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8

9 **Abstract**

10 Transient westward electric fields from the magnetosphere generate equatorward plasma drifts of the  
11 order of kilometers per second in the auroral ionosphere. This flow channel extends in north-south  
12 directions and is produced in the initial pulse of Pi2 pulsations. Drifts in the ionosphere of the order  
13 of kilometers per second that accumulated plasmas at the low latitude end of the flow channel are of  
14 such large degree that possible vertical transport effects (including precipitation) along the field lines  
15 may be ignored. In order to interrupt the excess accumulation through the drift, we suggest that  
16 ionosphere responds nonlinearly to decelerate the equatorward drifts in the flow channel analogous to  
17 a traffic flow of cars on crowded roads. We apply this analogy to the poleward expansion of auroras.

18

19 **1. Introduction**

20 “Auroras and solar corona observed at the solar eclipse are optical phenomena unique in space physics.  
21 With enough knowledge about the underlying physical processes, once auroras have been captured by  
22 a highly sensitive imager, they provide an unexpected wealth of information about plasma  
23 environment of the Earth” [Oguti, 2010]. Plasma drifts in the ionosphere observed by the balloon-  
24 measured electric fields [Kelley et al., 1971], by the Ba releases [Haerendel, 1972] and by radar  
25 observations [Nielsen and Greenwald, 1978] did not match the expanding trajectories of auroras. This  
26 fact raises one of several unanswered questions involving violent poleward motion of auroras  
27 [Akasofu et al., 1966]. To account for the difference in propagation directions, it was suggested that

28 auroras were directly connected to the reconnecting flux tube moving tailward in the plasma sheet.  
29 This idea suggests that the primary sources of particles are in the magnetosphere, though they might  
30 be accelerated in lower altitudes for precipitations. This concept has been accepted in the literature for  
31 many decades.

32 It is worthy to consider whether the above idea also explains auroras associated with Pi2 pulsations.  
33 This is because Pi2 pulsations are accompanied by non-vortical slippage motions in the equatorial  
34 plane of midnight magnetosphere [Saka et al., 2007] while plasma motions in the auroral ionosphere  
35 were dominated by vortical flows [Saka et al., 2015]. The third harmonic deformations of the  
36 geomagnetic fields were generated in the midnight magnetosphere for tying two regions between  
37 slippage motions in the magnetosphere and vortical motions in the auroral ionosphere [Saka et al.,  
38 2012]. We may thus infer that vortical flows in the ionosphere do not originate in the magnetosphere  
39 but are rather generated in the ionosphere itself [Saka et al., 2012]. In this context, we interpret the  
40 motion of auroras as of ionospheric origin.

41

## 42 **2. Auroras and field line reconfigurations associated with Pi2**

43 In Pi2 pulsations, poleward expansion of auroras arising out of the onset arc was observed in the initial  
44 pulse of Pi2 pulsations [Saka et al., 2012]. Statistical study of geomagnetic fields at geosynchronous  
45 orbit during Pi2 showed that field line inclination at geosynchronous orbit (Goes5/6 at  $285^\circ/252^\circ$  in  
46 geographic coordinates) decreased continuously in the growth phase and attained  $33.6^\circ/49.4^\circ$  in  
47 dipole coordinates 2-min prior to the initial peak of Pi2 amplitudes [Saka et al., 2010]. This result  
48 suggests the observed field line inclination prior to the onset conforms to T89 model of  $K_p=4$   
49 [Tsyganenko, 1989]. These field lines were mapped to auroral ionosphere at  $63.4^\circ\text{N}/62.7^\circ\text{N}$  in  
50 geomagnetic coordinates corresponding to a latitude of onset arc. From these estimations, we suggest  
51 that Bursty Bulk Flows (BBFs) appeared first at the onset latitudes and activated preonset auroras. In  
52 the initial pulse of Pi2 pulsations, field line inclination of Goes5 increased in a step-like manner, while  
53 for Goes6 transient pulses were observed [Saka et al., 2010]. The average latitudes of Goes5 and Goes6  
54 were at  $10.3^\circ\text{N}$  and  $7.9^\circ\text{N}$ , respectively in the T89 model for the average  $K_p$  index of 3. It is likely

55 that dipolarization was composed of transient pulses at latitudes closer to the equatorial plane. In the  
 56 following Pi2 pulses, an auroral surge was observed in all-sky images between 66°N to 74°N in  
 57 geomagnetic latitudes. They propagated eastward or westward at the poleward boundary of the auroral  
 58 zone and were interpreted as an auroral manifestation of flow bifurcation of fast earthward flows  
 59 (BBFs) [Saka et al., 2012].

