

# Comparisons between the WRF data assimilation and the GNSS tomography technique in retrieving 3D wet refractivity field in Hong Kong

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**Abstract:** Water vapor plays an important role in various scales of weather processes. However, there are limited means to accurately describe its 3-dimensional (3D) dynamical changes. The data assimilation technique and the Global Navigation Satellite System (GNSS) tomography technique are two of the limited means. Here, we conduct an interesting comparison between the GNSS tomography technique and the Weather Research and Forecasting Data Assimilation (WRFDA) (a representative of the data assimilation models) in retrieving Wet Refractivity (WR) in Hong Kong area during a wet period and a dry period. The GNSS tomography technique is used to retrieve WR from the GNSS slant wet delay. The WRFDA is used to assimilate the zenith tropospheric delay to improve the background data. The radiosonde data are used to validate the WR derived from the GNSS tomography, the WRFDA output, and the background data. The Root Mean Square (RMS) of the WR derived from the tomography results, the WRFDA output, and the background data are 6.50 mm/km, 4.31 mm/km, and 4.15 mm/km in the wet period. The RMS becomes 7.02 mm/km, 7.26 mm/km, and 6.35 mm/km in the dry period. The lower accuracy in the dry period is mainly due to the sharp variation of WR in the vertical direction. The results also show that assimilating GNSS ZTD into the WRFDA only slightly improves the accuracy of the WR and that the WRFDA WR is better than the tomographic WR in most cases. However, in a special experimental period when the water vapor is highly concentrated in the lower troposphere, the tomographic WR outperforms the WRFDA WR in the lower troposphere. When we assimilate the tomographic WR in the lower troposphere into the WRFDA, the retrieved WR is improved.

**Keywords:** GNSS Tomography; Wet Refractivity; Weather Research and Forecasting model; Data Assimilation

## 1 Introduction

Water vapor (WV), mostly contained in the troposphere, plays an important role in various scales of atmospheric processes. But due to its active nature, there are limited models and techniques that can accurately describe or monitor its 3-dimensional (3D) dynamical changes (Rocken et al., 1993).

The development of Global Navigation Satellite System (GNSS) technique and the densely deployed GNSS receivers provide us the opportunity to monitor the WV field in near real time. When GNSS signal travels through the neutral atmosphere, it undergoes time delay and bending due to atmospheric refractivity. This effect is usually called the tropospheric delay in the GNSS community (Altshuler, 2002). The tropospheric delay is usually considered as the product of the zenith delay and the mapping function (Lanyi, 1984; Niell, 1996). The Zenith Tropospheric Delay (ZTD) consists of two parts: the hydrostatic part and the wet part. The wet delay is mainly associated with the WV and reflects WV content in the troposphere. Bevis et al. (1992) introduced the principle of using GNSS Zenith Wet Delay (ZWD) to retrieve the Precipitable Water Vapor (PWV). Since then, many scientists carried out the GNSS PWV experiments (Askne and Nordius, 1987; Bokoye et al., 2003; Yao et al., 2014; Lu et al., 2015; Shoji and Sato, 2016). Now, the GNSS PWV can be retrieved with an uncertainty of 1-2 mm in post-processing (Tregoning et al., 1998; Adams et al., 2011; Grejner-Brzezinska, 2013) or real-time modes (Yuan et al., 2014; Li et al., 2014; Li et al., 2015).

42 The GNSS WV tomography technique was first proposed to monitor the 3D or 4D WV in 2000 (Flores et al.,  
43 2000; Seko et al., 2000; Hirahara et al., 2000). Since then, many scientists have proposed refined methods to  
44 improve the GNSS WV tomography (Flores et al., 2001; Nilsson and Gradinarsky, 2006; Rohm and Bosy, 2011;  
45 Wang et al., 2014; Wang et al., 2014; Zhao and Yao, 2017). The tomographic inversion algorithm can be  
46 roughly categorized into two groups. One group solves the tomography equation in the least squares scheme or  
47 in the Kalman filter scheme with additional constraints or using a priori information (Flores et al., 2000; Rohm  
48 and Bosy, 2011; Cao et al., 2006; Zhang et al., 2017). The other group uses the algebraic reconstruction  
49 algorithm or similar methods (Bender et al., 2011; Wang et al., 2014; Zhao and Yao, 2017). Some scientists  
50 also use different methods from the above to solve the GNSS WR tomography problem (Nilsson and  
51 Gradinarsky, 2006; Perler et al., 2011; Altuntac, 2015). Besides the algorithm improvement, some scientists  
52 tried to optimize the voxel division (Chen and Liu, 2014) or use virtual reference stations (Adavi and Mashhadi-  
53 Hossainali, 2014) or use additional GNSS rays (Zhao and Yao, 2017) to increase the effective GNSS rays and  
54 thus improve the tomography results. Though the tomography technique has the advantages of (1) free of  
55 weather conditions and (2) retrieve 3D WR field in near real time, it still suffers some problems. The sparse  
56 distribution of the GNSS receivers and the bad satellite-receiver geometry lead to serious ill-posed and ill-  
57 conditioned problems, and also limit the WR retrieve resolution in both vertical and horizontal domains.

