

Reply to referees

Manuscript "Magnetosheath plasma flow model around Mercury" by Schmid et al.

We thank the both reviewers for taking time to carefully read and raise comments and suggestions. All the comments are well justified and helpful. The quality of manuscript has improved a lot thanks to the reviewer comments. We give our reply to each of the review comments in the following in red and changes in the manuscript are marked in blue.

Reviewer 1

[1.1]

- > This paper presents an analytical magnetosheath model for the Mercury environment.
- > The model is built on existing bricks that were published in the literature for the Earth
- > and were adapted for Mercury, notably the models for the bow shock and the
- > magnetopause. The procedure is well described and the code (in IDL) is given in reference
- > such that the user can easily adapt the model to any other particular use. I have a number
- > of non-blocking comments below that should be addressed by the authors before
- > publication. The paper deserves publication.
- >
- > Discussions points:
- > Do the authors foresee specific applications for their model at Mercury ?

Yes, and we added the following text (page 10, line 205--212):

"Two applications are in mind in view of the BepiColombo mission, where the Mercury Magnetospheric Orbiter (MMO also referred to as Mio) will probe Mercury's magnetosheath and solar wind with unprecedented fast measurements of the particle distribution functions: (1) the Tatrallyay method to observationally determine the growth rate or damping rate of specific mode such as the mirror mode along the streamline (Tatrallyay and Erdos, 2002; Tatrallyay et al., 2008), and (2) the Guicking method to observationally track the spectral evolution of turbulent fluctuations along the streamline (Guicking et al., 2010, 2012).

[1.2]

- > I would like to see a longer discussion on the limitation of constant density
- > in the magnetosheath. As this hypothesis implies a constant velocity along a given
- > flow line, it produces (Figure 3) a very different velocity patterns that the previous
- > models (Spreiter et al., 1966; Genot et al., 2011, Soucek & Escoubet, 2012) and will
- > likely underestimate propagation timing in the magnetosheath.

True and agreed. We added a paragraph (page 12, line 253--256):

"The assumption of constant density implies a constant velocity along a given flow line. The velocity profile may vary considerably from that estimated in the earlier models such as the Spreiter model (Spreiter et al., 1966), the Genot model (Genot et al., 2011), and the Soucek-Escoubet model

(Soucek and Escoubet, 2012). The constant density will likely underestimate the propagation timing in the magnetosheath."

[1.3]

- > Solar wind at Mercury
- > I don't find the explanation on how the solar wind parameters at Mercury
- > are computed very well described. It could be specified that the model
- > is 1D MHD and takes OMNI as input to compute propagation at all solar
- > system objects including Mercury.

Done. A sentence was added in the paragraph (page 8, line 163--165):

"The model is one-dimensional magnetohydrodynamic, and takes the OMNI dataset as input to compute propagation at all solar system bodies including Mercury."

[1.4]

- > Then I don't understand what are the average θ_{Vn} and θ_{Bn} ?
- > It does not make sense as these values depend on the position on
- > the shock (and on the shock model itself).

We use the average $|B_r|$ and $|B_t|$ values (which are the radial and tangential components of IMF) from the Tao dataset. The angles θ_{Vn} and θ_{Bn} are calculated from the averaged magnetic field components, $|B_r|$ and $|B_t|$, with respect to the bow shock normal, stream-wise traced upstream to the shock for the virtual spacecraft at $x = -3 R_m$ and $\rho = 3 R_m$. To avoid confusion, we use the averaged magnetic field components, $|B_r| \approx 18 \text{ nT}$ and $|B_t| \approx 6 \text{ nT}$, in the revision.

We added the following sentences (page 9 line 180--182):

"the average input solar wind plasma parameters for our model are: density of $n^u \approx 40 \text{ cm}^{-3}$, temperature of $T \approx 18 \text{ eV}$, flow speed of $|v^u| \approx 400 \text{ km/s}$, magnetic field magnitude of $|B^u| \approx 20 \text{ nT}$ with the radial component $B_r \approx 18 \text{ nT}$ (ignoring the sign) and the tangential component $B_t \approx 6 \text{ nT}$ (ignoring the sign)."

[1.5]

- > A note could be added on the average Parker angle at Mercury. From
- > the Tao dataset one finds 23° which is also the value for Mercury
- > at an average position of 0.4 UA and solar wind velocity of 400 km/s .
- > Note that the Tao B_x value is computed from the model B_y value and
- > an hypothesis of Parker field line which is consistent with the identical
- > 23° values above.

Agreed. Done. Page 9, line 184--187.

"It is worthwhile to note that one finds an angle of 23° from the Tao dataset, which is consistent to the spiral angle at Mercury at an average position of 0.4 astronomical units (AU) from the Sun for a solar wind speed of

400 km s⁻¹. The B_x component is computed from the B_y component using the Parker spiral field in the Tao model.

[1.6]

- > I confirm the average values given in the paper (n=40 cm⁻³, T=18 eV,
- > v=400 km/s, b=20 nT) for the ~1500 days of observations of
- > the Messenger mission. As |v^u| is a magnitude I would indicate
- > 400 instead of -400 km/s.

Thank you! Included to page 9, line 182–184:

"The mean values of density, temperature, flow speed, and magnetic field are valid for nearly 1500 days of observations of MESSENGER (confirmed by one of the reviewers)."

[1.7]

- > Please compute the corresponding M_A and beta values and
- > indicate them on Figure 3.

Done (Fig. 3 caption, page 10). We also mention the Alfvén Mach number and the plasma beta value in the main text. See page 9, line 187–189.

"The Alfvén Mach number in the upstream region is $MA = v^u / VA \approx 5.8$ (with an Alfvén speed of $VA \approx 69 \text{ km s}^{-1}$) and the plasma parameter beta (upstream) is $\beta = 2\mu_0 n k_B T / B^2 \approx 0.72$ (where μ_0 is the permeability of free space and k_B the Boltzmann constant) in our setup."

[1.8]

- > Orbital motion
- > Please explain the procedure for the orbital motion correction briefly
- > described at L147. The exact transformation should be given, perhaps
- > in a short appendix.

