

1 The increase of curvature radius of geomagnetic field lines preceding a classical
2 dipolarization

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9 Abstract

10 Based on assumptions that substorm field line dipolarization at geosynchronous altitudes is
11 associated with the arrival of high velocity magnetotail flow bursts referred to as Bursty Bulk
12 Flows, we propose following sequence of field line dipolarization: (1) Slow magnetoacoustic
13 wave excited through Ballooning instability by enhanced inflows in pre-onset intervals
14 towards the equatorial plane; (2) In the equatorial plane, slow magnetoacoustic wave
15 stretching of the flux tube in dawn-dusk directions resulting in spreading plasmas in dawn-
16 dusk directions and reduction in the radial pressure gradient in the flux tube. As a
17 consequence of the foregoing processes, the flux tube assumes a new equilibrium geometry
18 in which curvature radius of new field lines increased in the meridian plane suggesting an
19 onset of field line dipolarization. The dipolarization processes associated with changing the
20 curvature radius preceded classical dipolarization caused by reduction of cross-tail currents
21 and pileup of the magnetic fields.

22 Increasing curvature radius induced convection surge in the equatorial plane as well as
23 inductive westward electric fields of the order of mV/m. Electric fields transmitted to the
24 ionosphere produce electromotive force in the E layer for generating field-aligned current
25 system of Bostrom type. This is also equivalent to the creation of an incomplete Cowling
26 channel in the ionospheric E layer by the convection surge.
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29 1. Introduction

30 Substorms are spatially localized and temporarily variable processes in the nighttime
31 magnetosphere. It is often difficult to determine onset timing of substorm processes such as
32 magnetotail flow burst, field line dipolarization, and particle injections. To resolve the timing
33 uncertainties, auroras in global satellite images [Nakamura et al., 2001; Miyashita et al.,
34 2009], intensifications of auroral kilometric radiation [Fairfield et al., 1999; Morioka et al.,
35 2010], and dispersionless particle injection in geosynchronous orbit [Birn et al., 1997] were
36 used. Ground Pi2 pulsations are another useful tool for determination of the substorm timing

37 [Sakurai and Saito, 1976; Nagai et al., 1998; Baumjohann et al., 1999]. Particularly, Pi2s in
38 equatorial region exhibited small phase difference ($m < 1$, m denotes azimuthal wave number)
39 across widely separated stations in the equatorial countries [Kitamura et al., 1988],
40 minimizing the timing uncertainties arising from delays in longitudinal propagations. This
41 enabled us accurate onset timing study of substorms using magnetometer data from two
42 remote locations, geosynchronous altitudes and ground stations of the equatorial countries
43 [Saka et al., 2010].

44 In this study, we focus on the dipolarization events at geosynchronous orbit from growth to
45 expansion phase. Triggering mechanisms of the field line dipolarization in the vicinity of
46 geosynchronous orbit are our major concern. In this paper, onset timing study of substorms
47 using magnetometer data from equatorial countries are summarized in Sect. 2. In Sect. 3,
48 we present a pre-onset scenario leading to the dipolarization onset. In Sect. 4, excitation of
49 slow magnetoacoustic wave is discussed for triggering field line depolarization. We will focus
50 on the field line dipolarization in the vicinity of geosynchronous orbit in Sect. 5. A coupling of
51 magnetosphere and ionosphere associated with this dipolarization scenario will be presented
52 in Sect. 6. In Sect. 7, we present a triggering mechanism of low latitude Pi2s that enabled
53 the Pi2-based epoch analyses. Summary and discussion of this scenario is given in Sect. 8.

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56 2. Summary of onset timing study using ground Pi2s at the equator

57 In this section, we summarize field line dipolarization occurring at the geosynchronous orbit
58 based on the statistical results obtained by Saka et al. [2010]. The authors used
59 magnetometer data from geosynchronous satellites (Goes5 and Goes6) and those at ground
60 equatorial stations (Huancayo, Peru, $1.4^\circ N$ in geomagnetic latitudes) in the conjugate
61 meridian. Goes5 was located at higher latitudes, $10.3^\circ N$ in dipole coordinates, and Goes6
62 was closer to the equator; $7.9^\circ N$ in dipole coordinates. This difference was caused by the
63 separated meridians of the satellites (2.2 hours of local time). The dipole coordinate used are
64 equivalent to the HDV coordinates; H is positive northward along the dipole axis, V is radial
65 outward, and D denotes dipole east. The field line dipolarization at the geosynchronous orbit
66 can be characterized either by a step-like or impulsive increase of inclination angle of the
67 geomagnetic field lines. The inclination angle is measured positive northward from the dipole
68 equator. The step-like dipolarization was observed by Goes5 located at higher latitudes, while
69 the dipolarization pulse was observed by Goes6 at latitudes closer to the equatorial plane.

70 The onset of field line dipolarization preceded the initial peak of the ground Pi2 pulse by two
71 minutes, suggesting that the onset was initiated in association with the first increase of the
72 Pi2 amplitudes. Following the dipolarization onset, field line magnitude decreased at the

73 geosynchronous orbit, and field lines deflected westward in the dawn sector and eastward in
 74 the dusk sector (see Figure 1 for dawn-dusk deflection, reproduced from [Saka et al., 2010]).
 75 This is caused by the dawn-dusk expansion of the plasma flows occurring tailward of the
 76 geosynchronous orbit. These longitudinal expansions lasted for about 10 min and decreased
 77 the field magnitudes therein. Expansion in the dusk sector, however, continued over this
 78 characteristic 10-min-interval. Asymmetries of the dawn-dusk expansion may be caused by
 79 diamagnetic drifts in the plasma sheet [Liu et al., 2013]. It is suggested that classical
 80 dipolarization, caused by the reduction of cross-tail currents in the midnight magnetosphere,
 81 happened after the nightside magnetosphere experienced this characteristic 10-min-interval.
 82 For this reason, the first 10 min intervals are referred to as transitional state of substorm
 83 expansion [Saka et al., 2010].

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86 3. Pre-onset intervals leading to field line dipolarization

87 In the pre-onset intervals, decrease of the field line inclination started two hours prior to the
 88 dipolarization onset. It attained minimum angles (33.6° for Goes5 and 49.4° for Goes6 in
 89 dipole coordinates) right before the dipolarization onset [Saka, 2010; 2019].

90 One of the properties of plasmas in pre-onset intervals are continuing inflows of lobe plasmas
 91 towards the equatorial plane [Birn and Hesse, 1996], Poynting flux enhancement [Machida
 92 et al., 2009], and Ey (westward electric fields) penetration toward the equatorial plane
 93 [Machida et al, 2014]. Corresponding plasma properties at geosynchronous altitudes may be
 94 predominant perpendicular temperature anisotropies of thermal plasmas (30eV - 40keV)
 95 obtained from three-dimensional temperature matrix and their gradual decrease towards the
 96 onset [Birn et al., 1997]. At the onset, however, increase of parallel anisotropy stopped and
 97 perpendicular anisotropy increased again. Such changes of temperature anisotropy at onset
 98 were observed in roll-angle spectrogram of energy flux of electrons in 15eV-40keV [Saka and
 99 Hayashi, 2017]. This transition of the temperature anisotropies may be accounted for by the
 100 following scenario.

101 A continuing tailward stretch of the field lines in the pre-onset intervals as depicted in Figure

102 2 may increase equatorward flux by the counterclockwise rotation of the inflow vectors (F_{\perp})
 103 in the north of the equatorial plane (clockwise rotation in the south) and produce a parallel
 104 component as well by the relation,

$$105 \quad \delta F_{\parallel} = F_{\perp} (\omega \cdot \delta t) \quad (1)$$

106 Here, δF_{\parallel} denotes increase of parallel flux per time, δt , ω is angular velocity of rotation
 107 of F_{\perp} vectors associated with the thinning of the flux tubes caused by stretching. In pre-
 108 onset intervals lasting 90 min at geosynchronous altitudes, field line stretching decreased the
 109 field line inclination by 7° from 40.6° to 33.6° [Saka, 2019]. This gives angular velocity
 110 of rotation of field line inclination in equation (1) as $1.4 \times 10^{-3} \text{ rad / min}$. Total parallel flux
 111 gained in T min may be given by the integral of equation (1) with time from 0 to T. Substituting
 112 T=60 min and $1.4 \times 10^{-3} \text{ rad / min}$ for angular velocity of field line inclination, this yields
 113 $F_{\parallel} = 8.2 \times 10^{-2} \cdot F_{\perp}$. Gain of F_{\parallel} is about 10% of the perpendicular flux (F_{\perp}). This is
 114 consistent with the parallel temperature anisotropies gained prior to the onset (20% gain) in
 115 geosynchronous orbit [Birn et al., 1997].
 116 Continuing parallel flux flows associated with the flux tube stretching in the pre-onset intervals
 117 may increase plasma pressures in the flux tube at its tailward end. This condition leads to
 118 further stretching of the flux tube (small curvature radius) [Ohtani and Tamao, 1993; Rubtsov
 119 et al., 2018] by the relation,

$$120 \quad \frac{\beta}{2} \kappa + \kappa_B + \frac{1}{R} = 0 \quad (2)$$

121 Here, β is plasma to magnetic pressure ratio, κ and κ_B denote reciprocal spatial scales
 122 of radial inhomogeneity of plasma pressure and magnetic fields in the equatorial plane,
 123 respectively. R is curvature radius of the field lines.

