

Wavevector spectral signature of decay instability in space plasmas

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Abstract. Identification of a large-amplitude Alfvén wave decaying into a pair of ion-acoustic and daughter Alfvén waves is one of the major goals in the observational studies of space plasma nonlinearity. In this study, the decay instability is analytically evaluated in the 2-D wavenumber domain spanning the parallel and perpendicular directions to the mean magnetic field. The growth-rate determination of the density perturbations is based on the Hall-MHD wave-wave coupling theory for circularly-polarized Alfvén waves. The diagrams of the growth rates versus the wavenumber and propagation angle derived in analytical studies are replaced by 2-D wavenumber distributions and compared with the corresponding wavevector spectrum of density and magnetic field fluctuations. The actual study reveals a perpendicular-shape spectral pattern consistent with the result of a previous study based on 3-D hybrid numerical simulations. The wavevector signature of the decay instability observed in the two-dimensional wavenumber domain ceases at values of plasma beta larger than $\beta=0.1$. Growth-rate maps serve as a useful tool for predictions of the wavevector spectrum of density or magnetic field fluctuations in various scenarios for the wave-wave coupling processes developing at different stages in space plasma turbulence.

1 Introduction

Parametric instabilities driven by large-amplitude Alfvén waves have extensively been investigated by analytical studies or numerical simulations in one- or multi-dimensional approaches. A systematic analytical analysis of the multidimensional features of the parametric instabilities have been initiated by Viñas and Goldstein (1991a, b) by applying the Hall-magnetohydrodynamic (hereafter, Hall-MHD) theory to a large-amplitude field-aligned Alfvén wave with left-hand and right-hand circular polarization. Results of the two-dimensional predictions of Viñas and Goldstein (1991a, b) have successfully been confirmed by later numerical simulations. Obliquely propagating daughter waves excited by the decay of a field-aligned Alfvén wave have been observed in 2-D MHD numerical simulations by Ghosh et al. (1993) for a low-beta regime. Other studies on the nonlinear interaction of obliquely-propagating Alfvén waves confirm that the growth rate of the decay instability in direction oblique to the mean magnetic field is typically smaller than the field-aligned decay, see e.g., Mjølhus and Hada (1990), Laveder et al. (2002), Nariyuki et al. (2008). By using two-dimensional hybrid simulations, Matteini et al. (2010) discovered that a broad spectrum of Alfvén and density fluctuations is developing perpendicular to the direction of the mean magnetic field at the decay of a linear

polarized Alfvén pump wave with oblique direction of propagation in low beta plasmas. Gao et al. (2013) reported by means of
25 2-D hybrid simulations that a linear polarized Alfvén pump wave with parallel propagation can also generate a perpendicular
spectrum of daughter waves. Comișel et al. (2019) observed recently a perpendicular spectrum of daughter waves by using
field-aligned Alfvén pump waves with circular left-hand polarization and 3-D hybrid simulations. This result was not predicted
by previous 2-D numerical simulations. The three-dimensional setup has been also used by Comișel et al. (2020) for analyzing
the evolution of large-amplitude Alfvén waves into the azimuthal (or transversal) plane with respect to the mean magnetic field
30 in low-beta plasmas.

The purpose of this study is to recall the former Hall-MHD analytic approach developed by Viñas and Goldstein (1991a).
The analytical predictions show that at very low beta values, the oblique decay of a circularly-polarized Alfvén wave becomes
competitive with the field-aligned decay. We are looking whether the solutions of the dispersion equation provided by Viñas
and Goldstein (1991a) model can or cannot drive a perpendicular spectrum of daughter waves in accordance with the prediction
35 of the 3-D hybrid simulation. In the two-dimensional analytical analysis, the dispersion equation is typically solved by setting
a priori the propagation direction of the daughter wave and the complex solution for the frequency is investigated in the
wavenumber domain. Here we solve and display the imaginary part of frequencies (namely, growth rates) of the dispersion
equation into a wavevector-spectrum like diagram along the parallel and perpendicular directions to the mean magnetic field.
On basis on this study, the developed perpendicular spectrum of daughter waves can be considered as a signature for the decay
40 of a left-handed circularly-polarized Alfvén pump wave in low beta plasmas. This pattern describing the oblique-decay process
is vanishing for larger values of plasma beta parameter.