The transformation is explained (page 8, line 164 to page 9, line 177):

"The model is one-dimensional magnetohydrodynamic, and takes the OMNI dataset as input to compute propagation at all solar system bodies including Mercury. The correction for the orbital motion is achieved by adding the solar wind velocity vector, V_{SW}, (which is radially away from the Sun) and the orbital motion velocity vector of Mercury, V' with $V = V_{SW} + V'$. To obtain V' we use the dataset provided from Navigation and Ancillary Information Facility (NAIF, Acton, 1996) which provide the distance between Mercury and Sun, D, and absolute velocity of Mercury, V'. To determine aberration velocity vector, we first calculate the aberration angle ϕ on basis of Mercury's elliptical orbit with

$$\phi = \text{atan}(b/(\sqrt{a^2 - b^2} * \sin(\text{acos}((1 - p/D)/e))), \quad (15)$$

where a is the semimajor axis, b the semiminor axis, p the semi-latus rectum and e the eccentricity of the ellipse. With the aberration angle φ and the consideration whether Mercury moves towards/away from the sun we subsequently obtain the aberration velocity vector $V'_x = (+/-) |V'| \sin(\varphi)$ and $V'_y = |V'| \cos(\varphi)$. The transformation due to this aberration effect is made by applying a two-dimensional rotation matrix to the spatial coordinates (spanning the x and ρ coordinates):

$$\begin{pmatrix} x' \\ y' \end{pmatrix} = \begin{pmatrix} x \cos \theta_a - \rho \sin \theta_a \\ x \sin \theta_a + \rho \cos \theta_a \end{pmatrix} \begin{pmatrix} x \\ \rho \end{pmatrix}$$

where the aberration angle is given by the radial solar wind velocity V_{SW} and the apparent solar wind velocity V with $\theta_a = \cos^{-1}(V_{SW} \cdot V)$

[1.9]

> Equation 11

> I'm grateful to the authors for bringing my attention to Anderson, 1963

> that I had overlooked. I checked Equation 11 of the paper that is equivalent

> to Equation 2.43 of Anderson et al., 1963 although the notations are different.

> However, I have a problem with its solution. I ran the piece of code

> given by the authors, and I also used an independent method

> (Cardan for 3rd degree polynoms) in Python; both approaches give the

> same solution for the compression ratio as a function of θ_{Bn} and

> it is reproduced on the figure below for nominal solar wind

> conditions ($Ma=12$, $\beta=3$). The curve tends towards zero for perpendicular shocks.

> Entropy considerations preclude compression ratio below 1.

> So I'm wondering if the equation, hence the model, always leads

> to a physical solution for all solar wind inputs.

Thank you for the elaborate check! We only consider solutions between $1 \leq R \leq 4$, otherwise the program stops and the model does not provide a solution. Although the equation also yields a solution for $R < 1$, it has not a physical meaning, as that would entail a decrease in entropy from the upstream to the downstream side and thus would violate the second law of thermodynamics, as the referee correctly mentioned. Note that the upper limit $R \rightarrow 4$ is given in the high Alfvén Mach number limit ($M_A \rightarrow \infty$) under the assumption $\gamma = 5/3$.

We added the following text (page 8, line 148--153):

"Equation (15) is equivalent to Eq. 2.43 in Anderson (1963) with different notations. The solution is given in the form of compression ratio as a function of the shock angle θ_{Bn} . Solutions exist for a compression ratio in the range $1 \leq R \leq 4$ when using Eq. (12). Another class of solutions also exists for the expansion ($R < 1$) with a decrease of entropy from the upstream onto the downstream side. The latter case is not physically relevant, and is not considered here. The upper limit of compression ratio ($R \leq 4$) corresponds to the limit of high Alfvén Mach number ($MA \rightarrow \infty$) under

a polytropic index of $\gamma = 5/3$."

[1.11]

- > IDL code available at the OSF page
- > I was able to run the code satisfactorily and trace a low line from
- > a point in the magnetosheath (see below). The code is well commented.
- > This may be outside of the scope of this review though, but it shows
- > that the work complies with reproducibility principles.

Thank you!

[1.12]

- > Minor points
- > Figure 2 : please specify the parameters (M_A , β , ...) for which the figure is drawn

In Figure 2 five examples of streamlines are shown. No M_A and β values are necessary.

[1.13]

- > Figure 3 : same comment

Done. See Fig. 3 caption (page 10).

[1.14]

- > L123: reference of frame -> frame of reference

Done. Page 6, line 134.

[1.15]

- > L130 : the upstream magnetic field ; the shock normal

Done. Page 7, line 141.

[1.16]

- > L131 : why adding the last part "w.r.t. the shock normal" ? it is unnecessary here.

Deleted. The sentence closes now with "the upstream Alfvén Mach number." Page 7, line 142.

[1.17]

- > L138 : Equation 4 -> Equation 11

Corrected to Eq. (14). Page 8, line 154.

[1.18]

- > L158 : a word is missing in front of the reference

Corrected into "... based on the magnetosheath model by Soucek and Escoubet (2012)." Page 9, line 202.

Magnetosheath plasma flow model around Mercury

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Abstract.

The magnetosheath is defined as the plasma region between the bow shock, where the super-magnetosonic solar wind plasma is decelerated and heated, and the outer boundary of the intrinsic planetary magnetic field, the so-called magnetopause. Based on the Soucek-Escoubet magnetosheath flow model at the Earth, we present an analytical magnetosheath plasma flow model around Mercury. The model can be used to estimate the plasma flow magnitude and direction at any given point in the magnetosheath exclusively on the basis of the plasma parameters of the upstream solar wind. The model serves as a useful tool to trace the magnetosheath plasma along the streamline both in a forward sense (away from the shock) and a backward sense (toward the shock), offering the opportunity of studying the growth or damping rate of a particular wave mode or evolution of turbulence energy spectra along the streamline in view of upcoming arrival of BepiColombo at Mercury

10 1 Introduction

The magnetosphere of a planet constitutes an obstacle to the super-magnetosonic solar wind. Upstream of the planet a bow shock emerges, because the interplanetary magnetic field (IMF), embedded in the solar wind, cannot simply penetrate the magnetosphere. At the bow shock the super-magnetosonic solar wind plasma is decelerated and heated. The region with the subsonic, heated plasma downstream of the bow shock is called magnetosheath. The magnetosheath plays an important role in the interaction between bow shock and magnetosphere as it conveys energy between the solar wind and the planetary magnetosphere.

One of the earliest magnetosheath plasma flow models is the hydrodynamic model introduced by Spreiter *et al.* (1966). Basically the model solves the gas-dynamic differential equations of an unmagnetized fluid around an obstacle, represented by the magnetosphere. It has successfully been tested against in-situ spacecraft data (Song *et al.*, 1999; Stahara *et al.*, 1993; Spreiter and Alksne, 1968) and applied to model the magnetospheres of various planets in our solar system (see Stahara, 2002, for a review). A decisive drawback of this model, however, is the high complexity and computational demands to calculate numerically a set of differential equations.

To reduce the computational complexity, several analytical plasma flow models have alternatively been proposed (Russell *et al.*, 1983; Kallio and Koskinen, 2000; Romashets *et al.*, 2008). An analytical magnetosheath flow model, which has success-

25 fully been tested against spacecraft observations at Earth, has been implemented by *Soucek and Escoubet (2012)*. This model is based on the magnetic field model developed by *Kobel and Flückiger (1994)* and later modified and extended by *Génot et al. (2011)* to obtain a magnetosheath plasma flow model. The essential advantage of this model is its compatibility with a wide range of bow shock and magnetopause models while retaining the simplicity and computational efficiency of the original magnetic field model. Furthermore, the model allows to calculate the plasma flow velocity at any point in the magnetosheath using only the spacecraft position and solar wind parameter upstream of the bow shock.