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126 4. Excitation of slow magnetoacoustic wave

127 The continuing parallel flows may excite magnetoacoustic wave. From a set of linearized
 128 MHD equations we have relation between parallel displacement along the field lines (ξ_z)
 129 and divergence of perpendicular displacements (ξ_{\perp}) in the following form (see Appendix),

$$130 \quad \xi_z = \frac{C_s^2}{\omega^2} F \cdot B_0^2 \frac{\partial}{\partial z} (\text{div} \xi_{\perp}) \quad (3)$$

131 Here, C_s , ω and B_0 are the sound velocity, angular frequency of waves and background
 132 field magnitudes, respectively. F is given by

133

$$F = \frac{C_A^2}{B_0^2} \frac{1}{C_s^2 - \left(\frac{\omega}{k}\right)^2} \quad (4)$$

134 F is positive for the slow magnetoacoustic wave and negative for the fast magnetoacoustic
 135 wave. C_A and k denote Alfvén velocity and wave vector, respectively. We use equation (3) for
 136 the classification of slow and fast magnetoacoustic waves. Slow magnetoacoustic wave
 137 yields perpendicular expansion of the flux tubes at the converging point of parallel flows on
 138 the equatorial plane. For fast wave, perpendicular shrinkage of flux tubes occurs at the
 139 converging point of parallel flows (equatorial plane).

140 The equation (3) will be applied to simulate possible effect of magnetoacoustic wave on pitch
 141 angle spectrogram. For this, we used drift Maxwell distributions for phase space density
 142 (PSD) assuming gyrotropy for particle trajectories. PSD was composed of three parts: one
 143 drifting parallel, another anti-parallel along the field lines, and the third part perpendicular to
 144 the field lines. Figure 3(A) shows pitch angle spectrogram of energy flux with no drift velocities
 145 either perpendicular or parallel to the background field lines. Energy flux is defined by

146 $(2E^2/m^2)f$, where E , m , f are energy, mass of particles, and phase space density,

147 respectively. Energy flux is given in $eV / (cm^2 s \cdot sr \cdot eV)$. Only parallel drift increased in from
 148 $0.3V_{th}$, $0.6V_{th}$, and to $1.0V_{th}$ as shown in B, C, and D. For E and F, perpendicular drift
 149 increased to $0.3V_{th}$ and $0.5V_{th}$ while parallel drift remained at $1.0V_{th}$. Energy fluxes initially in
 150 quasi trapped distribution (A) changed to more parallel and anti-parallel fluxes as parallel and
 151 anti-parallel drift increased (B, C, and D). Increasing perpendicular drifts increased
 152 perpendicular fluxes in the pitch angle distributions of E and F.

153 We clarified that magnetoacoustic wave produced coupling of parallel flux along the field
 154 lines and the perpendicular flux. However, we choose slow magnetoacoustic wave for the
 155 wave mode because the flux tubes expanded (did not shrink) in the transitional interval as
 156 discussed in Section 2. Slow magnetoacoustic wave may be triggered through Ballooning
 157 instability, when enough pressure gradient is accomplished in an earthward direction [Ohtani
 158 and Tamao, 1989; Rubtsov et al., 2018].

159 We can estimate the Ballooning instability threshold κ (reciprocal scale of radial
 160 inhomogeneity of plasma pressure) using calculation results given in [Rubtsov et al., 2018].

161 In a distance from $L=5$ to $10R_e$, instability threshold is given approximately as $\kappa = -1.0R_e^{-1}$
 162 (κ denotes reciprocal spatial scale of radial inhomogeneity of plasma pressure, and R_e is
 163 the Earth radius) for beta defined by the ratio of plasma pressure and magnetic pressure
 164 exceeding 0.1. This suggests that the Ballooning instability develops at the geosynchronous
 165 altitudes (curvature radius R is $2.2 R_e$) when spatial scale of the earthward pressure gradient

166 caused by the inflows becomes steeper than 1.0 Re. We show in the following section that
167 this theoretical consideration matched observations.

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170 5. Field line dipolarization in the vicinity of geosynchronous orbit

171 *5.1 Relaxation of radial inhomogeneity*

172 We can assume the westward electric fields in Dipolarization Front (DF) [Runov et al., 2011]
173 embedded in the leading edge of Bursty Bulk Flow (BBF) as external stimulus for triggering
174 Ballooning instability. In this case westward electric fields in the DF temporarily amplified the
175 parallel flux flowing towards the end point of the flux tube in the equatorial plane and further
176 steepen earthward pressure gradient. If it exceeds instability threshold determined by β
177 and initial curvature radius R , slow magnetoacoustic wave can be excited [Rubtsov et al.,
178 2018]. Once the slow magnetoacoustic wave was excited, perpendicular fluxes spread the
179 plasmas in dawn-dusk directions and smooth (or relax) the radial gradient of plasma
180 pressures in the equatorial plane (smaller κ). This may result in the transition of the flux
181 tube geometry to a new configuration, an increase of the curvature radius of the field lines
182 (larger R) (see equation (2)).

183 We revisit multiple Pi2 events observed by AMPTE CCE on 31 August 1986 [Saka et al.,
184 2002] and show an example of relaxation of radial inhomogeneity of plasma pressures
185 associated with field line dipolarization in Figure 4. The satellite passed the midnight sector
186 (20 – 23 MLT) from 3 Re to 7 Re at latitudes south of the equatorial plane (-8° MLat) when
187 multiple Pi2 event (with positive bay) were observed at low latitude station (KUJ) at L=1.2 in
188 the midnight sector (Figure 4A). Inclination angle of field lines along the satellite trajectory is
189 shown in Figure 4(B). Dipolarization occurred as marked by vertical arrows correlating to

190 multiple onset of Pi2s, 1 through 4 in Figure 4(A). Ion fluxes coming from dawn sector (\mathbf{J}_-)

191 and from dusk sector (\mathbf{J}_+) at satellite altitudes were measured by the instruments (two

192 energy channels, 63-85 keV and 125-210 keV) on board AMPTE CCE [Takahashi et al.,
193 1996]. A schematic of particle measurement is shown at the top of Figure 5. The flux

194 difference ($\mathbf{J}_- - \mathbf{J}_+ > 0$) increased in association with the onset of multiple Pi2 (15:05 UT)

195 and positive bay at KUJ (Figures 4C and 4D). Sudden increase was followed by the slow
196 decrease of flux in 63-85 keV channel and rapid decrease of flux in 125-210 keV channel.