In the two-dimensional analysis of Viñas and Goldstein (1991a), the authors concluded the decrease of the oblique-decay
growth rates into narrow band-profiles (in the wavenumber domain) when moderate oblique propagation angles of the daughter
waves are considered. In the actual approach, we explore in more details the growth rates at beta values much smaller than
45 the typical value ($\beta=0.5$) used in the previous study. The obtained solutions of the dispersion equations represented in a
parallel- and perpendicular- wavenumber diagram reveal new spectral features of the decay instability in low beta plasmas
which have never been pointed out in former analytical investigations. Furthermore, this result strengthens the idea of multi-
channel coupling of decay instability as a proof-of-concept proposed by Comișel et al. (2019) in a former study based on
numerical 3-D hybrid simulations. By following the Hall MHD formalism of Viñas and Goldstein (1991a), we constructed the
50 $k_{\parallel} - k_{\perp}$ spectrum, and the results are in good agreement between the numerical simulation and the analytic treatment.

2 Method and results

We use the analytical analysis developed by Viñas and Goldstein (1991a, b) based on the two-fluid plasma model together with
the generalized Ohm's law. The dispersive effects are driven by the ion inertia and the Hall term. Monochromatic parallel-
propagating Alfvén waves are exact solutions of the nonlinear MHD equations describing a plasma system. Starting from this
55 property, the set of equations for the evolution of density, flow velocity, and magnetic field is linearized by using a perturbation
expansion in order to define a linear-mode wave (or eigenmode of the system) around the equilibrium of each of the above

mentioned quantities. Each linear mode is specified by its frequency and wavevector. The wave-wave coupling of the large-amplitude Alfvén pump wave with a density perturbation of wavevector \mathbf{k} and frequency ω is conducting to side-band daughter waves expressed by the relations, $\mathbf{k}^\pm = \mathbf{k} \pm \mathbf{k}_0$, $\omega^\pm = \omega \pm \omega_0$, where \mathbf{k}^\pm and ω^\pm describe the wavevectors and frequencies of the daughter waves, respectively, $\mathbf{k}_0 = k_0 \mathbf{e}_\parallel$ with k_0 - wavenumber of the Alfvén pump wave, \mathbf{e}_\parallel is the unity vector parallel to the mean magnetic field, and ω_0 - frequency of the Alfvén pump wave. The daughter waves are allowed to propagate parallel and obliquely to the magnetic field. The general dispersion equation is derived in terms of 6x6 matrices and depends on six independent parameters: frequency, wavenumber and angle of propagation of the linear mode, amplitude and wavenumber of the pump wave, and plasma β parameter. The frequency and growth rate are normalized according to Viñas and Goldstein (1991a) as $\omega_r = Re(\omega)/k_0 V_A$, $\gamma = Im(\omega)/k_0 V_A$, where V_A is Alfvén speed. The plasma beta is defined as $\beta = V_s^2/V_A^2$ with V_s - the sound speed.