60 Simultaneous with reconfigurations of field lines in meridional plane, field lines stretching initially  
 61 in tailward directions switched to dawn-dusk directions in the initial pulse of Pi2s [Saka et al., 2000].  
 62 This switching was associated with the excitation of slow MHD wave by the increasing inflows of  
 63 plasma sheet ions toward the equatorial plane in growth phase [Saka and Hayashi, 2017]. After  
 64 manipulating a set of linearized MHD equations [Kadomtsev, 1976], we have a relation between  
 65 parallel shrinkage of plasmas along the field lines ( $\xi_z$ ) and perpendicular stretching of the field lines  
 66 ( $\xi_\perp$ ) in the following form,

$$67 \quad \xi_z = \frac{C_s^2}{\omega^2} F \cdot B_0^2 \frac{\partial}{\partial z} (\text{div} \xi_\perp). \quad (1)$$

68 Here,  $C_s$ ,  $\omega$  and  $B_0$  are the sound velocity, angular frequency of waves and background field  
 69 magnitudes, respectively.  $F$  is given by  $F = \frac{C_A^2}{B_0^2} \frac{1}{C_s^2 - (\frac{\omega}{k})^2}$  and is positive for the slow mode and  
 70 negative for the fast mode.  $C_A$  denotes Alfvén velocity. If the wave mode was the fast mode, flux  
 71 tubes would have contracted in longitudes towards the midnight sector, which was not observed during  
 72 the first one-minute-interval of Pi2 onset (initial pulse of Pi2 onset). An alternative explanation of  
 73 polarization switching may involve Ballooning instability of the coupled poloidal Alfvén and slow  
 74 magnetoacoustic modes [Rubtsov et al., 2018]. This switching from tailward to dawn-dusk directions  
 75 disrupts the cross-tail currents creating a step like dipolarization or dipolarization pulses in the initial  
 76 pulse of Pi2 pulsations and producing transient convection surge and associated westward electric  
 77 fields in the midnight sector. The convection surge occurred once in the initial pulse of Pi2 pulsation  
 78 but is not repeated in the following pulses.

79

80 **3. Horizontal plasma flows in the ionosphere**

81 It is reasonable to assume that westward electric fields were transmitted along the field lines to  
 82 the auroral ionosphere by the guided poloidal mode [Radoski, 1967] from the surge location and  
 83 created an equatorward flow through  $E \times B$  drift of the order of kilometers per second in the auroral  
 84 ionosphere. Electric fields of the order of 100 mV/m generate these high velocity flows in the  
 85 ionosphere. The flows would be confined in a channel expanding in the north-south directions in the  
 86 midnight sector. The low-latitude end of the flow channel was at the latitudes of the onset arc  
 87 corresponding to earthward edge of the BBFs. The high-latitude end may not expand beyond the  
 88 poleward boundary of auroral zone. Longitudinal width of the flow channel may be in about 1 to 2  
 89 hours of local time ( $\sim 1000$  km along  $65^\circ$ N) corresponding to horizontal scale size of Pi2 vortices  
 90 [Saka et al., 2014].

91 In the flow channel, drift across the magnetic fields for the  $j$ -th species ( $\mathbf{U}_{j\perp}$ ) can be written in  
 92 the F region as [Kelley, 1989],

$$93 \quad \mathbf{U}_{j\perp} = \frac{1}{B} \left[ \mathbf{E} - \frac{k_B T_j}{q_j} \frac{\nabla n}{n} \right] \times \hat{\mathbf{B}}. \quad (2)$$

94 Here,  $\mathbf{E}$  denote westward electric fields in the flow channel and  $\hat{\mathbf{B}}$  denotes a unit vector of the  
 95 magnetic fields  $B$ , downward in the auroral ionosphere. Symbols  $k_B$ ,  $T_j$ ,  $q_j$ , and  $n$  are the Boltzmann  
 96 constant, temperature of the  $j$ -th species, charge of the  $j$ -th species, and density of electrons (ions),  
 97 respectively. The electric field of the order of 100 mV/m exceeded the diffusion (second term) by three  
 98 orders of magnitudes in low temperature ionosphere. The  $E \times B$  drift predominated in the F region  
 99 and diffusion term may be ignored. In the E region, drift trajectories may be written [Kelley, 1989] for  
 100 electrons by,

$$101 \quad \mathbf{U}_{e\perp} = \frac{1}{B} [\mathbf{E} \times \hat{\mathbf{B}}] \quad (3)$$