197 The flux difference, $\mathbf{J}_- > \mathbf{J}_+$, may be caused either by earthward pressure gradient or

198 westward convection of plasmas. From the different patterns of the flux decrease with time
199 in two energy channels, we can suggest that the measured flux difference, $\mathbf{J}_- - \mathbf{J}_+$, can be
200 attributed to increase of the earthward pressure gradient and succeeding relaxation. Note
201 that guiding center of $\mathbf{J}_- / \mathbf{J}_+$ is earthward/tailward of the satellite position as depicted in
202 top of Figure 5. The different relaxation speed in two energy channels, slower for 63-85 keV
203 and faster for 125-210 keV, suggest that the earthward pressure gradient (assumed to be
204 proportional to the flux gradient) decreased with time during the multiple Pi2 event (Figure 5).
205 The flux difference (50 counts/sample) was 10% of the background flux both for 63-85 keV
206 (Larmor radius is 250 km for 150 nT) and for 125-210 keV (Larmor radius is 450 km), that is,
207 the flux level differed by 10% at two locations 1000 km apart in radial distance for 63-85 keV
208 and 1800 km for 125-210 keV. This gives e-folding scale of the earthward pressure gradient
209 being 0.98 Re and 1.77 Re for 63-85 keV and 125-210 keV, respectively. The 31 August
210 event shows that radial pressure gradient was relaxed in the inner magnetosphere in
211 association with the increase of the field line inclination (dipolarization). Although the field line
212 dipolarization showed a sharp onset in satellite magnetometer data, we note that it did not
213 occur in ion flux data. This may be true because the ion flux change at the onset may be
214 obscured by the contamination from the past onsets transported across the field lines from
215 the adjoining sector by the electric fields and gradient/curvature drifts. We conclude that the
216 relaxation of spatial inhomogeneity started when the spatial scale of the radial inhomogeneity
217 approached 1.0 Re, consistent with theoretical consideration of Ballooning instability by
218 Rubtsov et al (2018).

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220 *5.2 Flux tube transition to a new geometry*

221 Meanwhile, field lines in the further earthward locations may be compressed by the inward
222 movement of the outer field lines. This process associated with the dipolarization onset may
223 increase the parameter κ_B in equation (2) which may result in transition to a new geometry
224 of earthward field lines, a decrease of the curvature radius R . Transition of the field line
225 geometries for onset locations and ones in earthward locations are schematically illustrated
226 in Figure 6. These field line geometries in meridian plane matched the third harmonic and
227 fundamental harmonic deformations of outer and inner field lines, respectively. This is often
228 observed in the midnight magnetosphere in the initial pulse of Pi2s [Saka et al., 2012].
229 Transitions of the flux tube geometry in magnetosphere also correspond to the production of
230 negative bay in higher latitudes and positive bay in lower latitudes. If we can assume that
231 negative bay switched to positive bay at latitudes, 60 degrees in geomagnetic coordinates

232 for examples, this latitude can be mapped beyond the geosynchronous orbit ($L \sim 7 R_E$ or
233 further tailward) as field line dipolarization occurs along the stretched flux tubes.
234 Consequently, this scenario requires that the BBFs are not necessary to reach inner
235 magnetosphere to trigger the substorm onset at lower latitudes. In the inset, flux tube
236 deformations are illustrated in the equatorial cross section at onset locations (field lines 1
237 and 2). Divergence of perpendicular flows (solid arrows) produced dawn-dusk expansion of
238 flux tube (2) and the shrinkage of stretched flux tube (1) by relaxation of the radial
239 inhomogeneity. Flux tube deformation from 1 to 2 tended to preserve the total magnetic fluxes
240 in the equatorial cross section. From the local time distribution of the dawn-dusk expansion
241 of the flux tubes shown in Figure 1, most of the flux tube transition such as from 1 to 2 may
242 occur tailward of geosynchronous orbit. Some of the events, however, may happen
243 earthward of the geosynchronous orbit [i.e., Ohtani et al., 2018].

244 Increasing of the curvature radius, or earthward shrinkage of the flux tubes, produce a
245 reduction of the radial component of the field lines (V in dipole coordinates) by adding positive
246 V in the north of the equatorial plane and negative V in the south. If amplitudes of the V
247 component changed by 10 nT in one minute, the expected inductive electric fields (westward)
248 could be of the order of 1.0 mV/m when shrinkage was confined within 1 R_E from the
249 equatorial plane. The dawn-dusk expansion of the flux tubes may also produce inductive
250 electric fields (earthward and tailward in dawn and dusk sector, respectively) of the same
251 order of magnitudes. They are Alfvén waves, a wave mode in Ballooning instability coupled
252 with slow magnetoacoustic wave [Rubtsov et al., 2018]. The westward electric fields produce
253 earthward flow bursts referred to as convection surge. The inductive electric fields produced
254 by the dipolarization are the same order of magnitudes observed in DF [Runov et al., 2011].

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257 6. Coupling of magnetosphere and ionosphere in association with field line dipolarization

258 The inductive electric fields may be transmitted along the field lines as poloidally and
259 toroidally polarized Alfvén waves [Klimushkin et al., 2004]. These electric fields produce a
260 dynamic ionosphere in polar region that includes nonlinear evolution of ionospheric plasmas
261 (poleward expansion), as well as production of field-aligned currents and parallel potentials
262 by exciting ion acoustic wave in quasi-neutral condition [Saka, 2019]. It is not the aim of this
263 paper to describe in detail the dynamic processes in the ionosphere, but to show a local
264 production of currents in the ionosphere as well as field-aligned currents by the penetrated
265 electric fields. For this purpose, we revisit the 10 August 1994 substorm event studied by
266 Saka and Hayashi (2017). In this event, eastward expansion was observed of the field line
267 dipolarization region, started at 11:55 UT (00:27 MLT) from 260° E of geomagnetic longitudes

268 and expanded to 351° E in about 48 min. At the leading edge of the expansion, ground
 269 magnetometer data showed bipolar event (quick change of the D component from positive
 270 to negative in about 5 min), being confined in the expanding dipolarization front as a
 271 substructure. The substructure in the leading edge of the field line dipolarization will be
 272 examined as follows.

273 We can assume that magnetic signals on the ground are associated with the sum of the
 274 horizontal Hall currents in the ionosphere [Fukushima, 1971]. These currents can be
 275 calculated by the relation,

$$276 \quad (\text{rot } \mathbf{J})_z = -\frac{1}{\mu_0} \nabla^2 B_z \quad (5)$$

277 We used the ground vertical component (b) as a proxy of B_z in the ionosphere. The second
 278 derivative in right-hand side of equation (5) is approximated as,

$$279 \quad \nabla^2 B_z^i = \left(\frac{b^{i+1} - b^i}{L_{i+1} - L_i} - \frac{b^i - b^{i-1}}{L_i - L_{i-1}} \right) / (L_{i+1} - L_{i-1}) \quad (6)$$

280 Here, i denotes i -th station in the meridian chain. L_i is the geomagnetic latitude of the i -th
 281 station. We considered meridional change only. This is because the vertical component
 282 changed from negative to positive across the meridian, while in longitudes it changed simply
 283 decreasing or increasing in lower and higher latitudes after onset, respectively. Hence,
 284 longitudinal variations may contribute less to the Laplacian. The results reproduced from
 285 Saka and Hayashi (2017) are shown in Figure 7(A). The eastward propagation of
 286 dipolarization front crossed this meridian (300° E) at 12:13 UT corresponding to the interval
 287 labelled 1. Two points arose from this figure; (1) Loop of Hall current pair existed, CCW
 288 viewed from above the ionosphere in the lower latitudes and CW in the higher latitudes, (2)
 289 These current patterns expand poleward. Current patterns in the interval from 1 to 5 in Figure
 290 7(A) are illustrated in Figure 7(B) to facilitate the poleward expansion. It is clearly
 291 demonstrated that current pair forming CW in higher latitudes and CCW in lower latitudes
 292 expanded in time towards the pole. Bipolar change can be recorded in the D component data
 293 (not shown) when the ground station, FSIM in this case, passes from segment 1 to 2 in Figure
 294 7(B). As a result, dipolarization front expanded eastward progressively by producing the
 295 poleward expansion at each meridian. The front left behind the current pattern comprising
 296 upward field-aligned currents in lower latitudes and downward in higher latitudes, or Bostrom
 297 type current system. We propose that the ionosphere itself has inherent electromotive force
 298 to drive this Bostrom type current system. The reasons are as follows.

