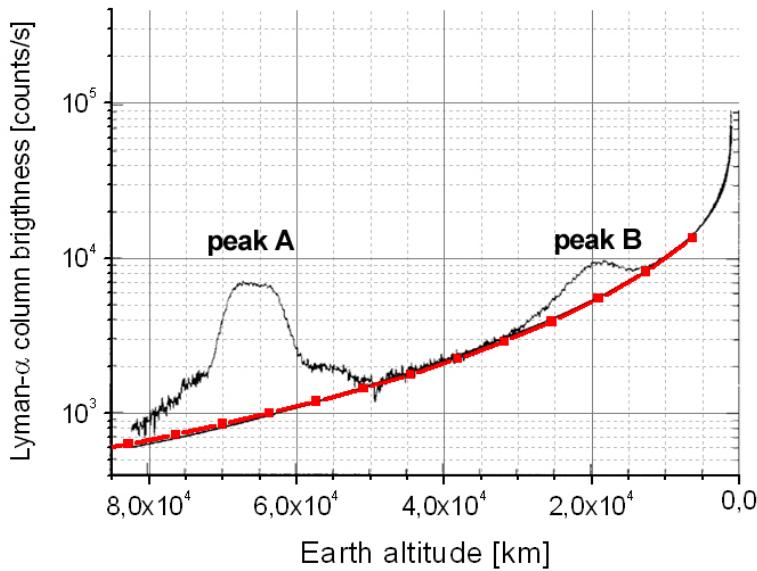
**Fig. 1.** Black: UVIS/HDAC Lyman- $\alpha$  intensity profile [counts/s] (black line) from (Werner et al., 2004); the origin of the two peaks were identified by (Werner et al., 2004) as (A) the Earthmoon and (B) distortion by the radiation belt; Red: numerical approximation of the intensity profile from Equation (1).

**Fig. 2.** Local ratio  $\epsilon(r, \theta, \phi)$  of the local Lyman- $\alpha$  illumination (influenced by multiple scattering effects) and the original solar illumination within the ecliptic plane calculated with a multiple scattering Monte Carlo model (Zoennchen et al., 2015).

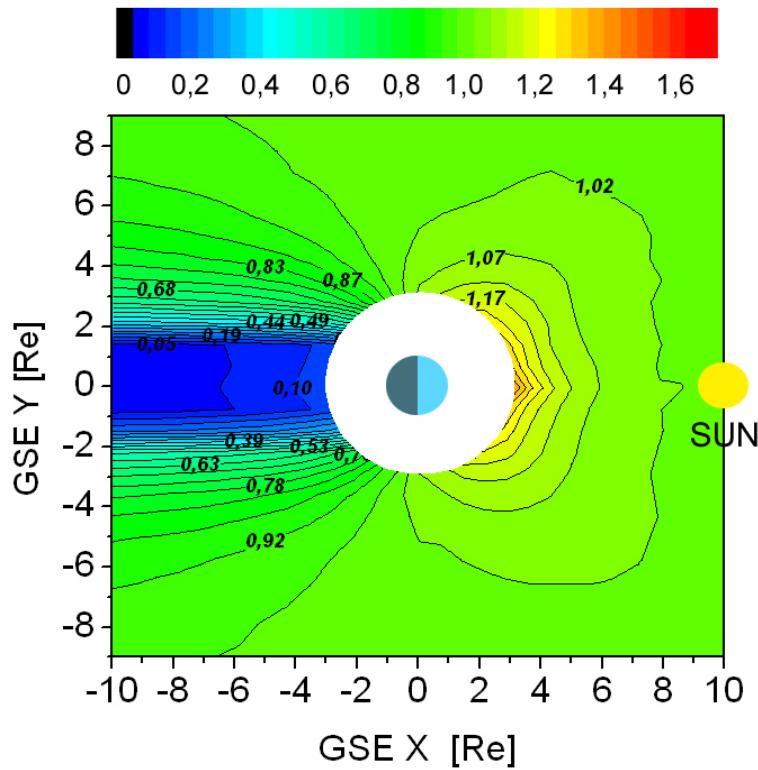
**Fig. 3.** (A) observed, uncorrected Lyman- $\alpha$  profile by UVIS/HDAC in [counts/s] from Equation (2) (black line) and the calculated column brightness profiles based on the TWINS 3D H-density model (red line) and the  $1/R^3$  model (blue line), both including background and in [R]  
(B) ratios between the UVIS/HDAC observed and the calculated profiles: with the TWINS H-density model (red line) and with the  $1/R^3$  model (blue line).

**Fig. 4.** (Black squares): Radial symmetric H-density profile (Equation (7)) fitted from UVIS/HDAC observations; (Red line): Powerlaw fit of the H-density profile in the lower radial range  $3-7 R_e$ ; (Cyan line): Powerlaw fit of the H-density profile in the upper radial range  $9-15 R_e$ ; The deviation of the red and the cyan lines from the **black squares** indicate, that the H-density profiles falls faster at larger distances  $>8 R_e$  than at lower distances  $<8 R_e$ .