102 and for ions by,

103 
$$\mathbf{U}_{i\perp} = b_i[\mathbf{E} + \kappa_i \mathbf{E} \times \hat{\mathbf{B}}]. \quad (4)$$

104 Here,  $b_i$  is mobility of ions defined as  $\Omega_i/(B\nu_{in})$ ,  $\kappa_i$  is defined as  $\Omega_i/\nu_{in}$ . Symbols  $\Omega_i$  and  
 105  $\nu_{in}$  are ion gyrofrequency and ion-neutral collision frequency, respectively.  $\hat{\mathbf{B}}$  denotes a unit vector  
 106 of the magnetic fields  $B$ . To derive equations (3) and (4), pressure gradient term (diffusion) was  
 107 again ignored. In the E region ( $\kappa_i = 0.1$ ), although the first term of (4) exceeds the second term by  
 108 one order of magnitudes, plasma accumulation in equatorward latitudes by the imposed westward  
 109 electric fields was produced by equation (3) for electrons and the second term in (4) for ions. However,  
 110 electron accumulation in lower latitudes increased southward electric fields and simultaneously ion  
 111 drifts in the first term of (4). If the southward electric fields grew to exceed the westward electric fields  
 112 by an order of magnitudes, ion drifts in the first term of (4) and electron drifts in (3) balanced to satisfy  
 113 the quasi-neutrality. This is equivalent to the generation of the Pedersen currents in the ionosphere.  
 114 Thus, electrostatic potential is generated in the E region, positive in poleward and negative in  
 115 equatorward. The Pedersen currents would have closed to the field-aligned current (FAC) and sustain  
 116 the steady state electrostatic potential produced in the ionosphere. Plasma drifts in the ionosphere,  
 117 both in E and F regions, accumulate density at the low-latitude edge of the flow channel. In the  
 118 following section, we discuss vertical transport of these accumulated materials from the low-latitude  
 119 edge of the flow channel.

120

121 **4. Vertical plasma flows in the ionosphere**

122 The transient compression of the ionospheric plasmas at the low-latitude edge of flow channel  
 123 would excite the ion acoustic wave in the ionosphere travelling along the field lines upward and  
 124 downward directions from the density peak of the F region. Figure 1 shows altitude distribution of the  
 125 pre-onset density profile of electrons (black) and density profile caused by the accumulation in red.  
 126 The accumulation doubled the electron density profile from 90 km to 1000 km in altitudes. Electron  
 127 density profile in black was plotted using sunspot maximum condition given in Prince and Bostic  
 128 (1964). The travelling ion acoustic waves, upward and downward, are denoted by vertical arrows. Ion

129 acoustic wave propagating downward may be eventually absorbed in the neutrals, while the upward  
 130 wave may propagate along the field lines further upward. We will focus only on the upward travelling  
 131 ion acoustic wave. The ion acoustic wave produced the parallel electric fields in accordance with the  
 132 Boltzmann relation [Chen, 1974],

$$133 \quad E_{//} = -\frac{k_B T_e}{q} \frac{\nabla_{//} n_e}{n_e}. \quad (5)$$

134 Here,  $k_B$  is Boltzmann constant,  $q$  is electron charge,  $T_e$  is electron temperature, and  $n_e$  is  
 135 electron density ( $n_e = n_i$ ). Equation (5) gives electric field strengths of the order of  $0.4 \mu V / m$  and  
 136  $2.0 \mu V / m$  for  $T_e = 1000 K$  and  $T_e = 5000 K$ , respectively, when the e-folding distance of  
 137 density dropout along the field lines was 200 km. For ions, steady-state motions exist in the ionosphere  
 138 in the altitudes where ion-neutral collision frequencies exceed ion acoustic wave frequencies. In that  
 139 case, parallel motions can be written as [Kelley, 1989],

$$140 \quad V_{i//} = b_i E_{//} - D_i \frac{\nabla_{//} n}{n} - \frac{g}{v_{in}}. \quad (6)$$

141 Here,  $b_i$  and  $D_i$  denote mobility and diffusion coefficient of ions defined by  $\frac{q_i}{M_i v_{in}}$  and

142  $\frac{k_B T_i}{M_i v_{in}}$ , respectively. Symbols,  $M_i$ ,  $q_i$ ,  $v_{in}$ , and  $g$  are ion mass, electric charge of ions, ion-