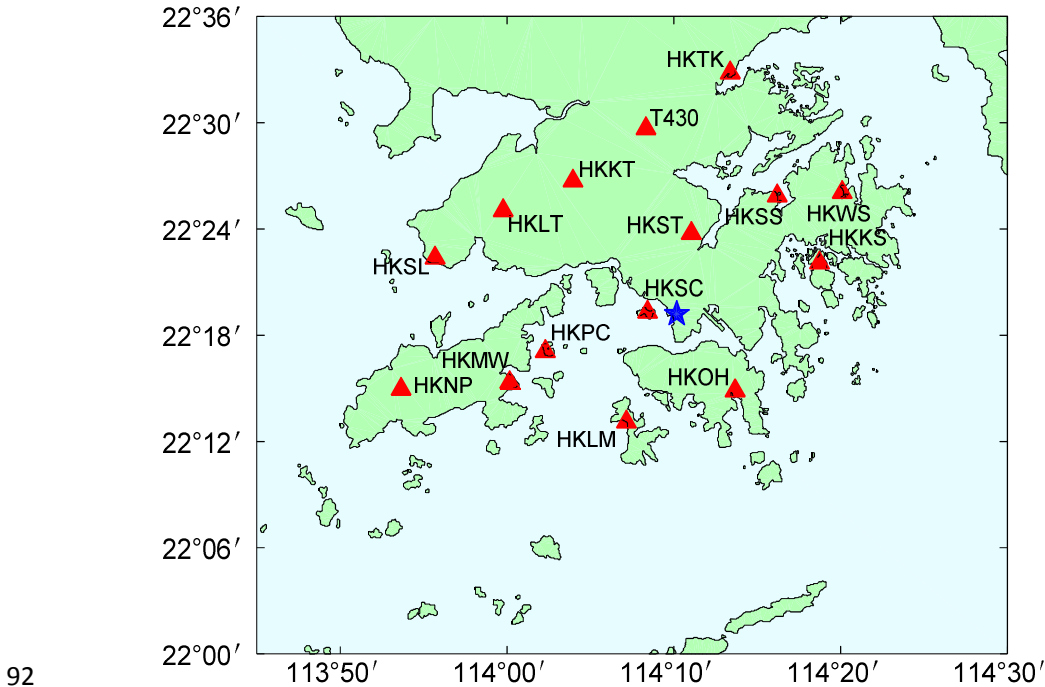
58 Besides the GNSS tomography technique, the WR can also be retrieved by data assimilation which is based on  
59 numerical weather prediction (NWP) models (Perler et al., 2011). The Weather Research and Forecasting (WRF)  
60 model is a state-of-the-art atmospheric modeling system that is used to simulate the dynamic processes of the  
61 atmosphere (Jankov et al., 2005; Carvalhoaabc et al., 2012). It is mainly developed and supported by Mesoscale  
62 and Microscale Meteorology (MMM) Laboratory of the National Center for Atmospheric Research (NCAR).  
63 And the WRF Data Assimilation (WRFDA) is designed to obtain the best estimate of the actual atmospheric  
64 state at any analysis time (Barker et al., 2004; Huang et al., 2008; Barker et al., 2012; Singh et al., 2017). Many  
65 studies have demonstrated that assimilating ZTD/PWV into WRFDA can improve the reanalysis water vapor  
66 field (Pacione et al., 2001; Faccani et al., 2005; Boniface et al., 2012; Bennitt and Jupp, 2012; Moeller et al.,  
67 2016; Lindskog et al., 2017). Besides the WRFDA model, the Japan Meteorological Agency (JMA) Mesoscale  
68 Numerical Weather Prediction Model (Nakamura et al., 2004) and AROME NWP system (Boniface et al., 2009)  
69 can also make use of ZTD/PWV data assimilation.

70 Though the GNSS tomography technique and the data assimilation technique belong to different fields, both of  
71 them could retrieve 3D WR field. It will be interesting to compare their capabilities in retrieving WR field under  
72 different weather conditions and to explore the feasibility to combine them. Such results may provides insights  
73 for the NWP community about this new technique and the possibility of assimilating the tomography results  
74 into the NWP models. For the GNSS community, they will get a better understanding of the WRF data  
75 assimilation and its capability in simulating the water vapor field. For this purpose, we conduct GNSS  
76 tomography and data assimilation experiments in Hong Kong area using SatRef Network in a wet period and a  
77 dry period. WR fields retrieved from GNSS tomography and WRFDA outputs are validated by the radiosonde  
78 data. We also explore the feasibility of assimilating the GNSS tomographic WR into the WRFDA to further  
79 improve the WR field.

## 80 **2 Research Area and Data Analysis**

81 The study area is within 113.75°E-114.5°E and 22°N-22.6°N as shown in Figure 1. There are 15 continues  
82 GNSS stations belonging to the Hong Kong SatRef Network deployed in the study area. They are all equipped  
83 with Leica GNSS receivers and antennas to receive the GNSS signals and automatic meteorological devices to  
84 record the temperature, pressure, and relative humidity. The average inter-distance between stations is about 10  
85 km. The altitudes of the highest station (HKNP) and the lowest station (HKLM) are 354 m and 10 m. In GNSS  
86 tomography, we regard a network whose altitude differences of its stations are less than 1 km as a flat network.  
87 Therefore, the SatRef network is a flat network.

88 Two periods of GNSS observation data are processed to generate ZTD and Slant Wet Delay (SWD). One is a  
89 wet period from July 20 to 26, 2015 when Hong Kong suffered the heaviest daily rainfall of 2015 (191.3 mm  
90 rainfall on July 22). The other is a dry period from August 1 to 7, 2015 when Hong Kong is rainless. The details  
91 about the GNSS data processing and the SWD reconstruction can be found in Appendix A.

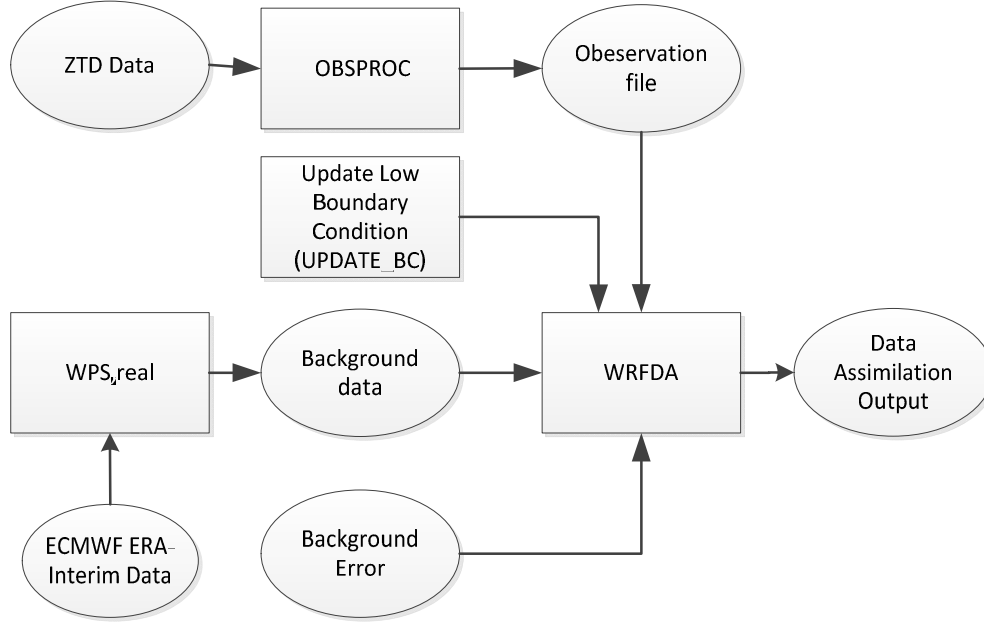


92  
93 **Figure 1.** Research area of the experiment. The red triangles indicate the GNSS stations and the blue star  
94 indicates the radiosonde station in Hong Kong.