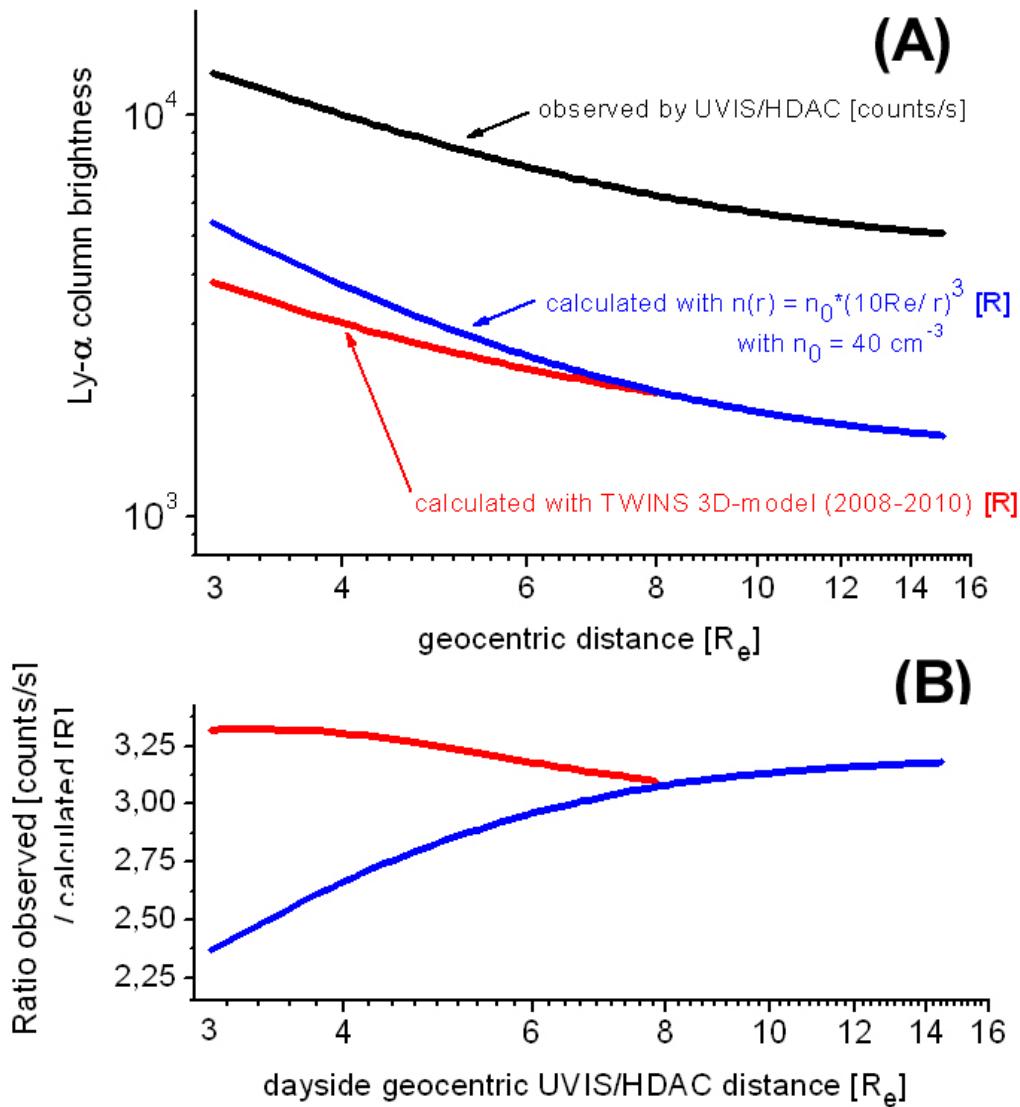
## Figures:



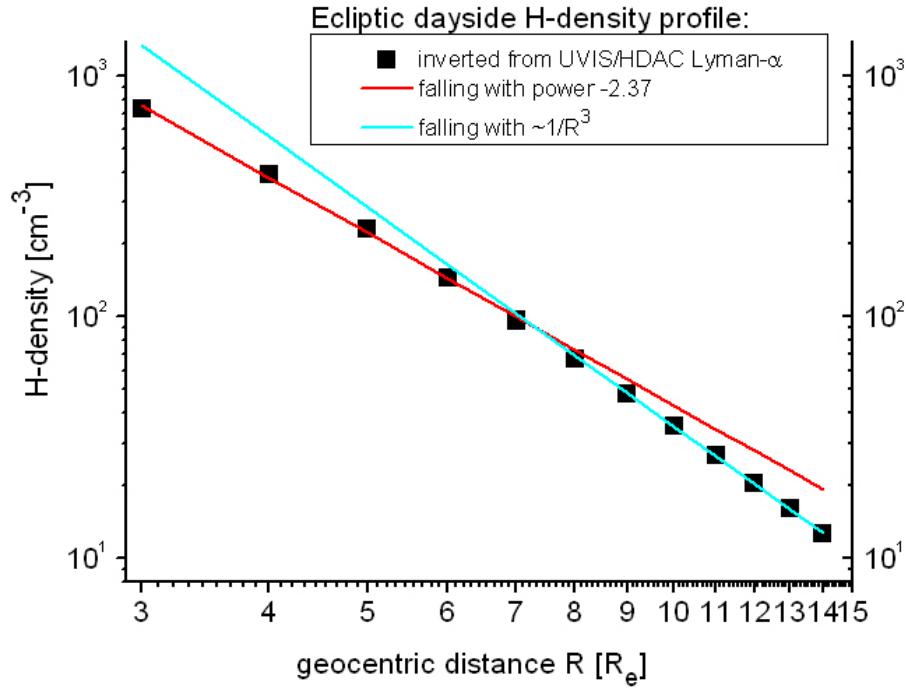
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