## 1 Validation and application of optimal ionospheric shell height model

### 2 for single-site TEC estimation

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6

#### 7 Abstract

8 We recently proposed a method to establish optimal ionospheric shell height model 9 based on the international GNSS service (IGS) station data and the differential code 10 bias (DCB) provided by Center for Orbit Determination in Europe (CODE) during the 11 time from 2003 to 2013. This method is very promising for DCB and accurate total 12 electron content (TEC) estimation by comparing to traditional fixed shell height 13 method. However, this method is basically feasible only for IGS stations. In this study, 14 we investigate how to apply the optimal ionospheric shell height derived from IGS 15 station to non-IGS stations or isolated GNSS receivers. The intuitional and practical 16 method to estimate TEC of non-IGS stations is based on optimal ionospheric shell 17 height derived from nearby IGS stations. To validate this method, we selected two 18 dense networks of IGS stations located in US and Europe region. Two optimal 19 ionospheric shell height models are established by two reference stations, namely 20 GOLD and PTBB, which are located at the approximate center of two selected 21 regions. The predicted daily optimal ionospheric shell heights by the two models are

22	applied to other IGS stations around these two reference stations. Daily DCBs are
23	calculated according to these two optimal shell heights and compared to respective
24	DCBs released by CODE. The validation results of this method present that 1)
25	Optimal ionospheric shell height calculated by IGS stations can be applied to its
26	nearby non-IGS stations or isolated GNSS receivers for accurate TEC estimation. 2)
27	As the distance away from the reference IGS station becomes larger, the DCB
28	estimation error becomes larger. The relation between the DCB estimation error and
29	the distance is generally linear.
30	
31	Keyword
32	Ionospheric shell height, Single layer model (SLM), Differential code bias (DCB),
33	Total electron content (TEC)
34	
35	Introduction
36	Dual-frequency GPS signals propagation are affected effectively by ionospheric

dispersive characteristic. While, by taking advantage of this property, ionospheric TEC along the path of signal can be estimated by using differencing the pseudorange or carrier phase observations from dual-frequency GPS signals. Carrier phase leveling/smoothing of code measurement is widely adopted to improve the precision of absolute TEC observations (Mannucci et al., 1998; Horvath and Crozier, 2007). In general, it is considered that the derived TEC in carrier phase leveling/smoothing
technique consists of slant TEC (STEC), the combination differential code bias (DCB)
of satellite and receiver, multipath effects and noise. The DCB is usually considered
as the main error source and could be as large as several TECu (Lanyi and Roth, 1988;
Warnant 1997).

47 For TEC and DCB estimations, mapping function with single layer model (SLM) 48 assumption have been intensively studied for many years. Sovers and Fanselow (1987) 49 firstly simplified the ionosphere to a spherical shell. They set the bottom and the top 50 side of the ionospheric shell as h-35 and h+75 km, where h is taken to be 350 km 51 above the surface of the earth and allowed to be adjusted. In this model, the electron 52 density was evenly distributed in the vertical direction. Based on this model, Sardón et 53 al. (1994) introduced the Kalman filter method for real-time ionospheric VTEC 54 estimation, which can also be promising prediction of DCBs under adverse conditions 55 (antispoofing, ionospheric disturbances). Klobuchar (1987) assumed that STEC 56 equals VTEC multiplied by the approximation of the standard geometric mapping 57 function at the mean vertical height of 350 km along the path of STEC. Lanyi and 58 Roth (1988) further developed this model into a single thin-layer model, and proposed 59 the standard geometric mapping function and the polynomial model. The single 60 thin-layer model assumed that the ionosphere is simplified by a spherical thin shell with infinitesimal thickness. Clynch et al (1989) proposed a mapping function in the 61 62 form of a polynomial by assuming a homogeneous electron density shell between

63 altitudes of 200 and 600 km. Mannucci et al (1998) presented an elevation scaling mapping function derived from extended slab mode. There are also many modified 64 mapping function according to the standard geometric mapping function. Schaer 65 (1999) proposed the modified standard mapping function using a reduced zenith angle. 66 67 Rideout and Coster (2006) presented a new mapping function which replaces the 68 influence of the shell height by an adjustment parameter, and set the shell height as 69 450 km. Smith et al (2008) modified the standard mapping function by using a 70 complex factor. Based on the electron density field derived from the international 71 reference ionosphere (IRI), Zus et al (2017) recently developed an ionospheric 72 mapping function at fixed height of 450 km with dependence on time, location, 73 azimuth angle, elevation angle, and different frequencies.