The dispersion equation is implemented and solved by using the Mathematica software. We first investigate the solutions (ω_r, γ) for the decay of a right-handed polarized Alfvén wave with same parameters used by Viñas and Goldstein (1991b). Figure 1 (left panel) reports the growth rates (solid line) and frequencies (gray solid line) obtained for plasma $\beta=0.5$. The amplitude of the Alfvén pump wave is 0.2 (normalized to the background magnetic field) and its wavenumber (normalized in terms of ion inertial length) $k_0 V_A/\Omega_p$ is 0.3, where Ω_p is the ion-gyrofrequency (for protons). The maximum growth rate for parallel propagation is obtained at $k/k_0 \approx 1.25$. The peaks of the growth rates determined at oblique-propagation angles of 10 deg, 20 deg, and 30 deg are decreasing and slightly moving to lower wavenumbers. Their corresponding frequencies are also reducing at larger propagation angles consistent with Viñas and Goldstein (1991b) result. In the same panel we show the solutions of the dispersion equation obtained at a lower plasma β value of 0.02. For a better visualization of both frequencies and growth-rate profiles, the values of the wavenumbers along horizontal axis are represented in a logarithmic scale. At small plasma-beta values, the maximum growth rate determined for parallel propagation is significantly larger and is located at $k/k_0 \approx 1.9$ (see black solid line). At an angle of 30 deg, the growth rate is slightly smaller (dotted line) while at a larger value (40 deg), the solutions are splitted into two peaks (thick diamond symbol). The dominant peak has a maximum close to that one derived at parallel propagation. The oblique decays have growth rates similar with that of the field-aligned decay (see also Fig. 3 in Viñas and Goldstein (1991b) at low β values). The result for a left-handed polarized Alfvén pump wave is given in the right panel of Fig. 1 calculated at the same low plasma beta value ($\beta=0.02$). The growth rates are slightly smaller for both parallel- and obliquely- propagating daughter waves than those analyzed by considering a right-handed polarized pump wave. At propagation angle of 30 deg, the splitting of the growth rate into two peaks is more pronounced and its maximum value is shifted to larger wavenumbers. In contrast with the left panel of Fig 1, at larger propagation angles (30, 40 deg), the prominent peak of the growth rate (thick diamond) is located in the right-hand side of the plot at wavenumbers $k/k_0 > 2$.

The growth rates derived from the dispersion equation shown in Fig. 1 can be visualized in a different way by constructing a wavevector diagram or growth-rate map analogue to the representation of the 2-D wavenumber spectrum of density or magnetic field fluctuations. The mapping of the growth rates in such coordinates is helpful in our study for a two-folded purpose discussed bellow for: (i) establishing or finding of a specific pattern for the parametric decay in the wavevector domain

and (ii) direct comparison of the analytical predictions with spectra of fluctuations obtained from numerical simulations (or presumably in-situ measurements).

The top panels of Fig. 2 are the arrangement of the plots shown in Fig. 1 into the parallel and perpendicular wavenumber domain for the right-handed and left-handed Alfvén pump waves. The growth rates in the new coordinates are obtained by solving the dispersion relation for k/k_0 wavenumbers spanning the domain (1,3) and (0,3) along the parallel and perpendicular direction with respect to the main magnetic field. Because this procedure is a demanding numerical task, the solutions of dispersion equations are searched in a limited wavenumber range where decay instability is expected (for instance, the domain below $k_{\parallel}/k_0 = 1$ where modulational instability could be operational is omitted). The solution is determined for a given pair of values $(k_{\parallel}, k_{\perp})$ which is then advanced by a discrete Δk step for each parallel or perpendicular direction. The resulted solutions are smoothed and represented in the wavevector domain. One may observe an "arc"-shape branch of solutions and a perpendicular one for the right-handed polarized Alfvén pump wave. For left-handed polarized waves, the perpendicular branch clearly dominates the "arc"-shape branch in accordance with the profiles drawn in Fig. 1. The bottom panels of Fig. 2 present the map of growth rates determined at larger beta values for left-handed polarized Alfvén pump waves. While the parallel wavenumber of the maximum growth rate is shifting to lower values, the perpendicular branch becomes weaker and at larger beta values ($\beta > 0.1$) the oblique-decay becomes insignificant with respect to the lowest-beta analyzed case. From this analysis we conclude that a perpendicular spectral pattern of the decay products can be associated with the decay process of a circularly polarized Alfvén wave in low-beta plasma.