In this work we follow the procedure proposed by *Soucek and Escoubet (2012)* and rescale their terrestrial magnetosheath flow model to the space environment at Mercury. First, we introduce the Hermean bow shock and magnetopause model, used to obtain the magnetosheath plasma flow model. Second, we revisit the magnetic field model of *Kobel and Flückiger (1994)* which *Soucek and Escoubet (2012)* used to determine the plasma velocity direction in the magnetosheath. Third, we extend the model by the Rankine-Hugoniot relations in a similar way as *Génot et al. (2011)* to determine the velocity magnitude downstream of the shock.

The aim of this paper is to provide a tool to estimate the plasma flow at a given point of spacecraft observation inside the Hermean magnetosheath on the basis of the solar wind conditions.

2 Bow shock and magnetopause model at Mercury

40 In the following we use an aberrated Mercury Solar Magnetospheric (MSM) coordinate system. This coordinate system is based on the Mercury Solar Orbital (MSO) coordinate system, but its origin is shifted northward by 479 km from the MSO origin to account for Mercury's dipole offset and rotated into the solar wind velocity direction. In the MSO coordinate system the X_{MSO} -axis points sunward, the Y_{MSO} -axis points anti-parallel to Mercury's orbital velocity, and $Z_{\text{MSO}} = X_{\text{MSO}} \times Y_{\text{MSO}}$ completes the right-handed system. To compensate for the aberration of the solar wind direction due to the orbital motion of Mercury around the sun, the X_{MSO} -axis is rotated anti-parallel to the solar wind flow velocity direction. In the MSM coordinate system the bow shock and magnetopause models are considered to be cylindrically symmetric around the X_{MSM} -axis, reducing the three dimensions $\{X_{\text{MSM}}, Y_{\text{MSM}}, Z_{\text{MSM}}\}$ to two dimensions $\{X_{\text{MSM}}, \rho_{\text{MSM}}\}$ with $\rho = \sqrt{Y_{\text{MSM}}^2 + Z_{\text{MSM}}^2}$.

Slavin et al. (2009) modeled the bow shock at Mercury by a conic section of the form

$$\xi = \sqrt{(x_{BS} - x_0)^2 + \rho_{BS}^2} = \frac{p\epsilon}{1 + \epsilon \cos\phi}, \quad (1)$$

50 with x_0 the distance of the focus of the conic section from the dipole center along X_{MSM} , $\rho_{BS} = \sqrt{y_{BS}^2 + z_{BS}^2}$ the distance from the X_{MSM} -axis, p the focal parameter, and ϵ the eccentricity. With the advent of the MESSENGER (MErcury Surface, Space ENvironment, GEophysics and Ranging *Solomon et al., 2007*) spacecraft in an orbit around Mercury, it was possible to characterize the spatial location of the bow shock and magnetopause statistically. *Winslow et al. (2013)* determined that the best-fit parameters to the bow shock are given by $x_0 = 0.5 R_{\text{M}}$, $p = 2.75 R_{\text{M}}$ and $\epsilon = 1.04$. With these parameters the extrapolated subsolar bow shock stand-off distance is $R_{\text{BS}} = 1.9 R_{\text{M}}$ (Mercury radii, $1 R_{\text{M}} \sim 2440 \text{ km}$). For this work it is

advantageous to transform Equation (1) into the origin of the MSM coordinate system with

$$\begin{aligned} r_{BS} &= \sqrt{(\xi \cos \phi + x_0)^2 + (\xi \sin \phi)^2}, \\ \theta &= \cos^{-1} \left(\frac{\xi \cos \phi}{r_{BS}} \right), \end{aligned} \quad (2)$$

where r_{BS} is the distance from the dipole center to the bow shock and θ the angle between r_{BS} and the X_{MSM} -axis. Figure 1 shows a schematic illustration of the parameters ξ , ϕ , r_{BS} and θ , which are used in the formulation of the bow shock.

Korth et al. (2015) used the magnetopause model proposed from *Shue et al. (1997)* and found that the MESSENGER observations of magnetopause crossing are best-fit by

$$r_{MP} = \sqrt{x_{MP}^2 + \rho_{MP}^2} = R_{MP} \left(\frac{2}{1 + \cos \theta} \right)^\alpha, \quad (3)$$

with $\alpha = 0.5$ the best-fit flaring parameter, and $R_{MP} = 1.42 R_M$ the subsolar stand-off magnetopause distance.

Figure 1 shows the the *Slavin et al. (2009)*-bow shock model (S09-BS) and *Korth et al. (2015)*-magnetopause model (K15-MP) evaluated from Equations (2) and (3), respectively.

3 The KF94 magnetic field model

To obtain the magnetosheath plasma flow direction we follow the procedure proposed by *Soucek and Escoubet (2012)* and use the magnetic field model developed by *Kobel and Flückiger (1994)*. In the following we denote this model as KF94-model and mark all quantities pertaining to the KF94-model by a tilde $\tilde{\cdot}$. In the KF94-model the bow shock (BS) and magnetopause (MP) at Mercury are modeled by parabolic surfaces at a common focus with

$$\tilde{r}_{\{BS,MP\}} = \frac{-\cos \theta + \sqrt{\cos^2 \theta + 4R_{\{BS,MP\}} b_{\{BS,MP\}} \sin^2 \theta}}{2b_{\{BS,MP\}} \sin^2 \theta}, \quad (4)$$

with $b_{BS} = 1/(4R_{BS} - 2R_{MP})$ and $b_{MP} = 1/(2R_{MP})$ defined by the stand-off distances $R_{\{BS,MP\}}$.

Under the assumption that the IMF is parallel to the solar wind, the magnetic field lines of the KF94-model represent the flowlines of the solar wind and magnetosheath plasma. Using the magnetic field vector direction in the KF94-model, *Soucek and Escoubet (2012)* determined the flow velocity vector at a given position $\mathbf{r} = (x, \rho)$ by

$$\begin{aligned} \tilde{v}_x &= v_m (C/2d - C/R_{MP}), \\ \tilde{v}_\rho &= v_m (C\rho/[2d(d+x - R_{MP}/2)]), \end{aligned} \quad (5)$$

where v_m corresponds to the flow velocity magnitude, $d = |\mathbf{r} - \mathbf{r}_0|$ the difference between the given position in the magnetosheath and the parabolic surface focus $\mathbf{r}_0 = (R_{MP}/2, 0)$, and $C = R_{MP}(2R_{BS} - R_{MP})/(2R_{BS} - 2R_{MP})$ a constant defined by the bow shock and magnetopause stand-off distances.