74 Ionospheric shell height is considered to be the most important parameter for 75 mapping function, and the shell height is typically set to a fixed value between 350 76 and 450 km (Lanyi and Roth, 1988; Mannucci et al., 1998). Birch et al. (2002) 77 proposed an inverse method for estimate the shell height by using simultaneous 78 VTEC and STEC observations, and suggested the shell height is preferred to be a 79 value between 600 and 1200 km. Nava et al. (2007) utilized multiple stations to obtain 80 a shell height estimation method by minimizing the mapping function errors, this 81 method is referred as the "coinciding pierce point" technique. Their results indicated 82 that the suitable shell heights for the mid-latitude is 400 km and 500 km during the 83 geomagnetic undisturbed conditions and disturbed conditions, respectively. In the

84 case of the low-latitude, the shell height at about 400 km is suitable for both quiet and disturbed geomagnetic conditions. Jiang et al. (2018) applied this technique to 85 86 estimate the optimal shell height for different latitude bands. In their case, the optimal 87 layer height is about 350 km for the entire globe. Brunini et al. (2011) studied the 88 influence of the shell height by using an empirical model of the ionosphere, and 89 pointed out that a unique shell height for whole region does not exist. Li et al. (2018) 90 applied a new determination method of the shell height based on the combined IGS 91 GIMs and the two methods mentioned above to the Chinese region, and indicated that 92 the optimal shell height in China ranges from 450 to 550 km. Wang et al. (2016) 93 studied the shell height for grid-based algorithm by analyzing goodness of fit for 94 STEC. Lu et al. (2017) applied this method to different VTEC models, and 95 investigated the optimal shell heights at solar maximum and at solar minimum. 96 In the recent study by Zhao and Zhou (2018), a method to establish optimal 97 ionospheric shell height model for single station VTEC estimation has been proposed. 98 This method calculates the optimal ionospheric shell height with regards to minimize 99  $|\Delta DCB|$  by comparing to the DCB released by CODE. Five optimal ionospheric shell 100 height models were established by the proposed method based on the data of five IGS 101 stations at different latitudes and the corresponding DCBs provided by CODE during 102 the time 2003 to 2013. For the five selected IGS stations, the results have shown that 103 the optimal ionospheric shell height models improve the accuracies of DCB and TEC

104 estimation comparing to fixed ionospheric shell height of 400 km in a statistical sense.

We also found that the optimal ionospheric shell height show 11-year and 1-year periods and is related to the solar activity, which indicated the connection of the optimal shell height with ionospheric physics.

108 While the proposed optimal ionospheric shell height model is promising for 109 DCB and TEC estimation, this method also can be implemented to isolated GNSS 110 receivers not belonging to IGS stations, if we can get the long-term observations and 111 reference values of DCB from the isolated GNSS receivers. The purpose of this study 112 is to investigate the application of the optimal ionospheric shell height derived from 113 IGS station to non-IGS stations. By considering the spatial correlation of ionospheric 114 electron density, it is intuitive and practical to adopt the optimal ionospheric shell 115 height of a nearby IGS station for the non-IGS stations.

The purpose of this study is to investigate the feasibility of applying the optimal ionospheric shell height derived from IGS station to nearby non-IGS GNSS receivers for accurate TEC/DCB estimation. By selecting two different regions in U.S. and Europe with dense IGS stations, we calculate the daily DCBs of 2014 by using the optimal ionospheric shell heights derived from 2003-2013 data of two central stations in two regions. We also try to find the DCB estimation error and its relation to distance away from the central reference station.

123

124 Method

125 In (Zhao and Zhou, 2018), we proposed a concept of optimal ionospheric shell height 126 for accurate TEC and DCB estimation. Based on daily data of single site, this approach searches daily optimal ionospheric shell height, which minimizes the 127 128 difference between the DCBs calculated by VTEC model for single site and reference values of DCB. For a single site, its long-term daily optimal ionospheric shell heights 129 130 can be estimated and then modeled. In our case, the polynomial model (Wild, 1994; 131 Komjathy, 1997) is applied to estimate satellite and receiver DCBs, and the DCBs 132 provided by CODE are used as the reference.