299 In the E region, drift trajectories may be written [Kelley, 1989] for electrons by,

300
$$\mathbf{U}_{e\perp} = \frac{1}{B}[\mathbf{E} \times \hat{\mathbf{B}}] \quad (7)$$

301 and for ions by,

302
$$\mathbf{U}_{i\perp} = b_i[\mathbf{E} + \kappa_i \mathbf{E} \times \hat{\mathbf{B}}]. \quad (8)$$

303 Here, b_i is mobility of ions defined as $\Omega_i/(B\nu_{in})$, κ_i is defined as Ω_i/ν_{in} . Symbols Ω_i
 304 and ν_{in} are ion gyrofrequency and ion-neutral collision frequency, respectively. $\hat{\mathbf{B}}$ denotes
 305 a unit vector of the magnetic fields B . We assumed that $\mathbf{E} \times \mathbf{B}$ drifts for electrons and
 306 ions were driven by westward electric fields transmitted from the convection surge. Because
 307 of very low mobility of ions in E layer ($\kappa_i = 0.1$), electric field drifts accumulate electrons (not
 308 ions) in lower latitudes and produce stronger secondary southward electric fields in the
 309 ionosphere. The southward electric fields produced southward motion of ions due to the first
 310 term of equation (8). They carry Pedersen currents (ion currents) for producing quasi-
 311 neutrality of ionosphere. $\mathbf{E}_w \times \mathbf{B}$ drifts caused by the transmitted westward electric fields
 312 (\mathbf{E}_w) may propel electrons against southward electric fields from higher latitudes to lower
 313 latitudes as electromotive force to maintain the potential drop for driving Pedersen currents.
 314 This means the ionospheric E layer contains both generator and load in it. In quasi-neutral
 315 condition, a small imbalance of particle densities of electrons and ions ($n_e - n_i \sim 10^2 m^{-3}$)
 316 may induce in lower latitudes negative potential region of the order of -100 kV with horizontal
 317 scale length of 100 km. To sustain this negative potential, upward field-aligned currents of
 318 the order of $1.0 \mu A / m^2$ for $\Sigma_p \sim 10^0 S$ must flow. Downward field-aligned currents from
 319 the positive potential regions in the higher latitudes may also be expected. It is supposed that
 320 upward field-aligned currents may be carried mostly by ions flowing outwards and downward
 321 currents are escaping electrons to the magnetosphere. Those ions and electrons escape
 322 from the ionosphere into the magnetosphere to assure quasi-neutral conditions of the
 323 ionosphere. The above scenario may be adapted to a creation of the incomplete Cowling
 324 channel [Baumjohann, 1983], where unbalanced primary northward Hall currents and
 325 secondary southward Pedersen currents driven by the polarization electric fields yielded
 326 field-aligned currents.

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329 7. Triggering mechanisms of low latitude Pi2s

330 From ground magnetometer observations in auroral zone, it is natural to assume that flux
331 tubes linked to negative bay (decreasing of the H component) and positive bay (increasing
332 of the H component) at higher and lower latitudes, respectively, oscillated coherently at Pi2
333 periods. Oscillating flux tubes associated with positive bay may produce local compression
334 of magnetic fields in the equator and trigger cavity mode in low latitudes [Takahashi et al.,
335 1995]. Oscillations, however, are short-lived and may not establish true cavity modes. They
336 excite cavity/waveguide modes in the plasmasphere [Allan et al., 1996; Li et al., 1998].

337 In the dip-equator, a singular latitude of the cavity/waveguide mode, only isotropic mode can
338 be excited [Allan et al., 1996]. This leads us to suppose that a very large propagation velocity
339 (or large wavelength exceeding whole circle of the Earth) of equatorial Pi2s in the nightside
340 sector [Kitamura et al., 1988] would be associated with the dawn-dusk asymmetries of non-
341 propagating compressions.

342 Pi2 periodicity may be determined primary by consecutive arrival of BBF substructures
343 referred to as dipolarization front bundle (DFB) [Liu et al., 2013, 2014]. Repeating arrival of
344 DFB produces periodic dipolarization or oscillation of negative bays. Positive bay oscillations
345 in the plasmasphere would follow the negative bay oscillations to excite cavity/waveguide
346 modes for low to equatorial Pi2s at the same periodicities. To estimate the onset time of the
347 field line dipolarization using the very low latitudes Pi2s, delays in transmission are from the
348 magnetosphere; longitudinal delays across the meridian may not be significant.

349 High latitude Pi2s may not be caused by cavity/waveguide modes but by oscillation of field-
350 aligned currents comprising Bostrom type current system (incomplete Cowling channel), R1
351 (region 1) type current system associated with convection surge [i.e., Birn and Hesse, 1996],
352 and R2 (region 2) type current system of expanding flux tubes in longitudes [i.e., Tanaka et
353 al., 2010]. In contrast to the very-low latitude Pi2s associated with the non-propagating
354 compression, the high-latitude Pi2s propagated on the ground typically at 20km/s eastward
355 and westward in the sector east and west of the substorm center, respectively [Samson and
356 Harrold, 1985]. Propagation across the meridian may cause further delays, 35 sec for
357 propagation of 1 hour of local time. We should exercise caution when using high latitude Pi2s
358 for timing study.

359 The above scenario assumes that the DFBs arrived periodically in the inner magnetosphere
360 at a frequency not very different than the cavity frequency of plasmasphere.

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362

363 8. Discussion and Summary

364 Definition of field line dipolarization is a configuration change from stretching to shrinkage of
365 geomagnetic field lines in the midnight meridian of magnetosphere. Two models have been
366 proposed to account for the configuration change; diversion of the cross-tail currents via
367 ionosphere, referred to as substorm current wedge (SCW), as first proposed in McPherron
368 et al. [1973] and extinction of the cross-tail currents by a local kinetic instability, current
369 disruption (CD) [Lui, 1996]. These models have been adopted for many decades to account
370 for the critical issues associated with substorm onset. We propose, based on Ballooning
371 instability scenario, that field line dipolarization is caused by the relaxation of radial
372 inhomogeneity of plasma pressures in association with the excitation of slow
373 magnetoacoustic wave. Dipolarization regions expand in longitudes and decrease field
374 magnitudes by expanding flux tubes therein. This condition continued for about 10 min and
375 classical dipolarization caused by the reduction of cross-tail currents or pileup of the magnetic
376 flux transported from the tail begins.

377 It is noted that BBFs with low entropy plasmas (plasma bubbles) often penetrated to the inner
378 magnetosphere [Dubyagin et al., 2011]. In numerical simulations, those bubbles localized in
379 local time produced global dipolarization in the inner magnetosphere [Merkin et al., 2019]
380 and generated ionospheric current system such as westward electrojet, Harang discontinuity,
381 and poleward expansion of aurora in substorm expansion phase [Yang et al., 2012]. These
382 classical features of substorm expansion occurred in this first 10 min intervals of Pi2 onset
383 referred to as transitional intervals in the midnight magnetosphere. The transitional intervals
384 may be the most active periods in the substorm phase.

385 The proposed scenario was deduced from the geosynchronous observation and cannot be
386 readily applied to the onset scenario beyond the geosynchronous orbit. Nevertheless, dawn-
387 dusk expansion of the flux tubes may be a fundamental property of field line dipolarization
388 not only at geosynchronous altitudes but also in tailward locations (8 - 12 Re) [Yao et al.,
389 2013; Liu et al., 2013]. It is suggested that the field line dipolarization at tailward locations is
390 subdivided by faster expanding (in longitudes) dipolarization front (DF) and slower expanding
391 dipolarization front bundle (DFB) led by DF [Liu et al., 2015]. Such substructures in field line
392 dipolarization are also observed at geosynchronous altitudes [Saka and Hayashi, 2017]. The
393 geosynchronous dipolarization expanded (in longitudes) at 1.9 km/s, while Pi2s emitted in
394 the dipolarization region propagated one order of magnitude faster. The fast longitudinal
395 velocities associated with Pi2s may be embedded within the slowly expanding region of
396 dipolarization, similarly to the relationship between DF and DFB. If this relationship can be
397 adapted also to the transitional state and succeeding field line pileup, the dipolarization
398 scenario at geosynchronous observations can be extended further tailward in upstream. Or,

399 the onset scenario in 10 Re can be applied in geosynchronous dipolarization. In that case,
400 dipolarization pulse at Goes6 latitudes ($7.9^\circ N$) may represents DFs. This assumption may
401 be supported because electron energy flux pitch angle distributions in tailward locations
402 beyond 10Re show parallel to perpendicular transitions, like ones in Figure 3, at the arrival
403 of DF [Deng et al., 2010].

404 We emphasize that two different types of the dipolarization exist in the substorms; one is
405 associated with change of curvature radius of field lines in the transitional state (faster
406 expansion in longitudes) and the other is subsequent pileup of the magnetic flux transported
407 from the tail (slower expansion). Field line pileup caused by the flow braking processes
408 [Shiokawa et al., 1997] may lead to tailward regression of the dipolarization region as
409 reported in Baumjohann et al. [1999].