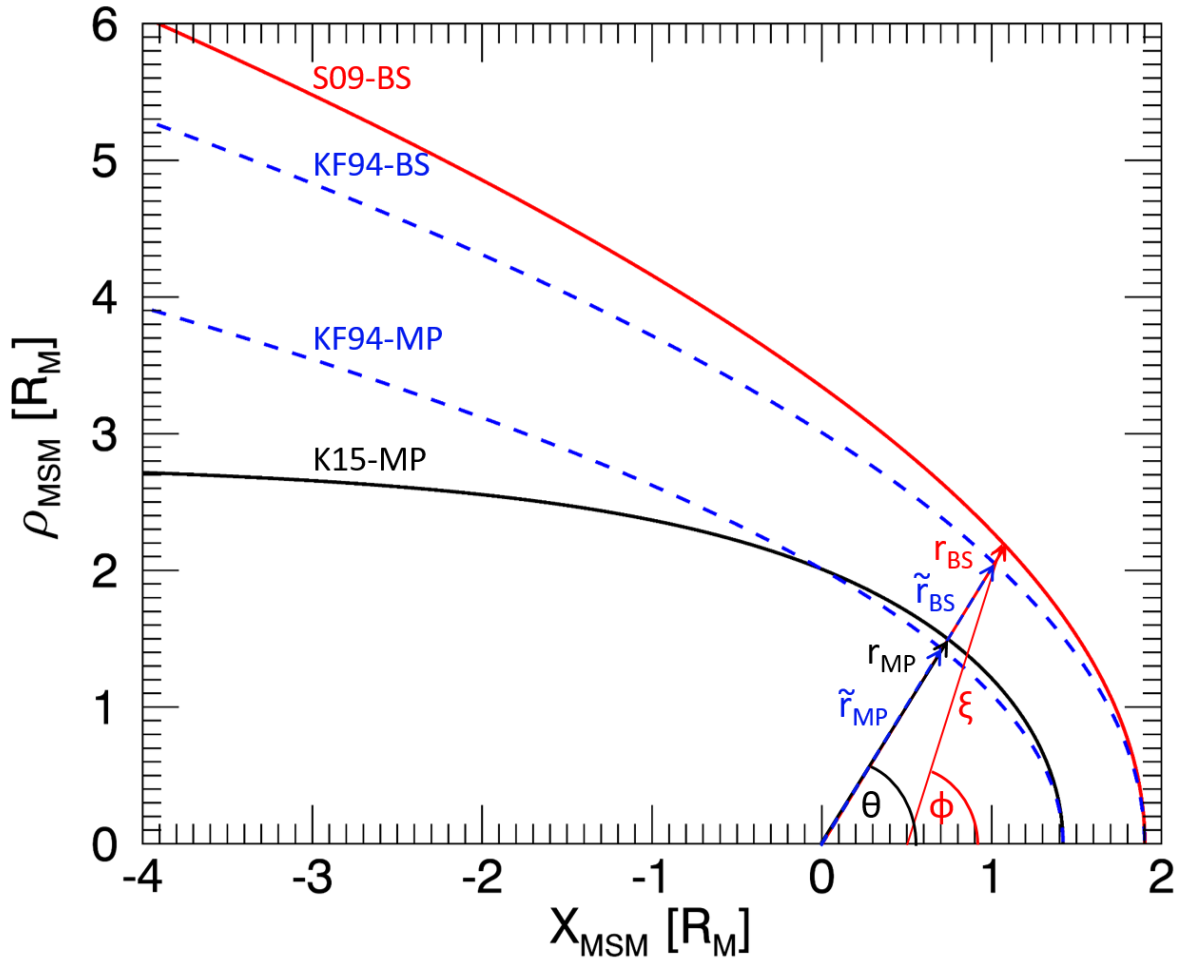


Figure 1. Schematic representation of the parameters used in the formulation of the bow shock and magnetopause in the MSM equatorial plane. The solid red line is the bow shock evaluated from Equation (2) (S09-BS, *Slavin et al.*, 2009). The solid black line represents the magnetopause determined by Equation (3) (K15-MP, *Korth et al.*, 2015). The dashed blue lines are the bow shock and magnetopause determined by Equation (4) from the KF94-model (*Kobel and Flückiger*, 1994).

4 The magnetosheath plasma flow model around Mercury

To obtain the magnetosheath plasma flow at a specific point ($\mathbf{r} = (x, \rho)$) in the magnetosheath at Mercury, we evaluate the plasma flow direction first, and then determine the magnitude of the velocity vector from the Rankine-Hugoniot relation across the bow shock.

85

A magnetic field model is used to describe the plasma flow here. The reason for this is explained as follows. Assumptions are made such that there are no proton sinks or sources in the magnetosheath. Strictly speaking, this assumption is only weakly

justified because of the neutral particles such as the hydrogen corona and the sodium exosphere around Mercury. A stationary case is taken in the fluid picture. The continuity equation reads then:

$$90 \quad \nabla \cdot (n\mathbf{U}), \tag{6}$$

where n and \mathbf{U} are the density and velocity of protons, respectively. Now we make an analogy such that

$$(n\mathbf{U}) \longrightarrow \mathbf{B}, \tag{7}$$

holds, and Equation 6 is equivalent to the divergence-free condition of magnetic field,

$$\nabla \cdot \mathbf{B} = 0, \tag{8}$$

95 For a more detailed discussion see e.g. *Génot et al. (2011)*.

4.1 Plasma flow direction

Following the procedure proposed by *Soucek and Escoubet (2012)*, we rescale the plasma flow direction from the KF94-model to Mercury's space environment as follows:

1. As a first step we calculate the angle $\theta = \cos^{-1}(x/\sqrt{x^2 + \rho^2})$ between \mathbf{r} and the X_{MSM} -axis.

100 2. Then we estimate the fractional distance, \mathcal{F} , of \mathbf{r} between the bow shock and magnetopause from Equations (2) and (3) with

$$\mathcal{F} = \frac{r(\theta) - r_{\text{BS}}(\theta)}{r_{\text{BS}}(\theta) - r_{\text{MP}}(\theta)}. \tag{9}$$

3. Now we change into the KF94-model and calculate $\tilde{r}_{\text{BS}}(\theta)$ and $\tilde{r}_{\text{MP}}(\theta)$ from Equation (4) with the angle θ . Note that the stand-off distances (R_{BS} and R_{MP}) and the focus ($\mathbf{r}_0 = (R_{\text{MP}}/2, 0)$) in Equation (4) are the best-fit values from
105 Equations (2) and (3).

4. In a next step we determine the fractional position within the magnetosheath in the KF94-model with

$$\tilde{r}(\theta) = \mathcal{F}[\tilde{r}_{\text{BS}}(\theta) - \tilde{r}_{\text{MP}}(\theta)] + \tilde{r}_{\text{BS}}(\theta), \tag{10}$$

according to Equation (9).