143 neutral collision frequency, and gravity, respectively. Ion-neutral collision frequencies from 400 km  
 144 to 1000 km in altitudes were plotted in Figure 2 using nighttime sunspot maximum condition in  
 145 Prince and Bostick (1964). Frequencies of ion acoustic wave were calculated by substituting  
 146 wavelength of ion acoustic wave into the dispersion relation. The wavelength was assumed to be  
 147 identical to initial accumulation distance along the field lines. We chose two cases, 1000 km and  
 148 4000 km. Phase velocity of the ion acoustic wave of the order of 1600 m/s for the electron  
 149 temperatures of 5000K yields the wave frequencies of  $1.6 \times 10^{-3} s^{-1}$  for the wavelength of 1000 km  
 150 and  $4.0 \times 10^{-4} s^{-1}$  for 4000 km. These frequencies were overlaid in Figure 2. Steady-state ion  
 151 motions can be adopted up to 800 km, for a wavelength over 1000 km.

152 Altitude profile of steady-state ion flows were evaluated substituting 1000K for ion temperatures  
 153 and the same e-folding distance in equation (5). Ions are oxygen and parallel electric fields are given  
 154 by the equation (5). Snapshot of the velocity profile in altitudes from 400 km to 800 km is shown in  
 155 Figure 3 for the two cases of electron temperatures, 5000K for black dots and 1000K for red dots.  
 156 For the low temperature case (1000k), there occurred no ion upflow because the parallel electric  
 157 fields could not overcome gravity. We suggest that electron temperatures over 2700K would be  
 158 needed to excite ion upflow. When electron temperature was set to 5000K, ion velocity 15 m/s at 400  
 159 km in altitudes increased rapidly to 1369 m/s at 800 km. The altitude profile of the flow velocity in  
 160 Figure 3 matched Type 2 ion outflow observed by EISCAT radar [Wahlund et al., 1992]. We conclude  
 161 that the ion upflow in topside ionosphere was caused primarily by the parallel electric fields excited  
 162 by the upward travelling ion acoustic wave. Below 600 km in altitudes, upflow velocity was one-to-  
 163 two orders of magnitudes smaller than the equatorward drift in the flow channel. Upflow velocity  
 164 became comparable to the horizontal drift over 800 km in altitudes and exceeded the phase velocity  
 165 of ion acoustic wave. Parallel velocity that prevailed the ion acoustic phase velocity may excite a  
 166 shock at the topside ionosphere. The shock velocity may increase with altitudes in higher electron  
 167 temperatures. A part of them would be observed as electrostatic shock or double layers at the altitudes  
 168 of 6000 – 8000 km [Mozer et al., 1976; Temerin et al., 1982]. Those electrostatic shocks would have  
 169 produced parallel potential structures referred to as inverted-V at the low latitude end of the flow  
 170 channel. In this scenario, inverted-V as well as upward FACs are major components contributing to  
 171 auroral acceleration in lower latitudes.

172

### 173 **5. Nonlinear evolution of the horizontal flows**

174 Accumulation of electrons and ions occurred at the equatorward end of the flow channel. We can  
 175 estimate a rate of accumulation by the following relation,

$$176 \quad \frac{\Delta n}{\Delta t} = -n_0 \frac{\Delta U}{\Delta x} . \quad (7)$$

177 Here  $n$  is plasma density,  $U$  denotes drift velocity in the flow channel in  $x$ . Substituting

178  $\Delta U = 10^3 \text{ m s}^{-1}$  and  $\Delta x = 10^4 \text{ m}$ , we have  $\frac{\Delta n}{\Delta t} = 10^{10} \text{ m}^{-3} \text{ s}^{-1}$  for the background density

179  $n_0 = 10^{11} \text{ m}^{-3}$ . This gives density pileup of the order of  $\frac{\Delta n}{n_0} = 100\%$  in ten seconds. If the

180 equatorward drift in the flow channel is an order of  $10^3 \text{ m/s}$  ( $E=100 \text{ mV/m}$  in auroral ionosphere) and

181 electron production by the precipitation do not exceed the accumulation rate which was 100% of the

182 background density in ten seconds, both outflows and precipitation may not bring significant changes

183 to the flux carried by  $E \times B$  drift in the flow channel. We then approximate one dimensional (along

184 the drift path in  $x$ ) conservation equation in the flow channel.

$$185 \quad \frac{\partial n}{\partial t} + \frac{\partial}{\partial x}(nU) = 0 \quad (8)$$