In the polynomial model, the VTEC is considered as a Taylor series expansion inlatitude and solar hour angle, which is expressed as follows:

135 
$$T_{V}(\varphi, S) = \sum_{i=0}^{m} \sum_{j=0}^{n} E_{ij}(\varphi - \varphi_{0})^{i} (S - S_{0})^{j}$$
(1)

where  $T_V$  denotes VTEC.  $\varphi$  and S denote the geographic latitude and the solar 136 hour angle of ionospheric pierce point (IPP), respectively;  $\varphi_0$  and  $S_0$  denote  $\varphi$ 137 and S at regional center.  $E_{ij}$  is the model coefficient. m and n denote the 138 139 orders of the model. A polynomial model fits the VTEC over a period of time. In our 140 case, a VTEC model is generated over 3 hours of time, therefore 8 VTEC models are 141 applied per day. DCB is considered as constant in one day. Since our analysis is based 142 on long-term single site data, we set m and n to 4 and 3, respectively. Huang and 143 Yuan (2014) applied the polynomial model with the same orders to TEC estimation.

Based on the thin shell approximation, the observation equation can be writtenas:

146 
$$T_{os}^{PRN}(\varphi, S) = T_V(\varphi, S) \cdot f(z) + DCB^{PRN}$$
(2)

147 where  $T_{os}^{PRN}$  is slant TEC calculated by carrier phase smoothing, the superscript *PRN* 148 denotes GPS satellite.  $DCB^{PRN}$  denotes the combination of GPS satellite and 149 receiver DCB. *z* denotes the zenith angle of IPP. According to Lanyi and Roth (1988), 150 the standard geometric mapping function f(z) is expressed as follows:

151 
$$f(z) = 1/\cos(z)$$
(3)

152 
$$z = \arcsin\frac{\operatorname{Re} \cdot \cos El}{\operatorname{Re} + h}$$
(4)

where Re denotes the earth's radius, El denotes the elevation angle, and h denotes the thin ionospheric shell height. Note that h also affects the location of IPP.

To estimate DCBs, The method above requires a definite thin shell height value. Conversely, if we get the daily solutions of DCBs, the optimal ionospheric shell height can be estimated. The optimal ionospheric shell height is assumed to be between 100 and 1000 km and is defined as the shell height with the minimum difference between  $DCB^{PRN}$  and the reference values. This optimization problem can be written as:

161 
$$\min_{100 < h < 1000} mean(|\mathbf{DCB}_{ref} - \mathbf{DCB}|) \text{ s.t. } \mathbf{T} = \mathbf{\Phi} \cdot \mathbf{E} + \mathbf{\theta} \cdot \mathbf{DCB}$$
(5)

162 where *h* is the daily optimal ionospheric shell height,  $\mathbf{DCB}_{ref}$  denotes the vector of 163 the reference values of DCBs, s.t. is the abbreviation for subject to,  $\mathbf{T} = \mathbf{\Phi} \cdot \mathbf{E} + \mathbf{\theta} \cdot \mathbf{DCB}$  is the matrix form of all the observation equations in one day, **T** denotes the vector of  $T_{os}$ , **E** corresponds to the coefficients of the models, **DCB** is the vector of  $DCB^{PRN}$ ,  $\mathbf{\Phi}$  and  $\mathbf{\theta}$  are the coefficient matrix of **E** and **DCB**, respectively. After the method above is applied to 11-year data, the estimated optimal ionospheric shell heights can be modeled by a Fourier series, which is expressed as follows:

171 
$$h(x) = a_0 + \sum_{n=1}^{k} \left( a_n \cos \frac{2n\pi x}{L} + b_n \sin \frac{2n\pi x}{L} \right)$$
(6)

172 where k is the order of Fourier series and is set to 40,  $a_n$  and  $b_n$  are the model 173 coefficients, x is the time, and L is the time span which equals to 4018 days. The 174 maximum frequency of model is 40/L $\approx$ 0.01 per day, which corresponds to a period 175 of 100 days. By least square method, the model coefficients can be estimated.

This model can be applied to neighboring stations' DCB estimation. Instead of fixed shell height, this model provide predicted optimal ionospheric shell height. While in the establishment and application of the model, the VTEC model, mapping function and elevation cut-off angle can't change. Both of them affect the optimal ionospheric shell height.

181

### 182 **Experiment and Results**

The previous section introduced a method to establish daily optimal ionospheric shell height model based on single site with reference values of DCBs. To analyze the improvement of DCB estimation by this model for the reference station and other neighboring stations, we present two experiments to evaluate and validate this method by using IGS stations located in U.S. and Europe region. To ensure the accuracy and 188 consistency of DCB, we only select IGS stations with pseudorange measurements of189 P1 code, and whose receiver DCBs have been published by CODE.