### 95 **3 Method**

#### 96 *3.1. WRF Data assimilation*

97 The WRF model version 3.7 is used in this study. The WRFDA-3DVAR is used to assimilate the GNSS ZTD  
98 to improve the background data. The horizontal resolution of WRFDA output is set to 3 km. And the atmosphere  
99 is vertically divided into 45 layers. The pressure of the top layer is 50 hpa. There are 10 layers in the planetary  
100 boundary layer (PBL). We use the ZTD error output by the Bernese 5.0 software as observation error. We use  
101 the reanalysis data from European Center for Medium-Range Weather Forecasts (ECMWF) ERA-Interim  
102 pressure levels and surface data as the background data, whose spatial resolution is  $0.75^{\circ} \times 0.75^{\circ}$ . And we run  
103 the WRFDA model at 0:00 UTC and 12:00 UTC, corresponding to the radiosonde observation time. The  
104 procedures to do the assimilation experiments are shown in Figure 2.



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**Figure 2.** Flowchart of data assimilation using the WRF model.

107 The background data are processed by WRF preprocessing system (WPS). The WRFDA is run with the generic  
 108 CV3 option, and the default background error is adopted in this study. The GNSS ZTDs are the input  
 109 observations for WRFDA. We run WRFDA to obtain the data assimilation output, labeled as Output1. The  
 110 output from WPS and real.exe is labeled as Output2. We compare the WR derived from Output1 and Output2.  
 111 We use Equation (1) to calculate WR (Vedel and Huang, 2004) from the Output1 and Output2.

$$WR = \frac{P_w}{T} \times \left( k_1 + \frac{k_2}{T} \right) \quad (1)$$

112 where  $P_w$  is the water vapor pressure in each grid point in Pascal,  $T$  is the temperature in each grid point in  
 113 Kelvin.  $k_1 = 2.21 \times 10^{-7}$  K/Pa,  $k_2 = 3.73 \times 10^{-3}$  K<sup>2</sup>/Pa. We use Equation (2) to calculate  $P_w$ .

$$P_w = \frac{p \times q}{0.622} \quad (2)$$

114 where  $p$  is the pressure in Pascal,  $q$  is the specific humidity in g/g.

115 The WRFDA has many options for different physical parameterizations. In order to find the best choice for the  
 116 data assimilation experiment, we follow Chien et al. (2006) to set 12 schemes to do the sensitivity tests, which  
 117 are listed in Table 1. We carry out the sensitivity test at 00:00 UTC 22<sup>nd</sup> July in 2015. The domain size is set to  
 118  $30 \times 24$  grids which just cover the study area. The grid size is 3 km  $\times$  3 km. We run WRFDA using the different  
 119 setting schemes. The radiosonde data are used to validate the wet refractivity derived by the WRFDA output.  
 120 Table 1 shows that all schemes have the same bias, standard deviation (STD), and Root Mean Square (RMS),  
 121 which suggests that the output wet refractivity is not affected by the physical parameterization settings in  
 122 WRFDA.

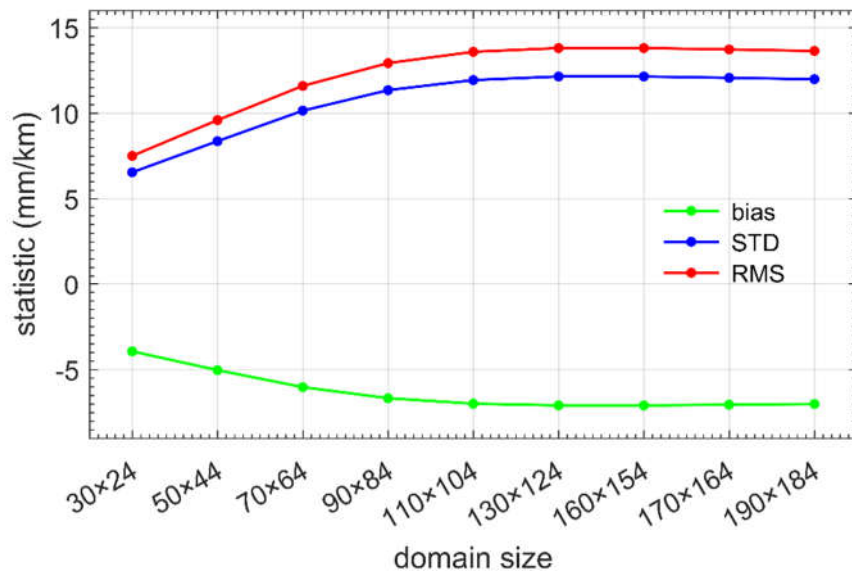
123 In this study, we use the Kain-Fritsch scheme (Kain and Frisch, 1990), WRF Single-Moment (WSM) 5-class  
 124 scheme (Hong et al., 2004) and Yonsei University PBL scheme (Hong et al., 2006), which are the same to Chien  
 125 et al. (2006). The other physical options include unified Noah land-surface model (Tewari et al., 2004), Revised

126 MM5 Monin-Obukhov scheme (Monin and Obukhov, 1954). The Rapid Radiative Transfer Model (Mlawer et  
 127 al., 1997) and Dudhia's scheme (Dudhia, 1989) are used for longwave radiation and shortwave radiation,  
 128 respectively.

129 **Table 1.** Physical parameterization schemes and statistics of bias, RMS, and STD of retrieved WR using  
 130 different schemes. Unit is mm/km.