186 A question arises regarding maximum accumulation of plasmas at the equatorward end of the flow

187 channel because unlimited accumulation may not occur. One possible mechanism to suppress the

188 accumulation may be associated with the ionospheric screening that decreased the amplitudes of

189 penetrated (total) westward electric fields by the increasing ionospheric conductivities. In a two-

190 dimensional ionosphere with uniform height-integrated conductivity, total electric fields  $E$  given by a

191 sum of the incident ( $E_i$ ) and reflected westward electric fields may be written as

192  $E = \left(2\Sigma_A / (\Sigma_A + \Sigma_P)\right) E_i$ , where  $\Sigma_A$  and  $\Sigma_P$  are Alfvén conductance defined by  $1/\mu_0 V_A$  and

193 height-integrated Pedersen conductance in the ionosphere, respectively [Kan et al., 1982]. Symbols

194  $\mu_0$  and  $V_A$  denote magnetic permeability in vacuum and Alfvén velocity, respectively. Amplitude

195 ratio of total electric fields to incident electric fields is a function of conductance ratio of Pedersen and

196 Alfvén;  $E/E_i = 2$  for a low conductivity of the ionosphere satisfying  $\Sigma_P/\Sigma_A \ll 1$ , and  $E/E_i = 0$

197 for a high conductivity of the ionosphere satisfying  $\Sigma_P/\Sigma_A \gg 1$ . Noting that  $\Sigma_P$  is proportional

198 to the plasma density in the ionosphere, the total electric fields monotonically decreased with

199 increasing plasma densities caused by accumulation itself and by the precipitations associated with

200 the auroral activity. Another explanation may be suggested in the polarization electric fields (eastward)

201 produced by the accumulation itself. These electric fields grew quickly with density accumulation and

202 decreased the incident electric fields (westward) by the superposition. In addition to the above  
 203 scenarios, we surmise that excess accumulation of the ionospheric plasmas may be suppressed through  
 204 the term,  $(\mathbf{U} \cdot \nabla)\mathbf{U}$ , in the equation of motion. From the ionospheric screening process discussed  
 205 above, we tentatively assume that flow velocity  $U$  is a function of the density  $n$ . Then the conservation  
 206 equation (8) may be written as,

$$207 \quad \frac{\partial n}{\partial t} + \frac{\partial}{\partial x} Q(n) = 0. \quad (9)$$

208 Here,  $Q(n)$  is a mass flux defined by  $Q(n)=nU(n)$ . This relation can be reduced to nonlinear wave  
 209 equation,

$$210 \quad \frac{\partial n}{\partial t} + c(n) \frac{\partial n}{\partial x} = 0. \quad (10)$$

211 Here  $c(n)$  is a wave propagation velocity defined by  $c(n) = U(n) + nU'(n)$ ,  $U(n)$  is a drift velocity  
 212 in the flow channel, and  $U'(n)$  denotes braking/acceleration of the drift velocity by increasing and  
 213 decreasing density. The equation (10) is often referred to as propagation of “kinematic waves” to  
 214 describe traffic flow [Lighthill and Whitham, 1955]. In the following, we use dimensionless units  
 215 normalized by  $U_m$ , and  $n_m$ . Here,  $U_m$  and  $n_m$  denote maximum drift velocity at  $n=0$  and maximum  
 216 density for complete stops of the drift, respectively. Assuming a constant braking in the flow channel,  
 217 we define  $U$  by a linear function of density  $n$  as  $U(n)=1-n$ . Noting that  $Q'(n)=c(n)$ , this relation is  
 218 reduced to the equation,  $Q(n)=n(1-n)$ , identical to the case for the traffic flow [Whitham, 1999]. Both  
 219 the  $U$  and  $Q$  are plotted in Figure 4A as a function of  $n$ . A nonlinear evolution of the waves is presented  
 220 in Figure 4B by the characteristic curves. In the case of vehicles in traffic, the initial flows started from  
 221  $n=0$  and stopped at  $n=1.0$  by the tailback of cars. For the case of the ionosphere, the ionospheric  
 222 density started from a finite density,  $n=0.3$  (Figure 4B), and increased to  $n=1.0$  to terminate the flow  
 223 by the full screening. The nonlinear evolution of the density profile in time is shown in Figure 4B in  
 224 colors from black ( $T=T_1$ ), red ( $T=T_2$ ), green ( $T=T_3$ ), blue ( $T=T_4$ ), and to purple ( $T=T_5$ ). After  $T=T_5$ ,  
 225 the waves propagate upstream (poleward) as a shock. The shock velocity,  $V$ , is given as [Whitham,  
 226 1999],