5. Using Equation (5) we evaluate the KF94 flow velocity vector, $\tilde{\mathbf{v}}$, at the position $\tilde{r}(\theta)$. Note that the velocity magnitude
110 v_{m} is determined in a later step.

6. With the obtained flow velocity vector, $\tilde{\mathbf{v}}$, we are able to estimate the new position of an adjacent point along the same flowline $\tilde{\mathbf{r}}' = \tilde{\mathbf{r}} + \tilde{\mathbf{v}}\Delta t$, by choosing an infinitesimally small time increment Δt .

7. Next we determine the angle between the new position and the X_{MSM} -axis, θ' , and the fractional distance inside the KF94 magnetosheath, \mathcal{F}' , using Equation (9).
- 115 8. Finally we transform the new position $\tilde{\mathbf{r}}'(\theta')$ back from the KF94-model to the original MSM reference frame where the magnetosheath is confined by Equations (2) and (3). The new position, \mathbf{r}' , inside this magnetosheath is then given by

$$\mathbf{r}' = \mathcal{F}' [\mathbf{r}_{\text{BS}}(\theta') - \mathbf{r}_{\text{MP}}(\theta')] + \mathbf{r}_{\text{BS}}(\theta'), \quad (11)$$

and thus the plasma flow direction can be determined by $\mathbf{v} = (\mathbf{r}' - \mathbf{r})/\Delta t$.

Applying recursively this procedure (step(1)-(8)) yields the plasma flowline within Mercury's magnetosheath. In Fig.2 five
120 examples of flowlines are shown.

4.2 Plasma flow magnitude

To evaluate the magnetosheath plasma velocity magnitude, v_m , we apply the Rankine-Hugoniot (RH) equations, which relate the upstream (u) with the downstream (d) plasma conditions. The downstream plasma flow velocity directly behind the bow shock, v^d , is derived by the following procedure:

- 125 1. From the given spacecraft position in the magnetosheath, $\mathbf{r} = (x, \rho)$, we trace the flowline back to the bow shock. Thereto we iteratively apply steps (1)-(8) from above, with reversed increments $\tilde{\mathbf{r}}' = \tilde{\mathbf{r}} - \tilde{\mathbf{v}}\Delta t$ in step (6), until the bow shock is reached ($\mathcal{F}' = 0$). Then we calculate the angle θ_{BS} between the X_{MSM} -axis and the bow shock intersection at $(x_{\text{BS}}, \rho_{\text{BS}})$ with $\theta_{\text{BS}} = \cos^{-1}(x_{\text{BS}}/\sqrt{x_{\text{BS}}^2 + \rho_{\text{BS}}^2})$.
- 130 2. In a next step we determine the bow shock tangent $\hat{\mathbf{t}}$ and normal $\hat{\mathbf{n}}$ unit vectors where the back-traced flowline intersects the bow shock. For any point along the bow shock, the normal, \mathbf{n} , and tangent, \mathbf{t} , vector can easily be computed by

$$\begin{aligned} \mathbf{t} &= \left[\frac{dr_{\text{BS}}}{d\theta} \cos\theta - r_{\text{BS}} \sin\theta \right] \hat{\mathbf{e}}_x + \left[\frac{dr_{\text{BS}}}{d\theta} \sin\theta + r_{\text{BS}} \cos\theta \right] \hat{\mathbf{e}}_\rho, \\ \mathbf{n} &= \left[\frac{dr_{\text{BS}}}{d\theta} \sin\theta + r_{\text{BS}} \cos\theta \right] \hat{\mathbf{e}}_x - \left[\frac{dr_{\text{BS}}}{d\theta} \cos\theta + r_{\text{BS}} \sin\theta \right] \hat{\mathbf{e}}_\rho, \end{aligned} \quad (12)$$

where $\frac{dr_{\text{BS}}}{d\theta}$ is numerically calculated from two consecutive points along the bow shock given by Equation (2). The shock reference [frame of reference](#) is then defined by the normalized normal and tangent vector at θ_{BS} .

- 135 3. In the shock reference frame the RH-equations can be combined to determine the downstream velocity vector component parallel v_n^d and perpendicular v_t^d to the shock normal (see e.g. *Génot, 2008*)

$$\begin{aligned} v_n^d &= v_n^u \frac{1}{\mathcal{R}}, \\ v_t^d &= v_n^u \left(\tan\theta_{\text{Vn}} + \frac{1 - 1/\mathcal{R}}{[M_{\text{A}}^{u2}/(\mathcal{R}\cos^2\theta_{\text{Bn}})] - 1} \tan\theta_{\text{Bn}} \right), \end{aligned} \quad (13)$$