410 In the transitional state lasting for about 10 min, the inductive electric fields pointing westward
411 were produced in the equatorial plane. They propagated along the field lines to the
412 ionosphere to produce meridional field-aligned currents of the Bostrom type (downward in
413 higher latitudes and upward in lower latitudes). The Bostrom type current system was indeed
414 observed on the ground at the front of dipolarization expanding towards east. The
415 magnetospheric dynamo produced by earthward electric fields in the equatorial plane
416 [Akasofu, 2003] and the E layer dynamo in the ionosphere worked together to activate the
417 Bostrom current system.

418

419

420 9. Code/Data availability

421 Satellite data from Goes5/6, AMPTE CCE and ground magnetometer data in Figures 1, 4
422 and 7 is available upon request to Osuke Saka (saka.o@nifty.com).

423

424 10. Competing interest

425 The author declares that there is no conflict of interest.

426

427

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430 Dynamics Campaign (GADC) [Oguti et al., 1988]. We are also grateful to anonymous
431 referees for their critical review.

432

433

434 Appendix

435 In order to derive equations (3) and (4), we first follow Kadomtsev (1979). Linearized MHD
 436 equations may be written as,

$$437 \quad \frac{\partial^2 \boldsymbol{\xi}}{\partial t^2} = C_s^2 \nabla \operatorname{div} \boldsymbol{\xi} + C_A^2 \nabla_{\perp} \operatorname{div} \boldsymbol{\xi}_{\perp} + C_A^2 \frac{\partial^2 \boldsymbol{\xi}_{\perp}}{\partial z^2}. \quad (\text{A1})$$

438 Here, C_s , C_A , $\boldsymbol{\xi}$ denote sound velocity, Alfvén velocity, plasma displacement, respectively.
 439 (\perp, z) denote perpendicular and parallel component with respect to the background field
 440 lines.

441 After a few manipulations of (A1), we have magnetoacoustic wave equations for finite β
 442 plasmas:

$$443 \quad \frac{\partial^2 \operatorname{div} \boldsymbol{\xi}_{\perp}}{\partial t^2} = C_A^2 \Delta \operatorname{div} \boldsymbol{\xi}_{\perp} + C_s^2 \Delta_{\perp} \operatorname{div} \boldsymbol{\xi} \quad (\text{A2})$$

444 and

$$445 \quad \frac{\partial^2 \xi_z}{\partial t^2} = C_s^2 \frac{\partial}{\partial z} (\operatorname{div} \boldsymbol{\xi}) \quad (\text{A3})$$

446 Equations (A2) and (A3) present compressive properties across and along the background
 447 field lines, respectively.

448 Assuming plane harmonic wave solutions, first order quantities of density and magnetic field
 449 compressions ($\delta n, \delta \mathbf{B}$) may be given by the following equation.

$$450 \quad \frac{\delta n}{n_0} = -\frac{C_A^2}{B_0^2} \frac{1}{C_s^2 - \left(\frac{\omega}{k}\right)^2} (\mathbf{B}_0 \cdot \delta \mathbf{B}) \quad (\text{A4})$$

451 Here, n_0 , B_0 denote background density and magnetic fields, respectively.

452 Substitution of (A4) into (A3) using $\operatorname{div} \boldsymbol{\xi} = -\delta n/n_0$ yields

$$453 \quad \frac{\partial^2 \xi_z}{\partial t^2} = C_s^2 F \frac{\partial}{\partial z} (\mathbf{B}_0 \cdot \delta \mathbf{B}). \quad (\text{A5})$$

$$454 \quad \text{Here, } F = \frac{C_A^2}{B_0^2} \frac{1}{C_s^2 - \left(\frac{\omega}{k}\right)^2}$$

455 Linearized Faraday's law in frozen-in condition, $\delta \mathbf{B} = \nabla \times (\boldsymbol{\xi}_{\perp} \times \mathbf{B}_0)$, may be reduced to

$$456 \quad \delta \mathbf{B} = -\mathbf{B}_0 \operatorname{div} \boldsymbol{\xi}_{\perp} + B_0 \frac{\partial}{\partial z} \boldsymbol{\xi}_{\perp}. \quad (\text{A6})$$

457 Substituting (A6) into (A5), we have final expressions relating parallel and perpendicular
 458 displacements as,

459
$$\frac{\partial^2 \xi_z}{\partial t^2} = -C_s^2 F \cdot B_0^2 \frac{\partial}{\partial z} (\text{div} \xi_{\perp}). \quad (\text{A6})$$

460 Replacing $\partial/\partial t$ with $-i\omega$, (A6) yields the equation (3) in Section 4,

461
$$\xi_z = \frac{C_s^2}{\omega^2} F \cdot B_0^2 \frac{\partial}{\partial z} (\text{div} \xi_{\perp}).$$

462

463

464

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596

597

598

599

600 Figure captions

601

602 Figure 1.

603 Upper panel: Local time distribution of W event and E event (see below). Lower panels:
604 Epoch superposition of field line deflections in degrees for Goes5/6. Those events with
605 eastward deflections (clockwise rotation, azimuth angle decreased) at T=0 shown to the left
606 (E event) and those with westward deflections (counterclockwise rotation, azimuth angle
607 increase) at T=0 are to the right (W event). T=0 marked by vertical dotted lines corresponds
608 to the first peak of the Pi2 waveform. Amplitudes at the onset (T=0) were subtracted from the
609 original data to adjust the pre-onset level. Plots covered 40 min from T-10 min to T+30 min.
610 Mean value of the epoch plot and mean value of band-passed (6-20 mHz: Pi2 band)
611 amplitudes are also shown. The field line rotations projected to the equatorial plane are
612 illustrated for E event and W event in the Figure (viewed from north of the equatorial plane).

613

614

615 Figure 2.

616 A progress of field line thinning in the growth phase is illustrated. The inflow flux (F_{\perp}) rotated
617 counterclockwise in times designated by red, green, and to blue arrows north of the
618 equatorial plane. South of the equatorial plane, rotation was in a clockwise direction. The
619 rotation of the inflow vectors produced the field-aligned component of the flux,
620 $\delta F_{\parallel} = F_{\perp}(\omega \cdot \delta t)$ as depicted in the inset with one in the northern hemisphere shown. Note
621 that inflows are localized earthward of the outer field lines.

622

623

624 Figure 3.

625 Simulated pitch angle spectrogram of energy flux for drift Maxwell distributions of phase
626 space density. Energy flux was shown in contour plots with arbitrary amplitudes. To show
627 how the pitch angle spectrogram evolves, drift velocities in parallel and perpendicular
628 directions with respect to the background magnetic fields have changed. No drifts in both
629 perpendicular and parallel to the background field lines (A). Only parallel drifts increased;
630 $0.3V_{th}$ (B), $0.6V_{th}$ (C) and $1.0V_{th}$ (D). For (E) and (F), perpendicular drift increased to $0.3V_{th}$
631 and $0.5V_{th}$ while parallel drift remained at $1.0V_{th}$. V_{th} denotes thermal velocity. The vertical
632 axis is for pitch angles, while the horizontal axis is for particle energies normalized by the
633 thermal energy.

634

635

636 Figure 4.

637 (A) Multiple Pi2 event (1, 2, 3, and 4 labelled in the Figure) with positive bay observed at low
638 latitude station (KUJ) at L=1.2 in the midnight sector (23:42 MLT at 15:00 UT). The figure,
639 from 1430 UT to 1600 UT 31 August 1986, was reproduced from [Saka et al., 2002]. (B)

640 Inclination angle of field lines in dipole coordinates along the satellite trajectories measured

641 by AMPTE CCE spacecraft. Inclination angle (θ) was defined as $\theta = \text{Tan}^{-1}\left(H/\sqrt{V^2 + D^2}\right)$.

642 H is positive northward parallel to the dipole axis, V is radial outward, and D is dipole east.

643 Vertical arrows denote dipolarization onset corresponding to the multiple Pi2; 1, 2, 3, and 4

644 in panel A. (C) Difference of duskward flux (counts/sample) (\mathbf{J}_-) and dawnward flux (\mathbf{J}_+) for

645 63-85 keV ion channel measured by AMPTE CCE spacecraft. (D) Same as for (C) but for
646 125-210 keV ion channel.

647 Radial distance (R) in Re, MLaT in degrees, and MLT at 14:30 UT, 15:00 UT and 16:00 UT
648 along satellite trajectory are shown in the bottom.