	PBL physics	cumulus physics	microphysics	bias	STD	RMS
1	Yonsei University	Kain-Fritsch	WSM 5-class	-3.95	6.55	7.51
2	Yonsei University	Betts-Miller-Janjic	WSM 5-class	-3.95	6.55	7.51
3	Yonsei University	Grell-Freitas ensemble	WSM 5-class	-3.95	6.55	7.51
4	Yonsei University	Kain-Fritsch	Ferrier	-3.95	6.55	7.51
5	Yonsei University	Betts-Miller-Janjic	Ferrier	-3.95	6.55	7.51
6	Yonsei University	Grell-Freitas ensemble	Ferrier	-3.95	6.55	7.51
7	Mellor-Yamada-Janjic	Kain-Fritsch	WSM 5-class	-3.95	6.55	7.51
8	Mellor-Yamada-Janjic	Betts-Miller-Janjic	WSM 5-class	-3.95	6.55	7.51
9	Mellor-Yamada-Janjic	Grell-Freitas ensemble	WSM 5-class	-3.95	6.55	7.51
10	Mellor-Yamada-Janjic	Kain-Fritsch	Ferrier	-3.95	6.55	7.51
11	Mellor-Yamada-Janjic	Betts-Miller-Janjic	Ferrier	-3.95	6.55	7.51
12	Mellor-Yamada-Janjic	Grell-Freitas ensemble	Ferrier	-3.95	6.55	7.51

131 In order to figure out how sensitive the wet refractivity output is to the domain size, we carry out another  
 132 sensitive test at 00:00 UTC 22<sup>nd</sup> July in 2015. And we increase the domain size gradually from  $30 \times 24$  grids to  
 133  $190 \times 184$  grids. In each run, we validate the wet refractivity derived by the WRFDA output using the radiosonde  
 134 data. The statistical results of the sensitivity tests are shown in Figure 3. It shows that the smaller domain size  
 135 has the smaller bias, STD, and RMS. So, the domain size of the data assimilation experiment is set to  $30 \times 24$   
 136 grids which just cover the study area.



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138 **Figure 3.** WR Statistics of sensitive test of domain size validated by radiosonde data.

139 *3.2. GNSS tomography*

140 The limited number of stations, flat vertical distribution of stations, and bad satellite-station geometry impose  
 141 serious ill-posed problem in the WR tomography. To well handle this problem, we use the tomography method  
 142 proposed by Zhang et al. (2017). This method is based on the adaptive Laplacian smoothing and Helmert

143 Variance Component Estimation. It also uses the meteorological data from each GNSS station to constrain the  
 144 WR near the ground. This tomography strategy is free of a priori information, which makes it an independent  
 145 technique and thus ensures the fairness when the tomography technique is compared with the WRFDA model.  
 146 The WR can be retrieved directly by this tomography strategy when the SWDs are used as observations. The  
 147 troposphere is vertically divided into 13 layers with a constant thickness of 800 meters, and horizontally divided  
 148 into grids whose resolution is ~10 km in longitudinal direction and ~8 km in latitudinal direction. The  
 149 tomography algorithm is described as follows:

$$\left. \begin{aligned}
 \mathbf{Y} &= \mathbf{A}\mathbf{X} \\
 \mathbf{0} &= \mathbf{V}\mathbf{X} \\
 \mathbf{0} &= \mathbf{H}\mathbf{X} \\
 \mathbf{0} &= \mathbf{B}\mathbf{X} \\
 \mathbf{X}_m &= \mathbf{X}
 \end{aligned} \right\} \quad (3)$$

151 where the first equation is the observation equation,  $\mathbf{Y}$  is the vector of SWDs,  $\mathbf{A}$  is the design matrix  
 152 consisting of intercepts in each voxel,  $\mathbf{X}$  is the vector of WR in each voxel. The second to the forth  
 153 equations in Equation (3) are the vertical, horizontal, and boundary constraints. The fifth equation is used  
 154 to constrain the WR near the ground using the meteorological data at each GNSS station.  $\mathbf{V}$ ,  $\mathbf{H}$ , and  
 155  $\mathbf{B}$  are design matrix for constraint equations. The boundary constraints are established by setting the  
 156 WR in the top layer to 0. The vertical and horizontal constraints are established by Laplacian smoothing  
 157 in the vertical and horizontal directions, respectively. The Laplacian smoothing can be described as:

$$x_1 + x_2 + x_3 + x_4 - qx_0 = 0 \quad (4)$$

159 where the WR  $x_0$  equals the weighted average WR of its nearest four voxels in the same plane,  $q$  is  
 160 the smoothing factor.

161 In a least square scheme, the solution can be found by:

$$\mathbf{X} = (\mathbf{A}^T \mathbf{A} + \lambda_1 \mathbf{V}^T \mathbf{V} + \lambda_2 \mathbf{H}^T \mathbf{H} + \lambda_3 \mathbf{B}^T \mathbf{B} + \lambda_4) \cdot^{-1} (\mathbf{A}^T \mathbf{Y} + \lambda_4 \mathbf{X}_m) \quad (5)$$

163 Where  $\lambda_i$  ( $i = 1, 2, 3, 4$ ) are the weights of corresponding constraints.

164 In Zhang et al. (2017), the solution is found in an iterative feedback-update process, which is be simply  
 165 described as follows:

166 (a) Establish the initial constraints and initialize their weights as 1, namely  $\lambda_1 = \lambda_2 = 1$ ,  $\lambda_3$  is set to a large  
 167 value,  $\lambda_4$  is set to 1;  $\lambda_3$  and  $\lambda_4$  are not updated in the following run.

168 (b) Determine the values of  $\lambda_1$  and  $\lambda_2$  by Helmert Variance Component Estimation method and calculate  
 169 the tomography solutions by Equation (5);

170 (c) Update the smoothing factors by using the solutions in (b):

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$$q = \begin{cases} n & \text{if } x_0 < x_m \\ \frac{\sum_{i=1}^n x_i}{x_0} & \text{if } x_0 > x_m \end{cases} \quad (6)$$

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where  $n$  is the number of voxels used to calculate the weighted average.  $x_m$  is a threshold set to prevent updating the smoothing factor by inaccurate solutions. The initial value for  $x_m$  is half of the maximum wet refractivity in the solutions.  $x_m$  is updated by multiplying  $x_m$  by a scale factor, say 0.9, after each run until it is no larger than 3 times the mean square error of  $\mathbf{X}$ .

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(d) Use the new smoothing factors in (c) to update the horizontal and vertical constraints and redo (b) and (c) until the mean square error of the solution differences between this run and the previous run approaches a stable value. In practice, we set a threshold of 20 iterations which is enough to ensure a stable solution.