In Fig. 3 we compare the result of the actual study for the left-handed polarization and beta value of 0.02 with the 2-D wavenumber spectrum of density and magnetic field fluctuations from a former 3-D hybrid simulation (Comişel et al., 2019). First, the growth-rate map given in Fig. 2 is extended towards both positive and negative perpendicular wavenumbers. Second, the growth rates for the lower side-band daughter waves ($\omega_- = \omega - \omega_0$) describing Alfvén waves with backward propagation are added at (negative) wavenumbers $k_{\parallel}^- = k_{\parallel} - k_0$ on the basis that $Im(\omega_-) \equiv Im(\omega)$ according to the wave-wave coupling scheme. The magnetic field and density fluctuations given in right panel of Fig. 3 are obtained from a former 3-D hybrid simulation based on AIKEF code (Müller et al., 2011) and a similar scenario with the current study. Magnetic field fluctuations are represented at negative wavenumbers corresponding to the backward propagating Alfvén daughter waves while the compressional forward propagating waves (acoustic-like) are shown as density fluctuations along the positive wavenumbers. Furthermore, the 2D wavenumber spectra are filtered in frequency domain such that only the frequencies expected for the Alfvén daughter waves at $\omega = \omega_s - \omega_0$ and for density mode at $\omega = \omega_s$ (here ω_s is the frequency of the ion acoustic wave) are shown. The spectral analyses report the Alfvén daughter modes at $k_{\parallel} V_A / \Omega_p \sim -0.2$ and the sound daughter waves at $k_{\parallel} V_A / \Omega_p \sim 0.4$. There is a good qualitative match between the two panels. As we already mentioned, the analytical model does not consider the wave damping or the harmonics of the excited daughter modes. The actual study and former hybrid simulation suggest that the field-aligned decay is accompanied by an oblique-decay process developing a perpendicular spectrum of density and magnetic field fluctuations.

3 Discussion

125 Former studies based on 2-D hybrid simulations, e.g., Matteini et al. (2010), reported a transversal spectrum of daughter waves
observed at the decay of a large amplitude Alfvén wave with linear polarization in low beta plasmas. Matteini et al. (2010)
discussed the observed result in terms of the finite oblique angle of propagation of the imposed Alfvén pump wave with respect
to the mean magnetic field. Gao et al. (2013) confirmed the former 2-D numerical study and even noticed a similar perpendicular
130 studies of Viñas and Goldstein (1991b) suggest, on basis of the beta dependence of the oblique-decay growth rates, that the
decay process of a field-aligned circullary-polarized Alfvén wave might become important at finite angles of propagation for
the daughter waves in low beta plasmas. The mechanism controlling the oblique decay instabilities has been discussed in
relation with the coupling between the electrostatic (dominant at parallel propagation) and electromagnetic (dominant at high
oblique angles) terms in the Hall MHD non-linear equations. By representing the growth rates provided by Viñas and Goldstein
135 (1991a) formalism in the wave-vector domain, the perpendicular spectrum of daughter waves can be straightfully noticed in
Fig. 2, while this feature is not obvious in the usual representation in Fig. 1. The perpendicular decay of daughter waves have
been therefore predicted by the Hall MHD theory well before the first observations provided by 2D hybrid simulations in
low beta plasmas. On basis of this result, one may expect that growth-rate maps in the wave vector domain could reveal new
properties of parametric instabilities which can be further investigated or diagnosed by analytical treatments or by numerical
140 simulations.

There are still open questions started in early studies about the role played by parametric instabilities to the generation of
turbulent cascades, (Hoshino and Goldstein, 1989; Ghosh and Goldstein, 1994). The perpendicular spectrum of daughter waves
triggered by the nonlinear wave-wave coupling processes is superposed to the perpendicular spectrum of plasma turbulence
generated by the post-saturation processes of the decay instability. The plasma anisotropy index as a quantitative measure
145 of the directional (perpendicular) turbulence evolution describes the wavevector anisotropy of a two-dimensional spectrum of
magnetic fluctuations (Shebalin et al. , 1983). An increasing number of 2-D or even 3-D wavevector spectra are observationally
being reported from in-situ solar wind measurements, see e.g., Narita et al. (2010); Narita (2014a); Narita et al. (2014b). It
would be interesting to compare the beta dependence of the wavevector anisotropy of solar wind turbulence, see e.g., Comişel
et al. (2014), with the anisotropy determined from the growth-rate maps of decay instability in its dependence on plasma beta
150 parameter as they are displayed in Fig. 2.

To our knowledge, the current study is the first step to bring together the results of the Hall MHD analytic approach and
kinetic simulations, in emphasizing the generation of oblique daughter waves through their nonlinear evolution described by
the MHD model. One may also notice that the MHD description can be helpful to clarify observed properties of the parametric
instabilities which could originate in the kinetic approach by non-physical fluctuations due to the particle discreteness expected
155 in hybrid or particle-in-cell simulations.