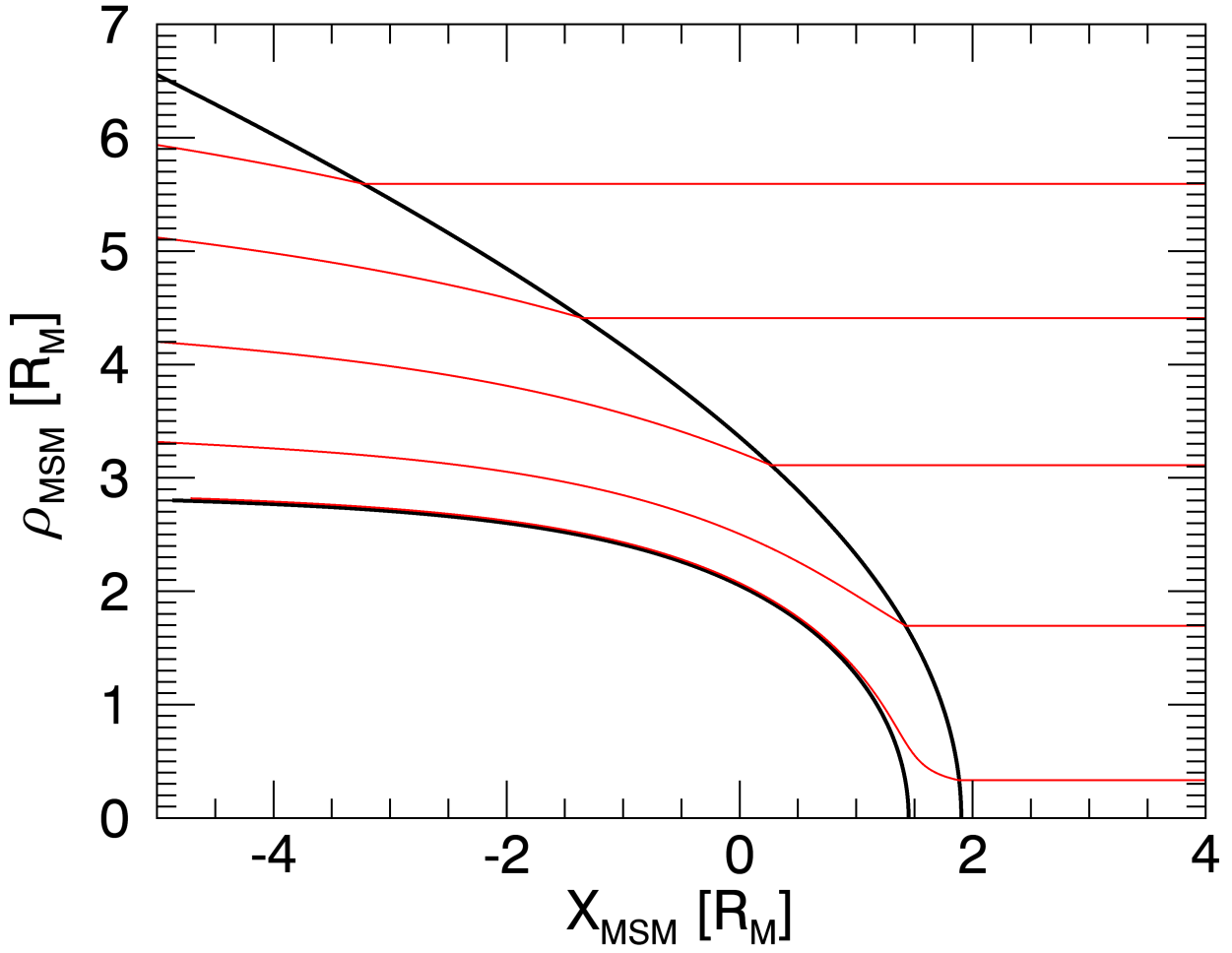


Figure 2. Schematic representation of the flowlines (red) in the MSM equatorial plane. The solid black lines are the bow shock and magnetopause evaluated from Equations (2) and (3), respectively.

where v_n^u is the upstream velocity vector component parallel to the shock normal, $\mathcal{R} = \rho^d / \rho^u$ the compression ratio between the upstream and downstream mass density, $\theta_{Vn} = \tan^{-1}(v_t^u / v_n^u)$ the angle between the upstream velocity vector and the shock normal, $\theta_{Bn} = \tan^{-1}(B_t^u / B_n^u)$ the angle between upstream magnetic field vector and shock normal, and $M_A^u = v_n^u \frac{\sqrt{\mu_0 \rho^u}}{B_n^u}$ the upstream Alfvén Mach number.

4. In Equation (13) all parameters pertain to the upstream side, except the compression ratio \mathcal{R} . However, \mathcal{R} can also be expressed by exclusively upstream parameters with (see e.g. *Anderson, 1963*)

$$145 \quad (M_A^{u2} - \mathcal{R})^2 (\gamma \beta^u \mathcal{R} + M_A^{u2} \cos^2 \theta_{\text{Bn}} [(\gamma - 1)\mathcal{R} - (\gamma + 1)]) + \\ \mathcal{R} M_A^{u2} \sin^2 \theta_{\text{Bn}} ([\gamma + (2 - \gamma)\mathcal{R}] M_A^{u2} + \mathcal{R} [(\gamma - 1)\mathcal{R} - (\gamma + 1)]) = 0 \quad (14)$$

where $\beta^u = (2\mu_0 p^u)/B^{u2}$ is the ratio of the upstream thermal to magnetic pressures, and γ the polytropic index which is typically assumed to be $\gamma = 5/3$. Equation 14 is equivalent to Equation 2.43 in *Anderson (1963)* with different notations. The solution is given in the form of compression ratio as a function of the shock angle θ_{Bn} . Solutions exist for a compression ratio in the range $1 \leq \mathcal{R} \leq 4$ when using Equation 14. Another class of solutions also exists for the expansion ($\mathcal{R} < 1$) with a decrease of entropy from the upstream onto the downstream side. The latter case is not physically relevant, and is not considered here. The upper limit of compression ratio ($\mathcal{R} = 4$) corresponds to the limit of high Alfvén Mach number ($M_A \rightarrow \infty$) under a polytropic index of $\gamma = 5/3$.

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155 5. By solving Equation 14 for \mathcal{R} the downstream velocity magnitude $v_d = \sqrt{v_n^{d2} + v_t^{d2}}$ is therefore entirely determined by only the upstream plasma parameters.

Since the detailed density profile along the flowline is unknown, we assume in a first approximation a constant plasma density and thus a constant velocity magnitude along the flowline. Therefore, the velocity magnitude at a given point \mathbf{r} , directly corresponds to the velocity magnitude downstream of the shock and $v_m = v_d$. Although this assumption has the tendency to underestimate the velocity close to the magnetopause, it yields satisfactory results in a first approach (*Génot et al., 2011*).

160 The entire procedure from above is implemented in an IDL computer program which can be retrieved from OSF (*Schmid, 2020*). The program is designed to evaluate the plasma flow velocity vector at a given observation point of a spacecraft inside the Hermean magnetosheath exclusively on basis of the upstream solar wind conditions. As the solar wind input parameters we use the solar wind propagation model of *Tao et al. (2005)* which is modified by the orbital motion of Mercury. The model is one-dimensional magnetohydrodynamic, and takes the OMNI dataset as input to compute propagation at all solar system
165 bodies including Mercury. The correction for the orbital motion is achieved by adding the solar wind velocity vector, \mathbf{V}_{SW} , (which is radially away from the Sun) and the orbital motion velocity vector of Mercury, $\mathbf{V}_{\text{♁}}$ with $\mathbf{V} = \mathbf{V}_{\text{SW}} + \mathbf{V}_{\text{♁}}$. To obtain $\mathbf{V}_{\text{♁}}$ we use the dataset provided from Navigation and Ancillary Information Facility (NAIF, *Acton, 1996*) which provide the distance between Mercury and Sun, D , and absolute velocity of Mercury, $V_{\text{♁}}$. To determine aberration velocity vector, we first calculate the aberration angle ϕ on basis of Mercury's elliptical orbit with

$$170 \quad \phi = \tan^{-1} \left(b / \sqrt{a^2 - b^2} \sin [\cos^{-1}((1 - p/D)/e)] \right), \quad (15)$$

where a is the semimajor axis, b the semiminor axis, p the semi-latus rectum and e the eccentricity of the ellipse. With the aberration angle ϕ and the consideration whether Mercury moves towards/away from the sun we subsequently obtain the aberration velocity vector $\mathbf{V}_{\text{♁},x} = \pm V_{\text{♁}} \sin(\phi)$ and $\mathbf{V}_{\text{♁},y} = \pm V_{\text{♁}} \cos(\phi)$. The transformation due to this aberration effect is

made by applying a two-dimensional rotation matrix to the spatial coordinates (spanning the x and ρ coordinates):

$$175 \quad \begin{pmatrix} x' \\ y' \end{pmatrix} = \begin{pmatrix} x \cos \theta_a & -\rho \sin \theta_a \\ x \sin \theta_a & \rho \sin \theta_a \end{pmatrix} \begin{pmatrix} x \\ \rho \end{pmatrix}, \quad (16)$$

where the aberration angle θ_a is given by the radial solar wind velocity, \mathbf{V}_{SW} , and the apparent solar wind velocity, \mathbf{V} with $\theta_a = \cos^{-1}(\mathbf{V}_{\text{SW}} \cdot \mathbf{V})$.