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#### 4 Results

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The radiosonde data are used to validate the WR derived from GNSS tomography, the Output1 and the Output2. Since the radiosonde launches at 0:00 and 12:00 UTC daily, the WR at these epochs are validated. Equation (1) is also used to calculate WR from radiosonde data. The vertical coordinates of the Output1 and the Output2 are converted to geopotential heights by NCAR Command Language (NCL) (UCAR/NCAR/CISL/VETS, 2013) and the geodetic heights of tomographic results are converted to normal height. The slight differences between geopotential heights and normal heights are neglected. We interpolate the Radiosonde to tomographic nodes since the former has a much higher resolution  $\sim 23$  layers from 0 to 10 km height than the latter (13 layers) and thus we can get a higher interpolation accuracy. We use a bilinear interpolation method in the horizontal domain and a linear interpolation method in the vertical direction. By these methods, we interpolate the WR derived from the Output1, the Output2 and radiosonde data to the tomography nodes. Finally, the WR are validated by the radiosonde data. For simplicity, WR from radiosonde data, and GNSS tomography are denoted as “Radiosonde”, and “Tomography” hereinafter.

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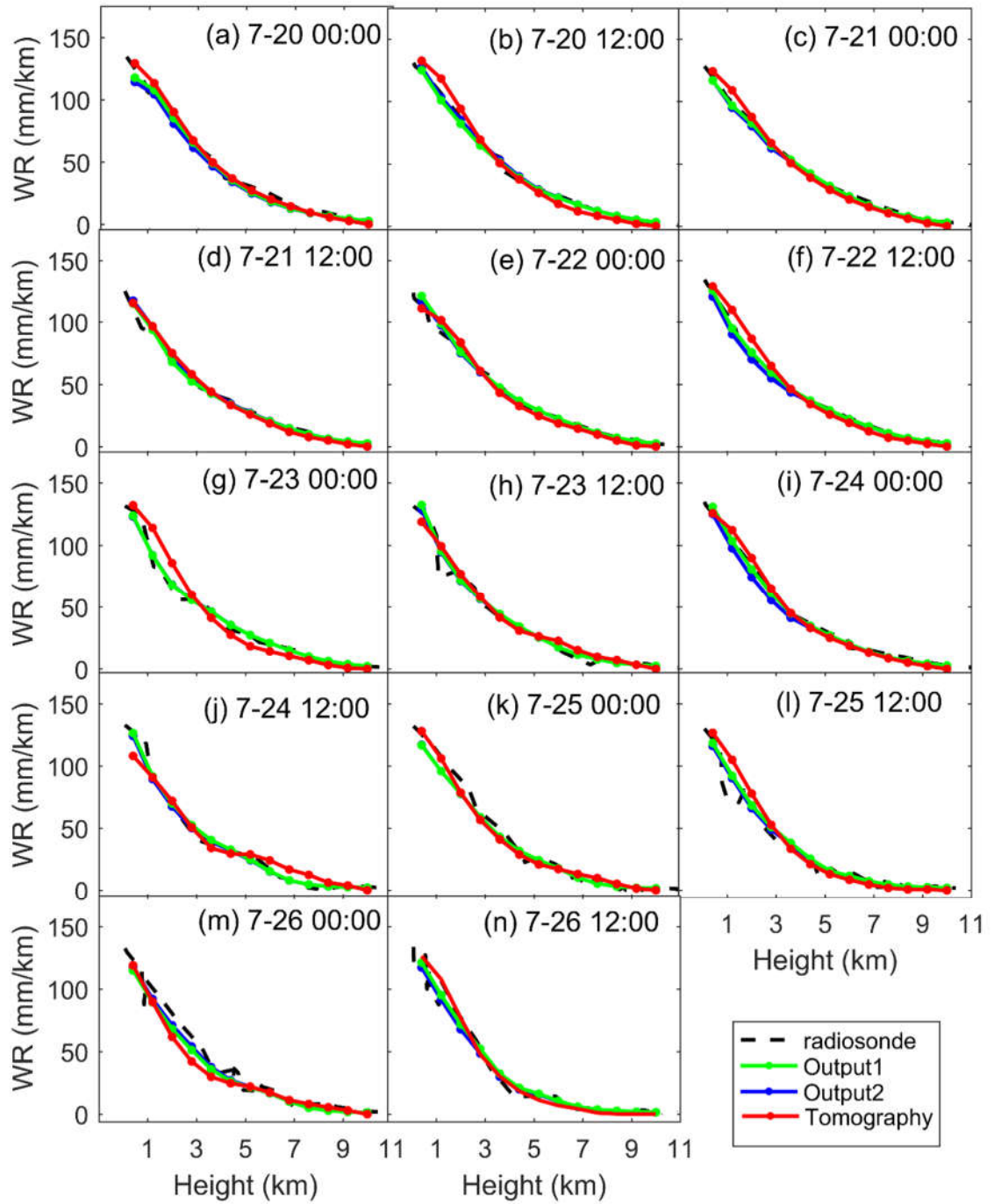
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Figures 4 and 5 show the vertical profiles of the Radiosonde, the Output1, the Output2 and the Tomography in the July and August periods, respectively. The Output1, the Output2, and the Tomography agree well with the Radiosonde, which indicates that these three methods successfully retrieved the vertical profile of the WR. It is also observed that the Output1, the Output2, and the Tomography agree better with the Radiosonde in the July period than in the August period. This difference should be due to the vertical distribution of WR. Though Hong Kong suffered heavy rain in the July period, the WR was more evenly distributed from 0 to 10 km height than that in the August period. In the dry August period, the WR was highly concentrated in the lower troposphere ( $< 6$  km) and its vertical changes were very sharp. This situation decreased the performance of the tomography technique and the data assimilation technique. This also indicate that the tomography technique has decreased capabilities in retrieving WR in highly changing troposphere. Compared with the Output2, the Output1 is slightly improved by reducing the mean absolute error (MAE) by 1.25 mm/km. The difference between the Tomography and the Output1 is obvious at some time epochs in the dry period (e.g., 12:00 on August 4 and 5).