649

650

651 Figure 5.

652 A schematic illustration of particle measurement in X-Y plane of GSE coordinates; X is
653 earthward, Y is duskward in ecliptic plane. For the time interval of multiple Pi2 event when

654 the satellite was at 22 MLT, duskward flux represented by (\mathbf{J}_-) came from the earthward

655 sector and dawnward flux (\mathbf{J}_+) from tailward sector. $\mathbf{J}_- > \mathbf{J}_+$ because of the pressure

656 gradient positive earthward. Spatial gradient represented by solid line relaxed to dotted line.

657 Radial separation, $X_1 - X_2$, is either 1000 km or 1800 km for 63-85 keV ions or 125-210
658 keV ions, respectively.

659

660

661 Figure 6.

662 A schematic illustration of the field line deformations in the meridian plane associated with
663 the changing curvature radius of the field lines. The outer field lines marked by (1) changed

664 to field lines (2) by increasing their curvature radius to R1 (red-dashed circle) in association

665 with the relaxation of radial inhomogeneity, while the inner field lines marked by (3) moved

666 to field lines (4) of smaller curvature radius R2 (blue-dashed circle). This transition, (3) to (4),
667 may be caused by the radial gradient of magnetic pressures becoming steeper in association
668 with the inward compression of the field lines (see text). In the inset, flux tube deformations
669 in the equatorial cross section is illustrated at onset locations (field lines 1 and 2). Divergence
670 of perpendicular flows in dawn-dusk directions (solid arrows) produced dawn-dusk expansion
671 of flux tube (2) coincide with the shrinkage of stretched flux tube (1). Flux tube deformation
672 from 1 to 2 tended to preserve the total magnetic fluxes in the equatorial cross section.

673

674

675 Figure 7.

676 (A) Vertical component of $(rot \mathbf{J})_Z$ in the meridian chain along $300^\circ E$ for the interval from
677 1000 UT to 1500 UT, reproduced from Saka and Hayashi (2017). Dipolarization onset was
678 at 12:13 UT at this meridian. For the calculation of $(rot \mathbf{J})_Z$, vertical component data from
679 RES ($83.0^\circ N, 299.7^\circ E$), CBB ($76.6^\circ N, 301.2^\circ E$), CONT ($72.6^\circ N, 298.3^\circ E$), YKC ($68.9^\circ N,$
680 $298.0^\circ E$), FSIM ($67.2^\circ N, 290.8^\circ E$), FSJ ($61.9^\circ N, 295.5^\circ E$), and VIC ($54.1^\circ N, 296.7^\circ E$) along
681 the magnetic meridian $300^\circ E$ were used (see text). Positive for the clockwise rotation (CW)
682 of ionospheric currents and negative for the counterclockwise rotation (CCW) viewed from
683 above the ionosphere. Amplitudes are color-coded. The scale is shown on the right.
684 Demarcation lines separating CCW and CW in latitudes are marked by dashed line. The
685 demarcation line moved to poleward after the onset. Note that negative $(rot \mathbf{J})_Z$ in
686 poleward edge indicates smooth decrease of the Z amplitudes.

687

688 (B) Time progresses of the CW/CCW patterns are illustrated separately in five segments from
689 1 to 5 marked in Figure 7 (A). The figure demonstrates a progress of CW/CCW pair in time,
690 CW in the poleward and CCW in the equatorward. This pair developed its size after onset
691 showing poleward expansion. The meridional current associated with this pair of loop current,
692 if closed in the equatorial plane via the field-aligned currents, comprised the Bostrom type
693 current system.