In Fig.3 the results of the model are shown for the average solar wind plasma parameters during the entire MESSENGER operation service between 2011 and 2015. After modifying the solar wind velocity vector of the *Tao et al.* (2005) model by
180 the orbital motion of Mercury (*Acton, 1996*), the average input solar wind plasma parameters for our model are: density of $n^u \approx 40 \text{ cm}^{-3}$, temperature of $T \approx 18 \text{ eV}$, flow speed of $|\mathbf{v}^u| \approx -400 \text{ km/s}$, magnetic field magnitude of $|\mathbf{B}^u| \approx 20 \text{ nT}$ with the radial component $B_r \approx 18 \text{ nT}$ (ignoring the sign) and the tangential component $B_t \approx 16 \text{ nT}$ (ignoring the sign). The mean values of density, temperature, flow speed, and magnetic field are valid for nearly 1500 days of observations of MESSENGER (confirmed by one of the reviewers). It is worthwhile to note that one finds an angle of 23° from the Tao dataset, which
185 is consistent to the spiral angle at Mercury at an average position of 0.4 astronomical units (AU) from the Sun for a solar wind speed of 400 km/s . The B_x component is computed from the B_y component using the Parker spiral field in the Tao model. The Alfvén Mach number in the upstream region is $M_A = v^u/V_A \approx 5.8$ (with an Alfvén speed of $V_A \approx 69 \text{ km/s}$) and the plasma parameter beta (upstream) is $\beta = 2\mu_0 n k_B T / B^2 \approx 0.72$ (where μ_0 is the permeability of free space and k_B the Boltzmann constant) in our setup. Color coded is the obtained velocity magnitude v_m . Additionally, the back-traced flowline
190 from a virtual spacecraft located at $x_{\text{MSM}} = -3R_M$ and $\rho_{\text{MSM}} = 3R_M$ is plotted (green line). At the bow shock intersection the calculated shock normal $\hat{\mathbf{n}}$ and tangent $\hat{\mathbf{t}}$ are illustrated in thin black lines. The thick black line downstream of the bow shock shows the velocity vector direction evaluated from the RH relations, which is in good agreement with the streamline direction determined by the KF94-model. At the virtual spacecraft position the model predicts a magnetosheath plasma flow velocity of $v_x \approx -200 \text{ km/s}$ and $v_\rho \approx 17 \text{ km/s}$.

195 A naive picture of the compression by a factor of 4 (in the limit of high Mach number) is not realistic because the interplanetary magnetic field around Mercury reaches a magnitude of 20 to 50 nT, and the Alfvén Mach number is correspondingly smaller than that around the Earth by 20 to 50, respectively. A picture of the constant density and a reduced flow speed to 1/4 of the solar wind speed at the magnetopause (along the streamline tangential to the magnetopause) is not valid, either, since the adiabatic expansion breaks down and the model is not applicable to the flow in the sub-solar region and at the magnetopause.

200 5 Discussion and Conclusions

Here we present the first analytical magnetosheath plasma flow model for the space environment around Mercury. The model is based on the magnetosheath model by *Soucek and Escoubet* (2012), which has successfully been tested against spacecraft observations at Earth. The proposed model is relatively simple to implement and provides the possibility to trace the flowlines inside the Hermean magnetosheath.

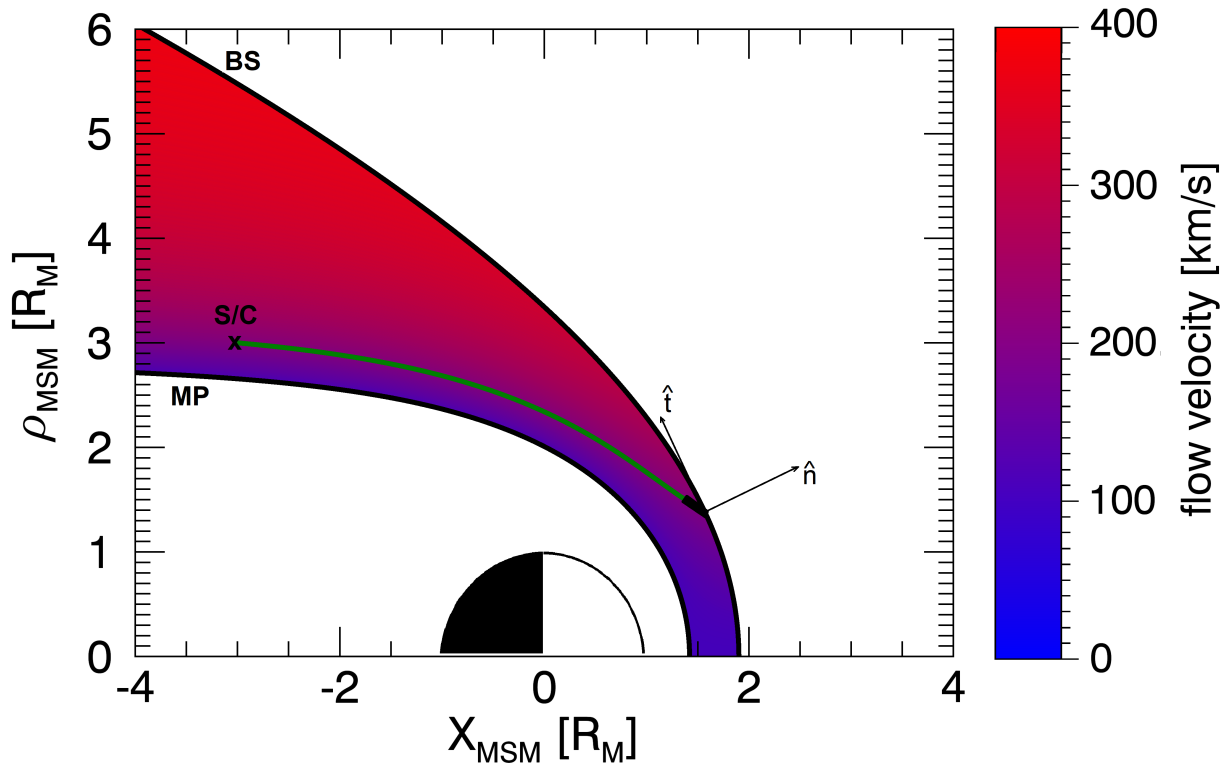


Figure 3. Color-coded flow speed calculated from Equation (13) with the averaged upstream parameters from the *Tao et al. (2005)* solar wind propagation model at Mercury between 2011 and 2015. Also plotted is a schematic representation of back-traced flowline (green) from a virtual spacecraft (S/C) to the bow shock (BS) with the respective shock normal \hat{n} and tangent \hat{t} obtained from Equation (12). The thick black line downstream of the BS is the downstream velocity vector direction determined by Equation (13). *Alfvén Mach number in 5.8 and plasma beta is 0.79.*