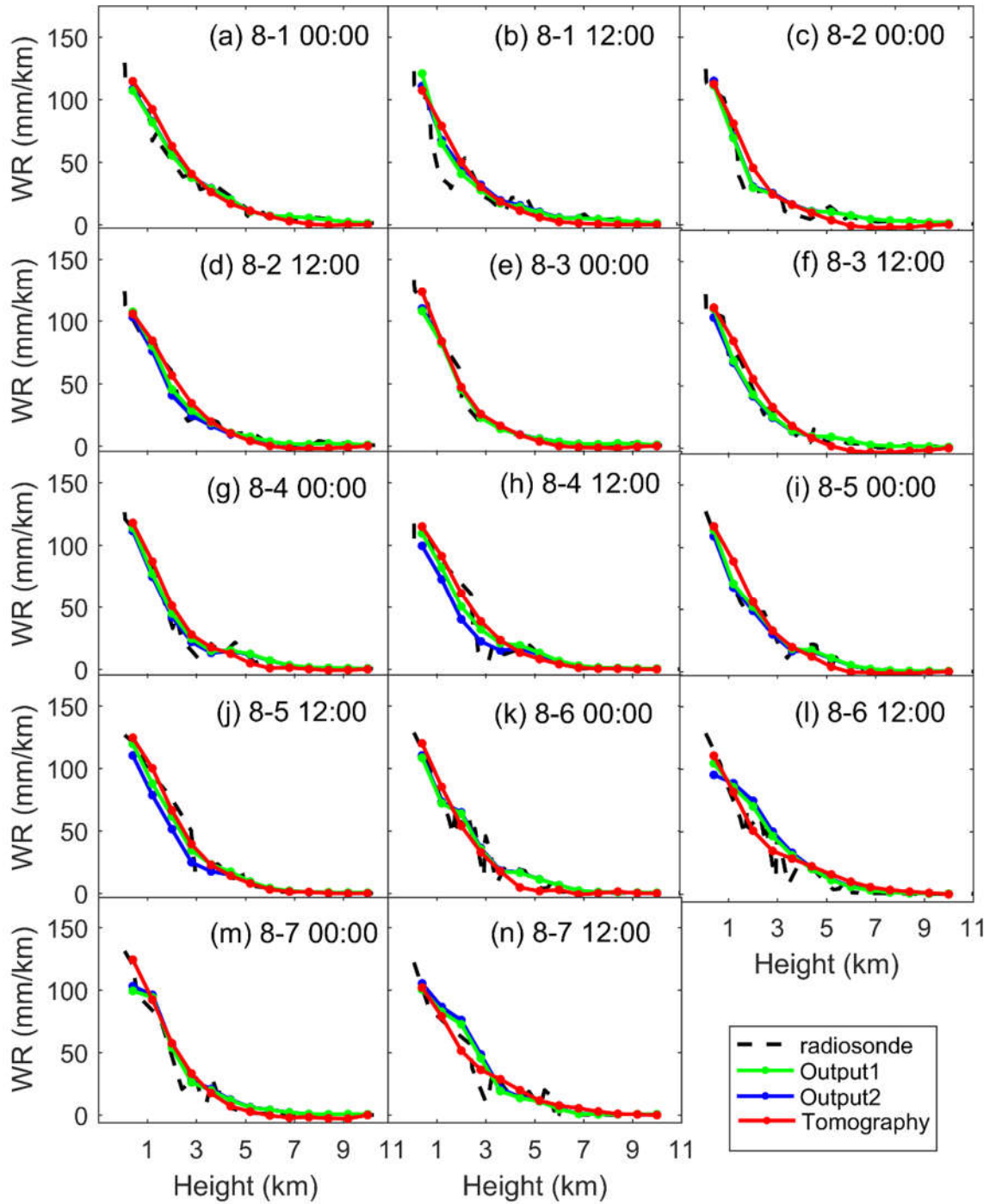
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**Figure 4.** Comparisons among WR derived from Output1, Output2, Tomography, and Radiosonde in the wet period, 2015.





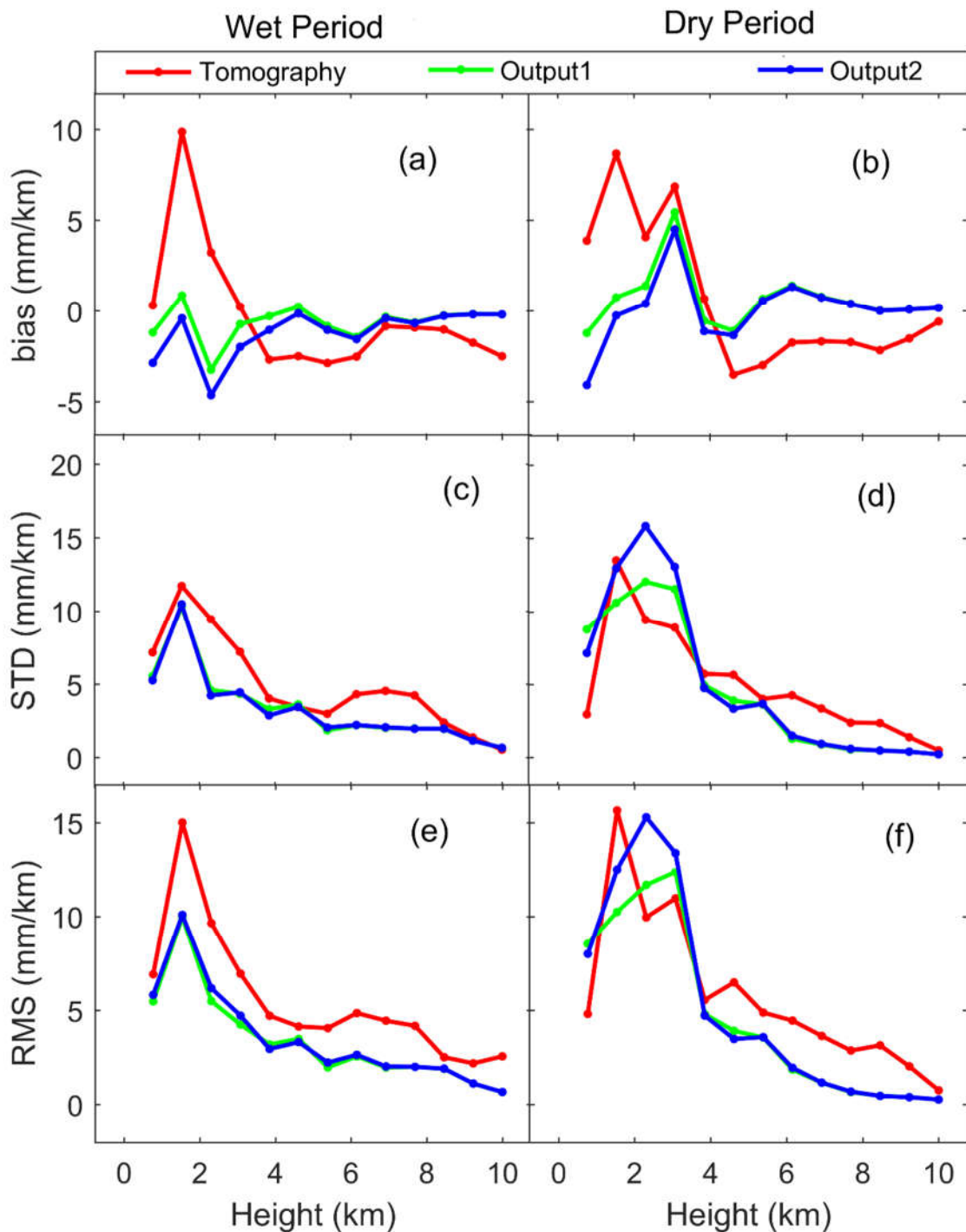
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208 **Figure 5.** Comparisons among WR derived from Output1, Output2, Tomography, and Radiosonde in the dry  
 209 period, 2015.