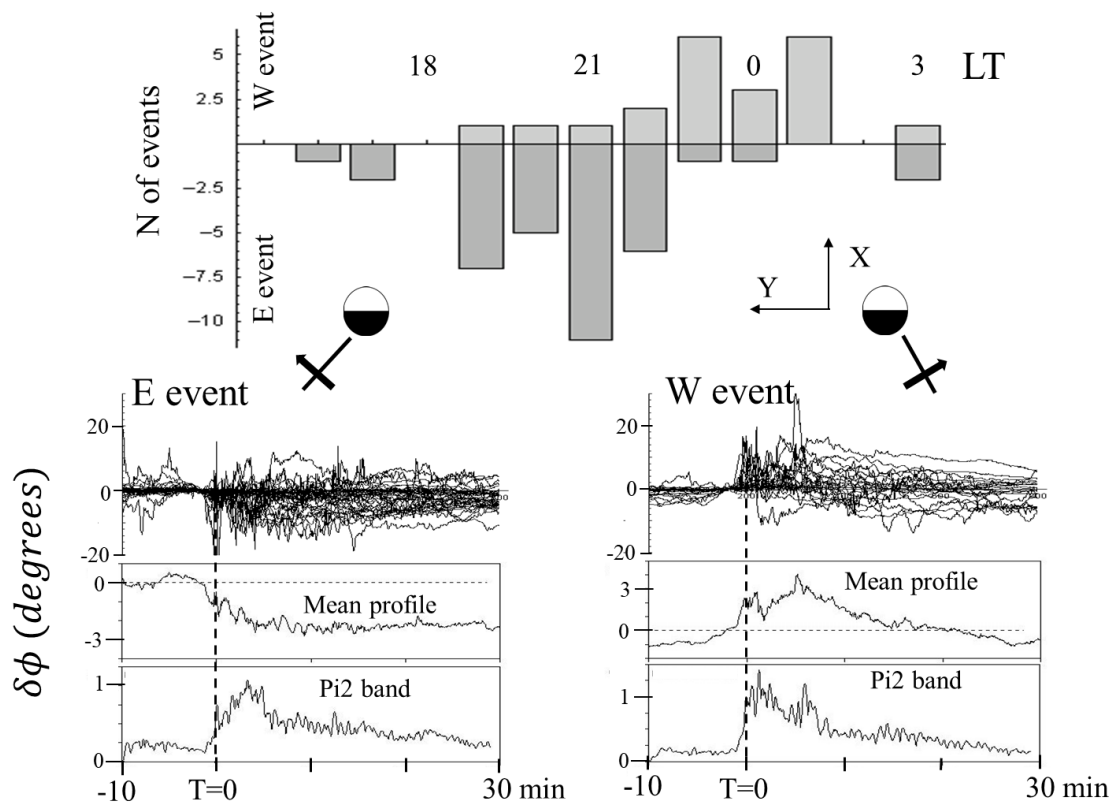


Figure 1

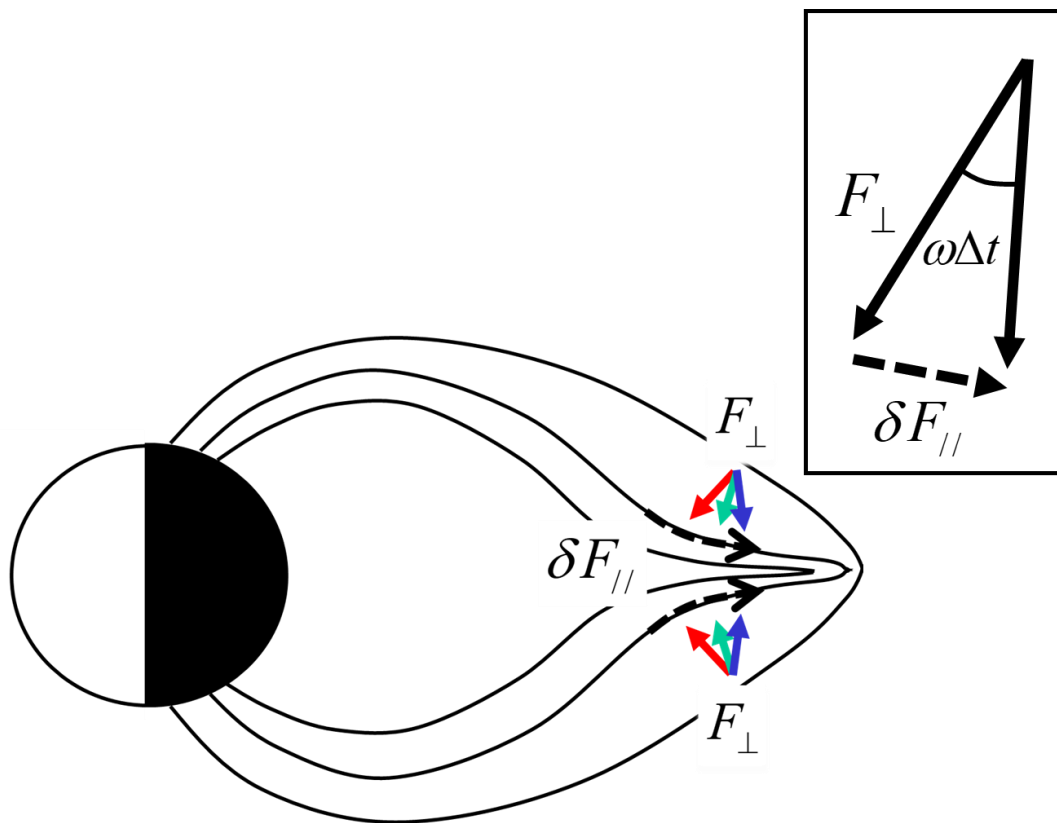


Figure 2

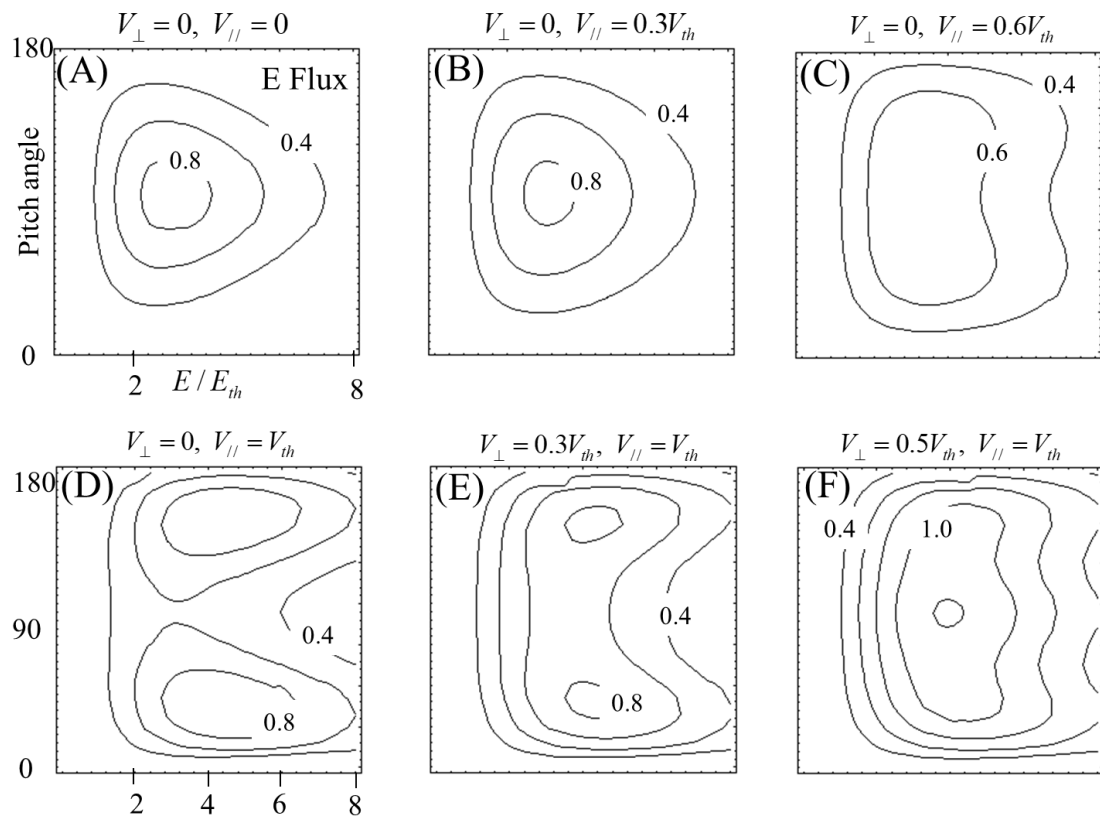


Figure 3

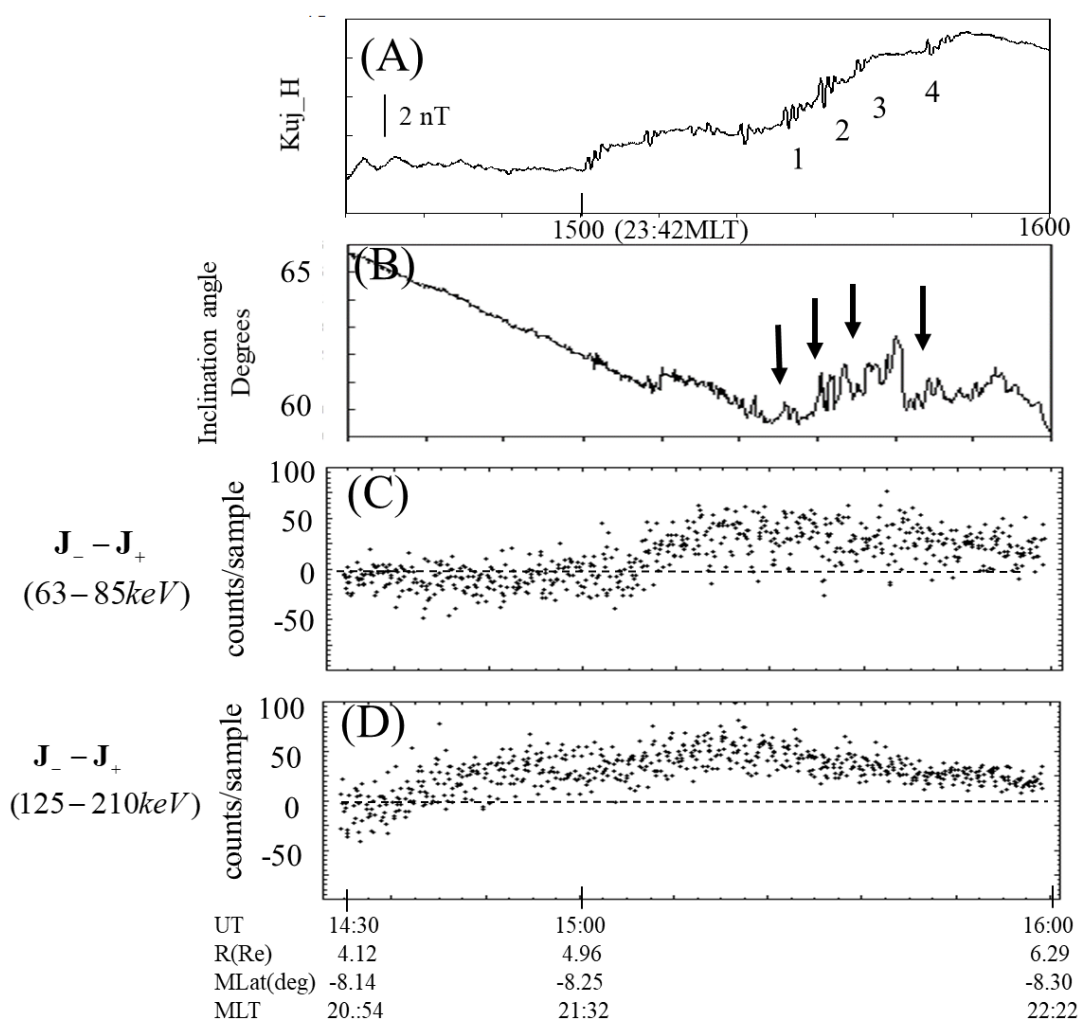