227 
$$V = \frac{Q(n_2) - Q(n_1)}{n_2 - n_1}. \quad (11)$$

228 Here, subscript 1 is for the values ahead shock and subscript 2 is for the values behind. Noting that  
 229  $Q(n_2)=0$  and substituting  $Q(n_1)=n_1(n_2-n_1)$ , the equation (11) can be reduced to  $V = -n_1$  in  
 230 dimensionless unit. The propagation velocity of the shock is related to the densities ahead. For the  
 231 case of  $n=0.3$  in Figure 4B, shock velocity can be estimated to be  $-0.3U_m$ . Here,  $U_m$  denotes maximum  
 232 drift velocity in the ionosphere where ionospheric screening effects vanished by the condition,  
 233  $\Sigma_p/\Sigma_A \ll 1$ .

234 We employed the traffic flow analogy to explain the poleward expansion of auroras. A similar case  
 235 may be found in “flow braking in near-Earth tail” [Shiokawa et al., 1997]. In this case, the advective  
 236 term in the equation of motion suppressed an excess pileup of the pressures caused by the fast  
 237 earthward flow itself. This may minimize the velocity of the ion flows at the pressure peak analogous  
 238 to a tailback of cars in traffic flows.

239

## 240 6. Summary

241 Allowing for the compressibility of the ionosphere caused by the ionospheric drifts of the  
 242 order of kilometers per second, we proposed a new scenario for the poleward expansion of auroras  
 243 including generation of field-aligned currents and parallel electric fields of the ionospheric origin. This  
 244 scenario, analogous to a traffic flow of cars on the crowded roads, partly explains the discrepant time  
 245 history of the auroras which is often described as the auroras expand opposite to that of plasma drift  
 246 in the ionosphere.

247

248

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253 are available at the Data Center for Aurora in NIPR (<http://polaris.nipr.ac.jp/~aurora>)

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328   **Figure Captions**

329   Fig. 1: Vertical profiles from 90 km to 1000 km in altitudes of electron number density in two  
330           conditions, pre-onset in black and after accumulation in red. Nighttime sunspot maximum condition  
331           given in Prince and Bostic (1964) was used to plot pre-onset condition. Vertical arrows directing  
332           upward and downward denote travelling ion acoustic waves propagating along the field lines from the  
333           density peak of F layer.

334

335 Fig.2: Ion-neutral collision frequency ( $\nu_{in}$ ) in altitudes from 400 km to 1000 km calculated using  
336 nighttime sunspot maximum condition in Prince and Bostick (1964). Wave frequencies of ion acoustic  
337 wave are overlaid for two wavelength, 1000 km and 4000 km along field lines (see text).

338

339 Fig. 3: Steady-state parallel velocity in altitudes for ions (oxygen) produced by parallel electric fields  
340  $0.4\mu V / m$  ( $T_e=1000K$ ) in red dots and  $2.0\mu V / m$  ( $T_e=5000K$ ) in black dots. Vertical flows in  
341 altitudes from 400 km to 800 km are shown. Flow velocity is positive upward and negative downward.

342

343 Fig. 4: (A) Normalized flux( $Q$ )-density( $n$ ) curve (thin curve) and velocity( $U$ )-density( $n$ ) line (thick  
344 line) in flow channel. Vertical scale of  $U$ - $n$  line is shown to the right, scale of  $Q$ - $n$  curve is to the left.  
345 Dotted line at  $n=0.5$  indicates the critical density where  $c(n)$  vanishes; waves are stationary relative to  
346 the ground. Waves propagate forward/backward at a density below/above the critical density. (B)  
347 Nonlinear evolution of the density accumulation. Density increased in a step like manner from  $T_1$  to  
348  $T_5$ . Shock velocity is 1.2 km/sec poleward when  $U_m=4.0$  km/s is assumed at  $n=0.3$  (see text).