205 The model presented in this paper is generally robust and easy to implement for its analytic expression using upstream parameters. It can help to determine the local plasma conditions of a spacecraft in the magnetosheath exclusively on basis of the upstream solar wind parameters. Two applications are in mind in view of the BepiColombo mission, where the Mercury Magnetospheric Orbiter (MMO also referred to as Mio) will probe Mercury's magnetosheath and solar wind with unprecedented fast measurements of the particle distribution functions: (1) the Tátrallyay method to observationally determine the growth rate or damping rate of specific mode such as the mirror mode along the streamline (*Tátrallyay and Erdős, 2002; Tátrallyay et al., 2008*), and (2) the Guicking method to observationally track the spectral evolution of turbulent fluctuations along the streamline (*Guicking et al., 2010, 2012*).

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At the moment a comparison with plasma data is technically not feasible for our model. Due to the limited particle measurements on board MESSENGER, it is not possible to obtain the plasma parameters properly in the solar wind and magnetosheath, that is, by covering the full velocity distributions and to compare with the model velocities. Above all, the plasma instrument is located behind the heat shield and has just a limited field-of-view. Due to this fact, the majority (thermal core part) of solar wind particles cannot be detected. Comparison with the numerical simulations would be another possibility to test for the model, but a quantitative comparison remains a challenge for the reason that there are large discrepancies in the density and flow velocity among various simulation models on the dayside from the sub-solar point to the northern terminator (Aizawa et al., 2011).

An approximation that the magnetic field is more aligned with the solar wind flow direction is more justified at Mercury than at the Earth because of the Parker spiral nature. One of the possible consequences of our assumption is that the magnetic field magnitude would change or evolve in the same sense as that of the plasma (or particle number flux) in the magnetosheath. The correlation between the magnetic field and that of the particle flux in the magnetosheath would ideally be tested against the plasma and magnetic field data on the arrival of BepiColombo at Mercury. The change in the number density can be interpreted as the change in the cross-sectional area of a fluxtube across which the plasma streams. The change in the flow velocity can then be compared with that from the adiabatic expansion and that from the measurement.

Following remarks are drawn as scientific message: First, Figure 1 visually demonstrates that different models predict different shapes of the tail and magnetosheath, which is an overlooked issue in the Mercury magnetosphere community. Second, Figure 2 shows that the flowlines near the sub-solar region (Sun-to-planet line if neglecting the planetary orbital motion) expand abruptly so that the adiabatic expansion may break down. In particular, the adiabatic expansion plays an important role in predicting the flow in the magnetosheath. Logical continuation of our model construction would be to evaluate also the density and velocity profile along the flowline and to test under which conditions the adiabatic expansion breaks down.

Although the proposed model has a good performance overall for a wide range of upstream conditions, the accuracy strongly depends on the used bow shock and magnetopause model. Here we utilize the bow shock and magnetopause model from *Slavin et al.* (2009) and *Korth et al.* (2015), which were adopted from MESSENGER boundary crossing observations.

The presented model is cylindrically symmetric around the X_{MSM} -axis. In reality, however, non-radial IMF conditions will lead to a spatially asymmetric magnetosheath (*Nishino et al.*, 2008; *Dimmock and Nykyri*, 2013; *Dimmock et al.*, 2016). On the quasi-perpendicular side, where the shock-normal angles θ_{Bn} are greater than 45° , the magnetosheath is known to be thicker with larger plasma flow velocities than on the quasi-parallel side, where $\theta_{\text{Bn}} < 45^\circ$. Such asymmetries cannot be reproduced by the simple model presented here, but should be addressed in future work.

Furthermore, the method used to determine the flow velocity magnitude can possibly be improved. Here we assumed a constant plasma density and velocity along the flowline which has the tendency to underestimate the plasma velocity in regions with lower densities e.g. close to the magnetopause. *Génot et al.* (2011) proposed a simple ad-hoc model of a plasma density profile which has been implemented by *Soucek and Escoubet* (2012). While this ad-hoc density model showed good correspondence with in-situ spacecraft plasma observation at Earth, the solar wind and magnetospheric conditions at other planets can be very different (like e.g. at Mercury) and thus might give a worse prediction (*Soucek and Escoubet*, 2012). Our model inherits the properties from the Soucek-Escoubet model by scaling the Kobel-Flückinger model of the near-Earth environment: (1) time

stationary flow, and (2) axially symmetric around the axis of (apparent) solar wind penetrating the planet. Assumption of time stationary flow may break down, when the change in the solar wind state is not negligible. Assumption of the axi-symmetric magnetosheath may also break down, when the magnetopause location is not symmetric between the northern and the southern hemisphere (in particular, in the tail region).

At this stage we decided not to include an ad-hoc density profile, also because it can hardly be tested due to the limited plasma observations around Mercury. The assumption of constant density implies a constant velocity along a given flow line. The velocity profile may vary considerably from that estimated in the earlier models such as the Spreiter model (*Spreiter et al.*, 1966), the Genot model (*Génot et al.*, 2011), and the Soucek-Escoubet model *Soucek and Escoubet* (2012). As mentioned above, the constant density will likely underestimate the propagation timing in the magnetosheath. In a future work such a density profile should be evaluated and included.

Code availability. An IDL program to evaluate plasma flow velocity vector in Mercury's magnetosheath from solar wind parameters of the Tao solar wind propagation model can be retrieved from OSF: https://osf.io/9jqqn/?view_only=2624aca3774c4ba8885dcb21a13e1b08 (*Schmid*, 2020).

Data availability. The plasma data of the heliospheric Tao model are open access and can be retrieved on the AMDA website (<http://amda.cdpp.eu/>, Centre de Données de la Physique des Plasmas (CDPP), 2018) via the WorkSpace Explorer: DataBase/Solar Wind Propagation Models/Tao Model/SW Input OMNI (*Tao et al.*, 2005). The orbital motion data of Mercury are provided by the Navigation and Ancillary Information Facility (NAIF) and can be retrieved on the NAIF website under <https://wgc.jpl.nasa.gov:8443/webgeocalc> (*Acton*, 1996).

Author contributions. DS initiated this study, collected the data and implemented the method. FP, YN, MV and WB helped evaluating the manuscript.

Competing interests. The authors declare that they have no conflict of interest.

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