Figure 4

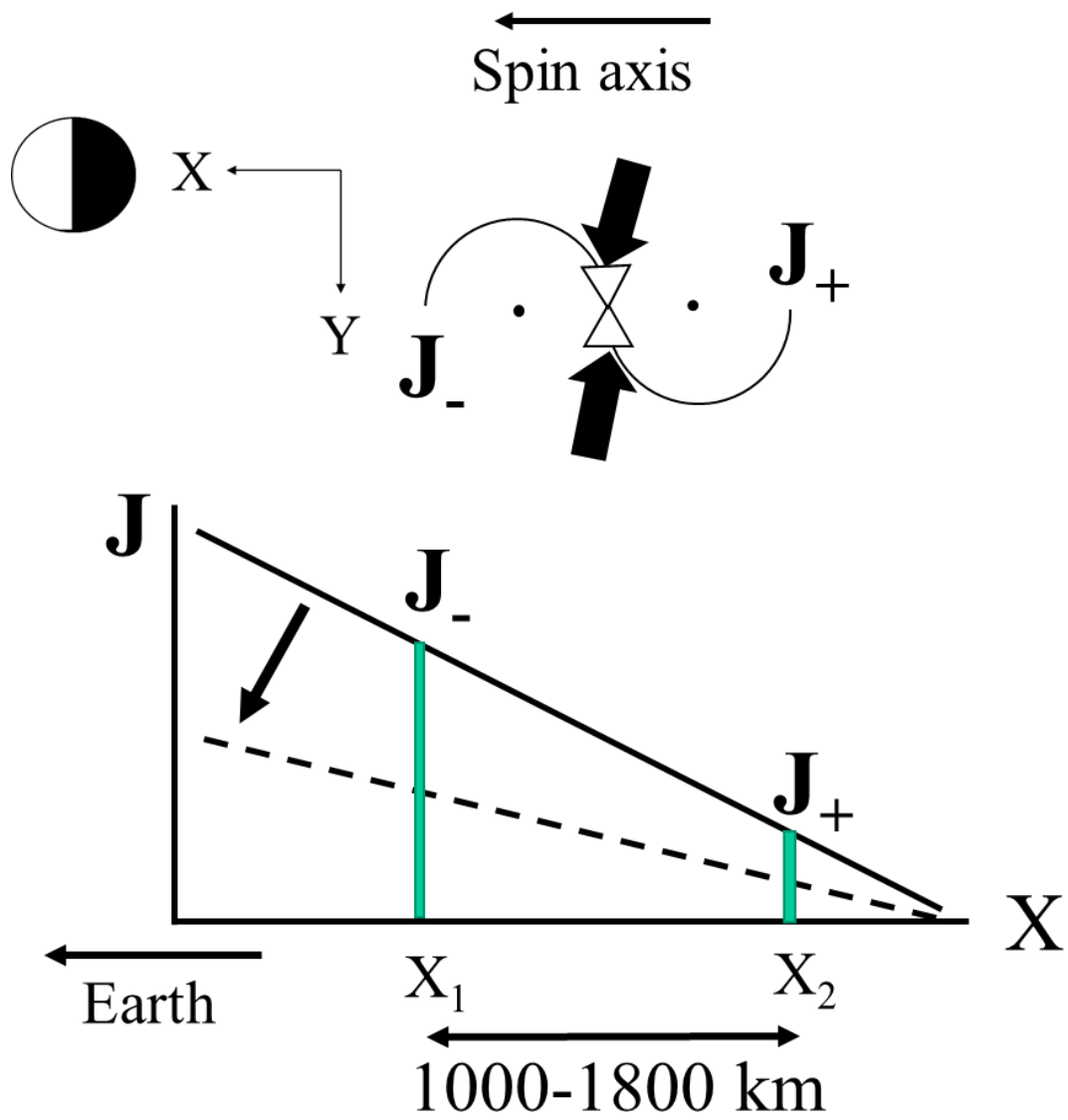


Figure 5

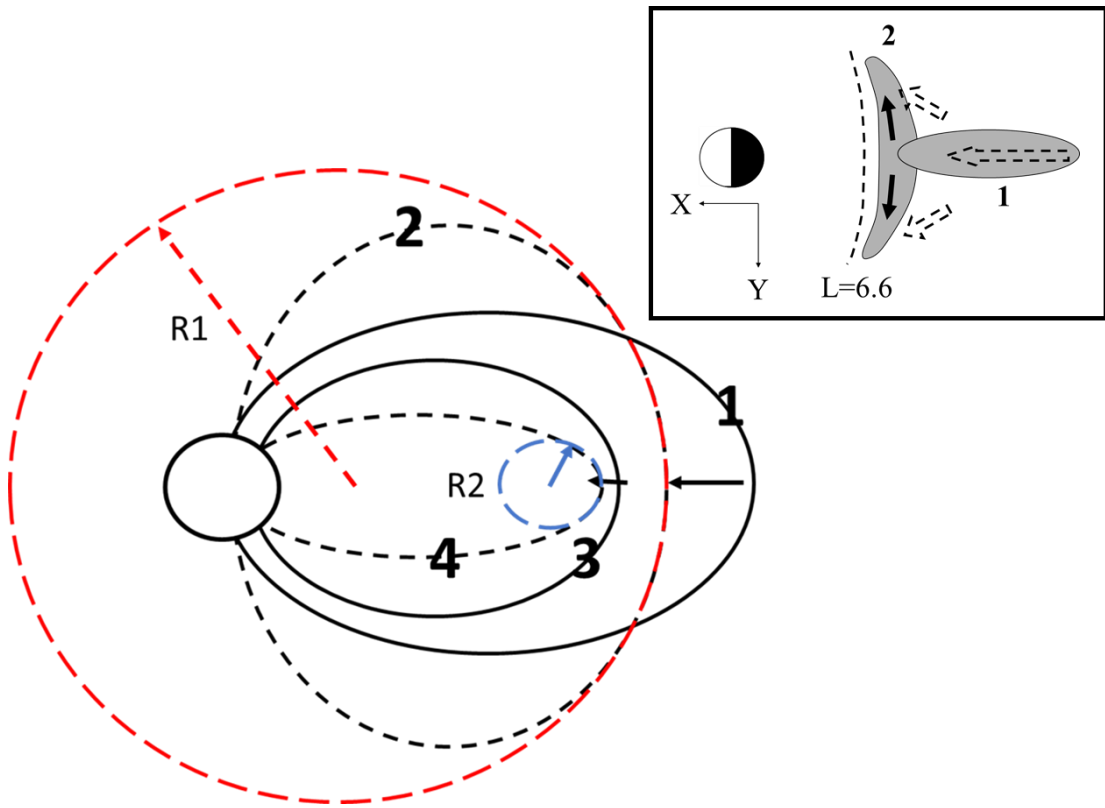


Figure 6

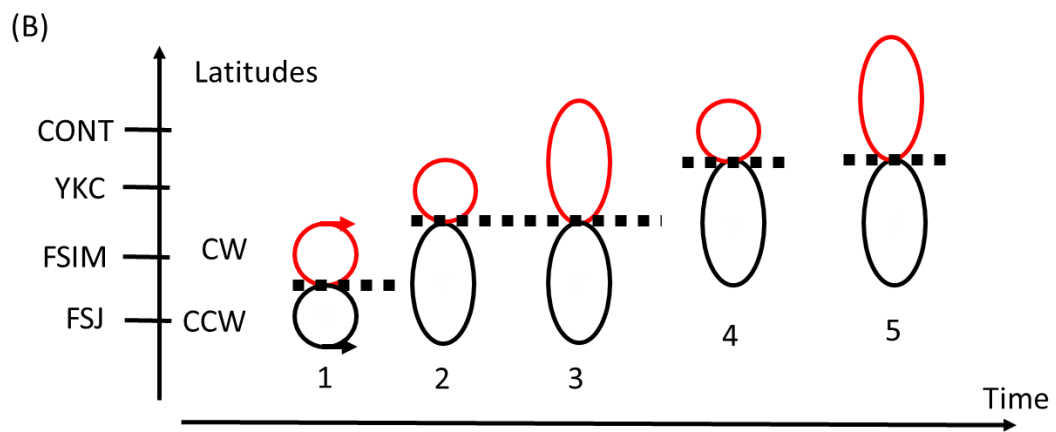
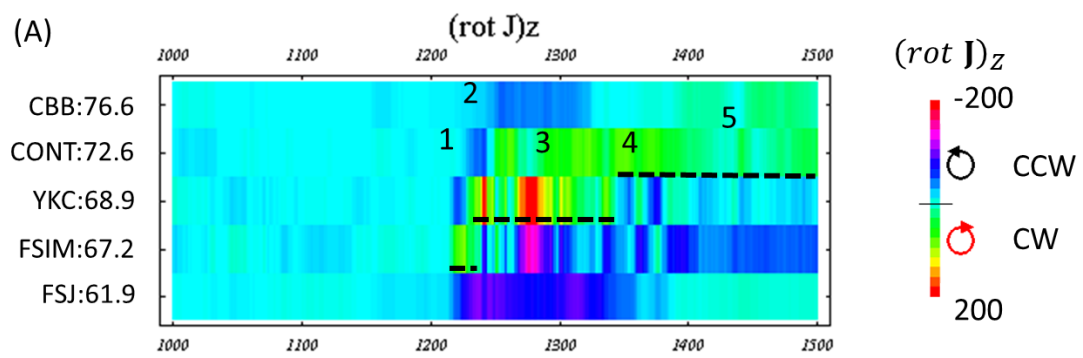


Figure 7