As limitations of the Viñas and Goldstein (1991a) method used in this analysis, the linear dispersion was restricted to exci-
tation of only fundamental side-band daughter waves (i.e., no harmonics are allowed). The electron-inertia effect is neglected;

one may expect that time scales or length of interest are larger than the electron gyroperiod or electron inertial length, respectively. The validity of the MHD approach with included Hall term is thus limited up to higher frequencies close to the ion gyro-frequency. The Landau and cyclotron damping effects have also been neglected in the MHD approach.

4 Summary

In conclusion, the analytic method developed by Viñas and Goldstein (1991a) prescribes that in low beta plasmas, circularly polarized Alfvén waves decay into parallel and obliquely-propagating daughter waves. The growth-rate values of the decay process plotted in the two-dimensional domain of the wavevector parallel and perpendicular to the mean magnetic field evince a displacement of the solutions into two branches: a perpendicular one predominant for both left- and right- hand polarization and an "arc"-shape one which is stronger for the right-hand polarization. The oblique decay significantly decreases at beta values larger than $\beta > 0.1$. The theoretical prediction for the left-handed polarized Alfvén pump wave derived in the 2-D wavenumber domain is consistent with the 2-D spectrum of density and magnetic field fluctuations resulted from 3-D hybrid simulations.

Growth-rate maps as those discussed above can be conveniently obtained for various values of the input parameters describing the dispersion equation. A catalogue of maps realized by a systematic analyzing for plasma beta, amplitude of pump wave, polarization or amount of dispersion can provide valuable information for further investigations of parametric instabilities by using hybrid or full-particle numerical simulations in two- or three- dimensional approaches. The growth-rate maps derived by analytical models and subsequently confirmed by numerical simulations can be helpful in future studies as predictions for the spectrum of density or magnetic field fluctuations expected from in-situ measurements. Furthermore, the particular signature of the oblique decay can serve as an evidence of wave-wave coupling processes acting at different evolution stages in space plasma turbulence.

Code and data availability. Software code and data sets are available by writing to the following email addresses: h.comisel@tu-braunschweig.de or comisel@spacescience.ro.

Author contributions. HC worked on theory implementation and manuscript writing. YN worked on representation of wave nonlinearities and application to space plasmas. UM worked on discussion and supervised of the study. All authors read and approved the final manuscript.

Competing interests. The authors declare that they have no conflict of interest.

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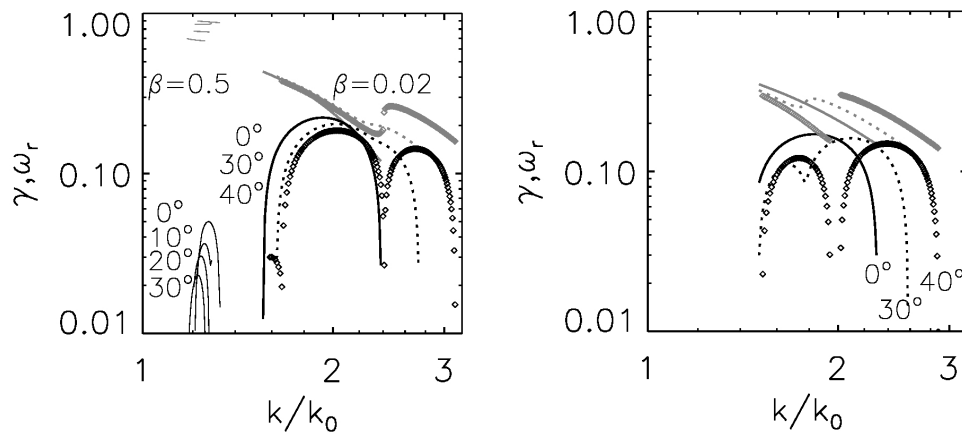


Figure 1. Solutions of the dispersion equation (growth rates in black and frequencies in gray) versus normalized wavenumber for right-handed (panel left) and left-handed (panel right) polarized Alfvén pump waves at propagation angles 0 deg, 30 deg, and 40 deg and plasma $\beta=0.02$. Left panel also shows the result obtained for right-hand polarization and plasma $\beta=0.5$.