210 Figure 6 shows the statistics of the bias, STD, and RMS of the Tomography, the Output1, and the Output2  
 211 validated by the Radiosonde at different heights. In the wet period, bias of the Output1 is smaller than that of  
 212 the Output2, but the differences are not obvious in terms of STD and RMS. In the dry period, the bias of the  
 213 Output1 in the lower troposphere is slightly greater than that of the Output2. Overall, the differences between  
 214 the Output1 and the Output2 are not significant.

215 In the wet period, the bias, STD, and RMS of the Tomography are greater than that of the Output1 in most of  
 216 the time. But in the dry period, the STD and RMS of the Tomography tend to be smaller than that of the Output1  
 217 in the lower troposphere, but its bias is still greater. In general, the WRFDA performs better than the tomography

218 technique in most of the cases, but the RMS of Tomography validated by the Radiosonde in 400 m, 1600 m and  
 219 2400 m height is smaller than WRFDA output as shown in Figure 6f. So, in the lower troposphere in the dry  
 220 period the tomography performed better than the WRFDA in terms of RMS.



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222 **Figure 6.** Statistics of bias, STD, and RMS of Tomography, Output1, and Output2 validated by the Radiosonde.

223 Table 2 shows the bias, STD, and RMS of the Tomography, the Output1, and the Output2 validated by the  
 224 Radiosonde. In the whole troposphere in the wet period, the Tomography has the smallest bias but the largest  
 225 STD and RMS. The Output1 and the Output2 have the similar STD and RMS that are much smaller than that  
 226 of the Tomography. But the Output2 has the largest bias than the Output1 and the Tomography. In the lower  
 227 troposphere in the wet period, the Output1 has the smallest STD and RMS while the Tomography has the largest

228 ones. The bias of Tomography is positive in the low troposphere but negative in the upper troposphere, this  
 229 should be due to the vertical smoothing constraints imposed on the WR. In the upper troposphere in the wet  
 230 period, Tomography has the largest bias, STD, and RMS while the Output1 has the smallest ones. Overall, both  
 231 the tomography and the WRFDA results have larger bias, STD, and RMS in the lower troposphere than in the  
 232 upper troposphere, indicating both the tomography technique and the data assimilation technique has decreased  
 233 capabilities in the lower troposphere.

234 In the whole troposphere in the dry period, the Output2 has the smallest bias but the largest STD and RMS. The  
 235 STD and RMS of the Tomography are larger than the Output1. In the lower troposphere in the dry period, the  
 236 Output2 has the largest RMS and STD while the Output1 as the smallest ones. In the low troposphere in the dry  
 237 period, the performance of the Tomography is not as good as the Output1 in terms of RMS. However, in the  
 238 upper troposphere in the dry period, the Tomography has relatively larger bias, STD and RMS than the WRFDA  
 239 results.

240 **Table 2.** Statistics of bias, RMS and STD of Tomography, Output1 and Output2 validated by the  
 241 radiosonde WR. Unit is mm/km.

		Wet Period			Dry Period		
		bias	STD	RMS	bias	STD	RMS
Total	Output1	-0.64	4.11	4.15	0.63	6.34	6.35
	Output2	-1.19	4.15	4.31	0.10	7.28	7.26
	Tomography	-0.31	6.51	6.50	0.63	7.01	7.02
Low ( $< 5.6$ km)	Output1	-0.74	5.37	5.40	0.77	8.62	8.61
	Output2	-1.73	5.37	5.62	-0.19	9.90	9.85
	Tomography	0.80	8.20	8.19	2.52	8.83	9.13
Upper ( $\geq 5.6$ km)	Output1	-0.51	1.75	1.81	0.47	0.86	0.97
	Output2	-0.55	1.77	1.84	0.45	0.91	1.01
	Tomography	-1.60	3.26	3.62	-1.57	2.63	3.05

242 In general, assimilating GNSS ZTD into the WRFDA has slightly improved the WR retrieval by decreasing the  
 243 RMS by 0.2 mm/km. The WR derived from the Output1 and the Output2 has apparently smaller RMS than the  
 244 tomographic WR (4.15 mm/km vs. 6.50 mm/km and 4.31 mm/km vs. 6.50 mm/km, respectively). The results  
 245 obtained from WRFDA and tomography are better in the wet period than in the dry period, which is mainly due  
 246 to the sharp vertical variation of WR in the dry period.

## 247 5 Discussion

248 In the dry period, due to the sharp vertical variations of WR, the Tomography, the Output1 have decreased  
 249 performance in retrieving the WR, especially in the lower troposphere. Compared with the results in the wet  
 250 period, the RMS of the Tomography and the Output1 increases by 0.94 mm/km, 3.24 mm/km in the dry period,  
 251 respectively. The accuracy decrease is more significant in the Output1 than in the Tomography, resulting in that  
 252 the tomographic WR becomes better than the Output1 (Figures 6d and 6f) in the low troposphere.

253 When assimilating ZTD into the WRFDA, we only use the total water vapor and cannot use the vertical profile  
 254 of water vapor. This leads to that the assimilation of ZTD has limited improvement in retrieving the vertical

255 structure of the WR. Therefore, it is natural to consider assimilating the tomographic WR into the WRFDA to  
 256 improve the retrieval of the vertical structure of WR. At present, WRFDA could not assimilate WR directly,  
 257 but can assimilate meteorological parameters such as relative humidity, temperature and pressure. To assimilate  
 258 the tomographic WR, we convert WR to relative humidity.