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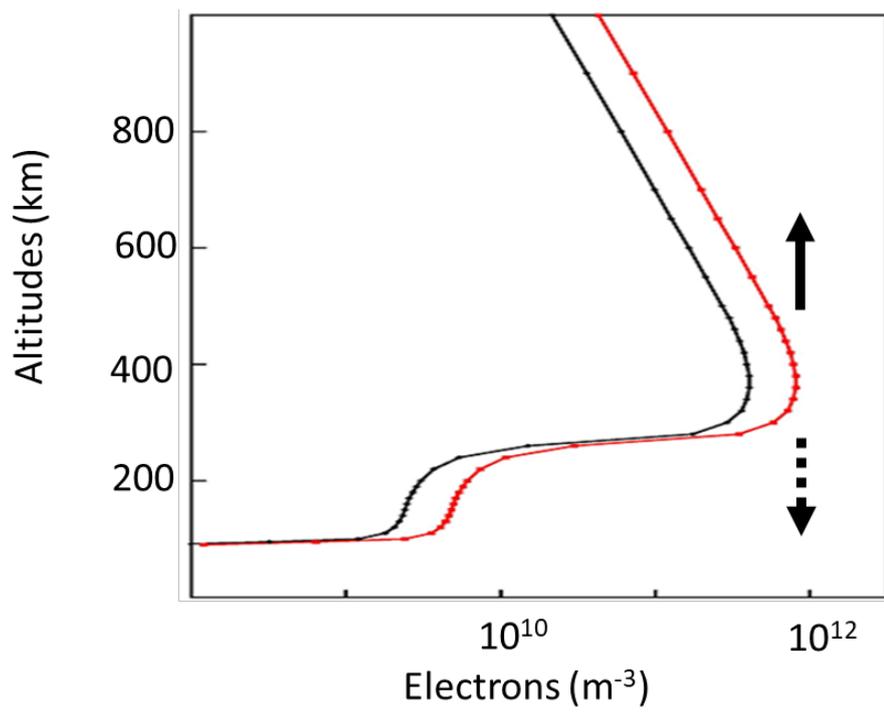