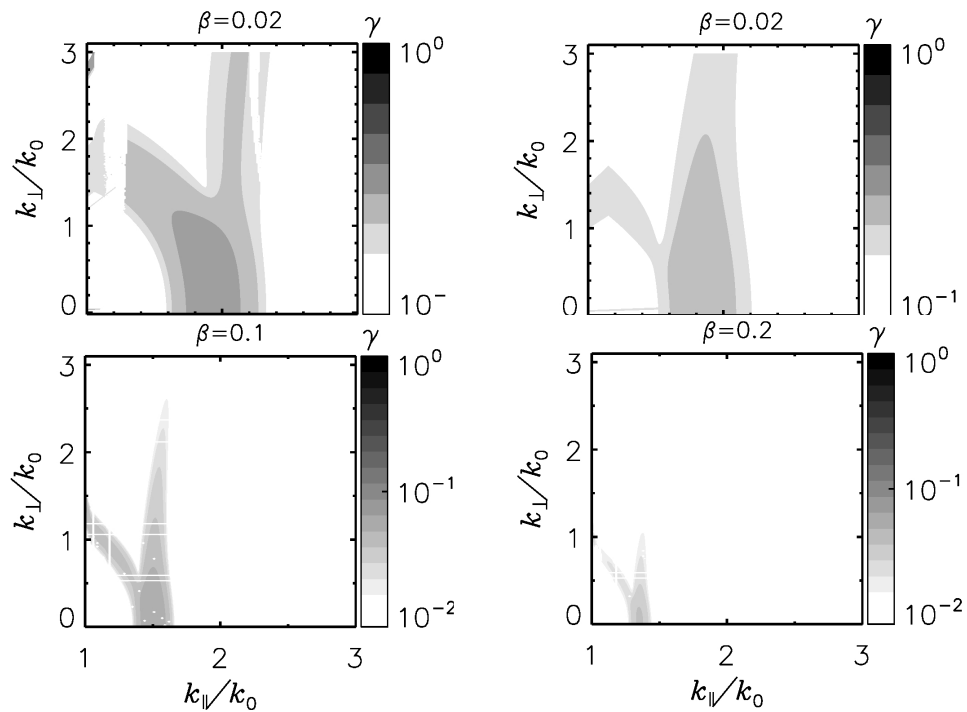


Figure 2. Top: Map of the growth rates in the $k_{\parallel} - k_{\perp}$ wavenumber domain for right- (panel left) and left- (panel right) handed polarization of the Alfvén pump wave corresponding to the analysis shown in Fig. 1 at plasma $\beta=0.02$. Bottom: Diagrams for left-handed polarized Alfvén pump wave at higher beta values.

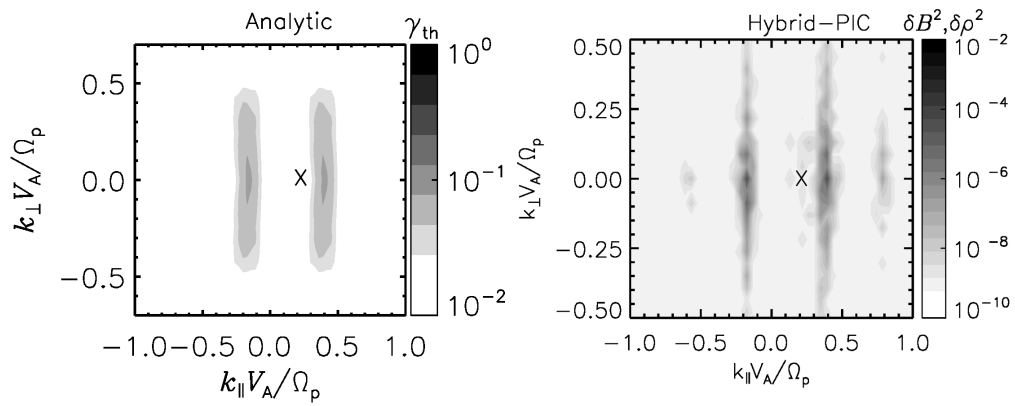


Figure 3. Comparison between the extended map of the growth rates in the $k_{||} - k_{\perp}$ wavenumber domain (left panel) and 2-D wavenumber spectrum of density and magnetic field field fluctuations (right panel) from Comişel et al. (2019). The location of Alfvén pump waves is marked by a cross symbol.