259 The relationship between relative humidity ( $RH$ ) and  $P_w$  is shown as Equation (7).

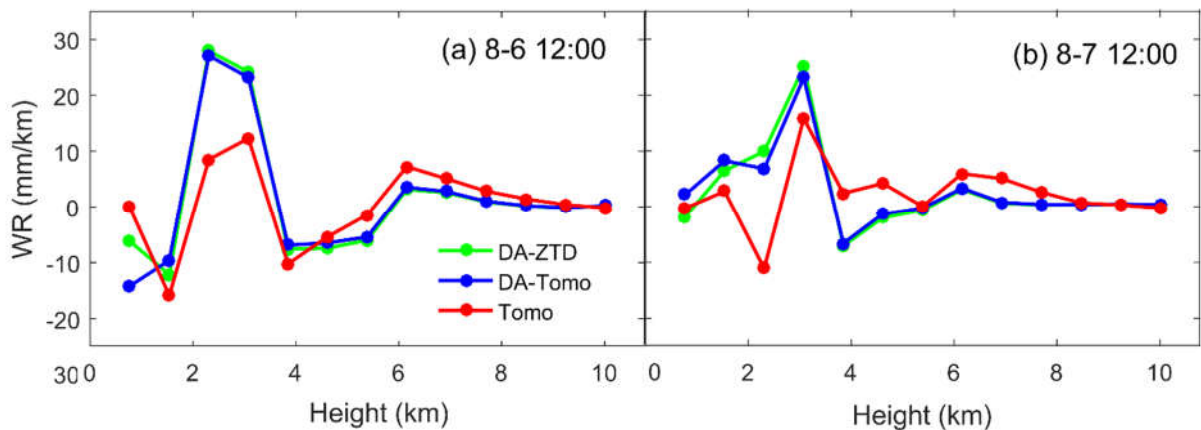
$$RH = \frac{P_w}{P_s} \quad (7)$$

260 where  $P_s$  is the saturated water vapor pressure which is related to temperature and can be calculated by Wexler  
 261 formula (Wexler, 1976,1977). The  $P_w$  is calculated by Equation (1). The needed temperature and pressure  
 262 data are from the Output2.

263 After converting the tomographic WR to  $RH$ , we assimilate the  $RH$  together with the corresponding temperature  
 264 and pressure into the WRFDA. Then, the similar procedures as described in Section 3.1 are performed to  
 265 generate new WRFDA output.

266 The Tomography agrees better with the Radiosonde than the Output1 and the Output2 in the lower troposphere  
 267 below 3 km at 12:00 on August 6 (Figure 5l) and at 12:00 on August 7 (Figure 5n). So, we assimilate the  
 268 tomographic WR below 3 km into the WRFDA at these two epochs. The generated output data are denoted as  
 269 “Output3”. The difference between Output3 and Radiosonde is denoted as “DA-Tomo”. The difference between  
 270 Output1 and Radiosonde is denoted as “DA-ZTD”. The difference between Tomography and Radiosonde  
 271 is denoted as “Tomo”. The MAE at different heights at 12:00 on August 6 and 7 are shown in Figure 7.

272



273

274

**Figure 7.** Differences between WR obtained by various methods and radiosonde WR.

275 Figure 7 shows that the DA-ZTD is very close to the DA-Tomo. The MAE of DA-ZTD is 6.04 mm/km and the  
 276 MAE of DA-Tomo is 5.92 mm/km. This indicates that assimilating tomographic WR into the WRFDA can  
 277 slightly improve the WR retrieve. But the large uncertainty (8.35 mm/km) of tomography WR in the lower  
 278 troposphere limit the improvement.

## 279 6 Conclusions

280 GNSS WR tomography and data assimilation experiments are conducted in Hong Kong during a wet and a dry  
 281 period to test the capabilities of the tomography technique and the WRFDA in retrieving WR. The results show

282 that both the tomography technique and the data assimilation technique can retrieve WR that agrees well with  
283 the radiosonde data.

284 In the wet period in the whole troposphere, the RMS of Tomography, the Output1 and the Output2 are 6.50  
285 mm/km, 4.31 mm/km, and 4.15 mm/km. The RMS becomes 7.02 mm/km, 6.35 mm/km, and 7.26 mm/km in  
286 the dry period. Both methods obtained better WR in the wet period than in the dry period. We infer that the  
287 sharp vertical variations of WR reduced the WR retrieving accuracy in the dry period. In most of the cases, the  
288 Output1 outperforms the tomographic WR but the tomographic WR is better than the Output1 in the lower  
289 troposphere in the dry period. By assimilating better tomographic WR in the lower troposphere into the WRFDA,  
290 we slightly improve the retrieved WR.

291 The above results suggest that both the WRFDA and the tomography technique can retrieve good WR but also  
292 have drawbacks. If we combine the two by assimilating good tomographic WR into the WRFDA, we may  
293 further improve the performance of the WRFDA in retrieving the water vapor field.

294

295 *Data availability.* All the data used in this paper are available upon request by email ([sggzb@whu.edu.cn](mailto:sggzb@whu.edu.cn)).

## 296 **Appendix A**

297 The GNSS observation data are processed by the precise point positioning module in Bernese 5.0 software  
298 using the same settings as detailed in Zhang et al. (2017). The International GNSS Service final orbit and clock  
299 products are used. The differential code Biases (DCB) is corrected by products from the Center for Orbit  
300 Determination in Europe. Antenna phase center offsets and variations, phase wind-up, Earth tides, Earth rotation,  
301 ocean tides and relativistic effects are corrected by conventional methods detailed in (Kouba and Héroux, 2001).  
302 We use the ionosphere-free combination of double frequencies to eliminate the first order ionospheric delay  
303 and the higher-order terms are ignored. The tropospheric delay models are Saastamoinen model (Saastamoinen,  
304 1972) and Niell mapping functions (Niell, 1996). The cut-off elevation angle is 10°. The station coordinates  
305 and ZTDs are estimated simultaneously. Accurate zenith hydrostatic delays (ZHD) are estimated by using the  
306 in-situ pressure observations and Saastamoinen model. The ZWD is estimated by removing the ZHDs from the  
307 corresponding ZTDs. The SWD is reconstructed by mapping the ZWD and horizontal gradients onto the ray  
308 direction. The phase residuals are added to SWD to consider the inhomogeneity of the troposphere.

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