Figure 1

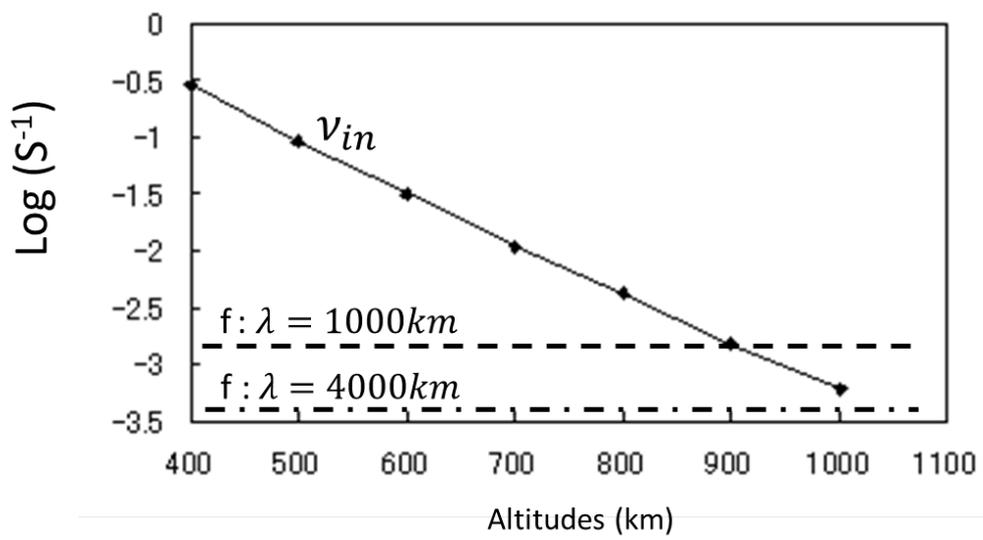


Figure 2

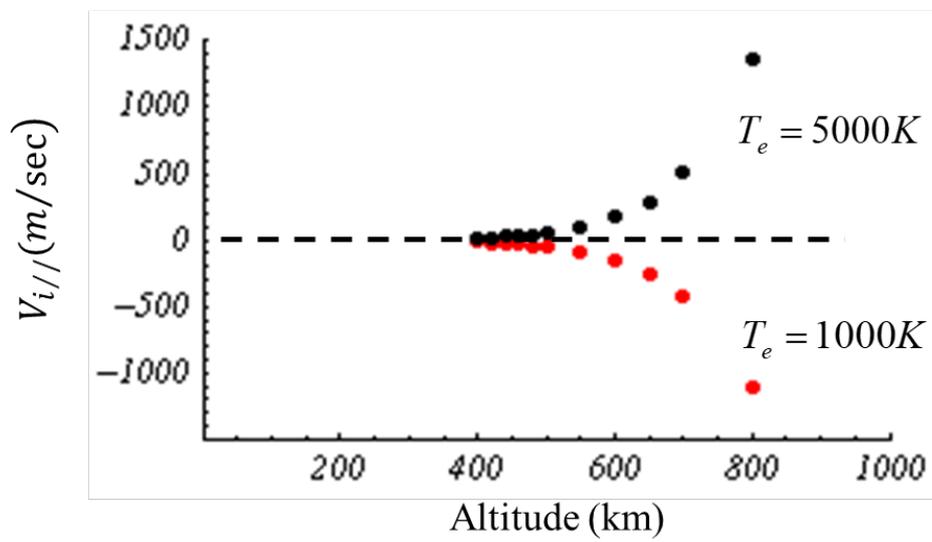


Figure 3

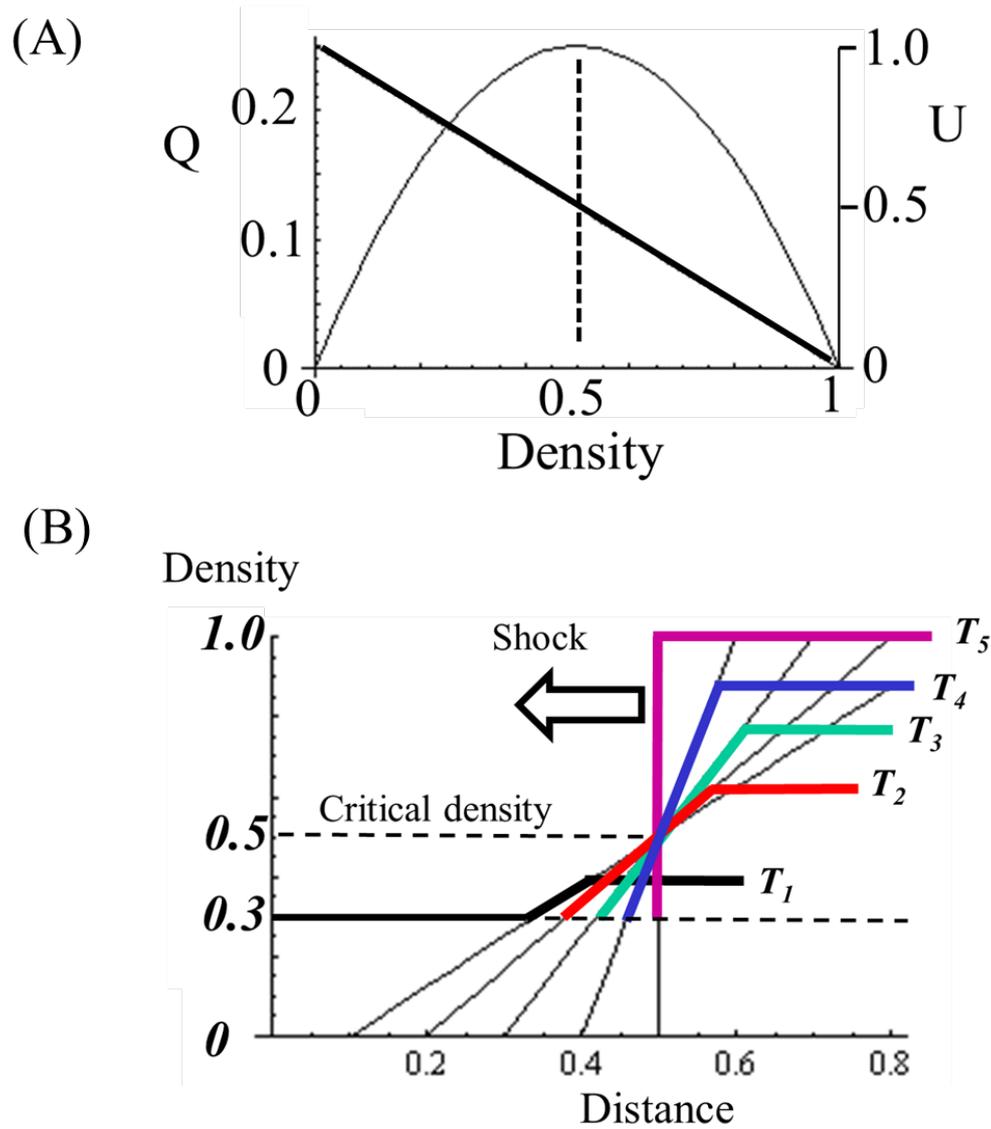


Figure 4