190 Figure 1 presents the location and distribution of the selected IGS stations in two 191 regions. Table 1 presents the information of the geographical location, distance to reference station in each region and receiver types of all stations. Based on the 192 193 RINEX data of GOLD station in Region I and PTBB station in Region II during the 194 period of 2003-2013, two separate optimal ionospheric shell height models for each 195 region are established by the aforementioned method. Then the model are applied to 196 DCB estimation in 2014 for all the other stations in each region. Note that reference 197 GOLD and PTBB stations are marked with black triangle in the figure. The other 198 neighboring stations are located in different orientations of GOLD and PTBB with 199 different distances, which range from 136 to 1159 km for region I and range from 200 190.82 to 1712.27 km for region II. In the table, the receiver type is corresponding to 201 2003~2014 for GOLD and PTBB, and 2014 for the other stations. In region I, the 202 receiver type of GOLD has been changed once in September 2011. The five selected 203 stations used four receiver types in 2014; TABV and PIE1 had the same receiver type. 204 In region II, there are nine receiver types for the sixteen stations. The receiver type of 205 PTBB has changed twice in 2006.



**Fig.1** Geographical location of the selected IGS stations in U.S. region (Region I) and

209 Europe region (Region II). The black triangle in each plot is the reference station.

## **Table 1** Information for the stations

			Distance		
Nomo	Latitude	Longitude	to GOLD	Dessiver type and convise data	muiaa data
Ivanie	(deg)	(deg)	or PTBB	Receiver type and service date	
			(km)		
	35.42	-116.89	0	ASHTECH Z-XII3 ~ 2011-09-14	
GOLD				JPS EGGDT 2011-09-19 ~	
TABV	34.38	-117.68	136.67	JAVAD TRE_G3TH DELTA	

QUIN	39.97	-120.94	619.55	ASHTECH UZ-12
PIE1	34.30	-108.12	810.51	JAVAD TRE_G3TH DELTA
AMC2	38.80	-104.52	1159.09	ASHTECH Z-XII3T
				SEPT POLARX2 2006-07-25~
PTBB	52.15	10.30	0	2006-11-13
				ASHTECH Z-XII3T else
POTS	52.38	13.07	190.82	JAVAD TRE_G3TH DELTA
WSRT	52.91	6.60	264.92	AOA SNR-12 ACT
WTZA	49.14	12.88	381.28	ASHTECH Z-XII3T
WTZS	49.14	12.88	381.28	SEPT POLARX2
WTZZ	49.14	12.88	381.28	JAVAD TRE_G3TH DELTA
GOPE	49.91	14.79	401.51	TPS NETG3
BRUX	50.80	4.36	439.03	SEPT POLARX4TR
ONSA	57.40	11.93	593.72	JPS E_GGD
ZIMJ	46.88	7.47	620.79	JAVAD TRE_G3TH DELTA
SPT0	57.72	12.89	641.78	JAVAD TRE_G3TH DELTA
OPMT	48.84	2.33	674.24	ASHTECH Z-XII3T
HERS	50.87	0.34	705.38	SEPT POLARX3ETR
IENG	45.02	7.64	816.64	ASHTECH Z-XII3T
VILL	40.44	-3.95	1696.62	SEPT POLARX4
MADR	40.43	-4.25	1712.27	JAVAD TRE_G3TH DELTA

Figure 2 presents the estimated daily optimal ionospheric shell height of GOLD and PTBB during the period from 2003 to 2013. The left panel shows the variation of the daily optimal ionospheric shell height and the fitting result by (6). From the overall trend, the variations of daily optimal ionospheric shell height for both two

stations appear wave-like oscillation during the 11 years period. In the right panel, the statistical result are fitted by a normal distribution. The mean and the standard deviation (STD) of the normal distribution are 714.3 and 185.4 km for GOLD, respectively. The mean and STD value for PTBB is 416.4 and 184.1 km, respectively. At the end of 2010, a gap appears, for the DCB provided by CODE is simultaneously anomalous (Zhao and Zhou, 2018), and the data during this period are abandoned.





Fig.2 Variation of the daily optimal ionospheric shell height (black) and the fittingresult (red)

225

Figure 3 presents the amplitude spectra of the daily optimal ionospheric shell height of two reference stations estimated by the Lomb-Scargle analysis (Lomb, 1976; Scargle, 1982). As can be found in Figure 3, the peaks correspond to 11-year, 1-year, 6-month and 4-month cycles. The amplitudes of 11-year and 1-year cycles are more evident than other periods in both two stations. Note that the frequencies above 0.01
per day are discarded because of their small amplitudes. As mentioned earlier, 0.01
per day is about the maximum frequency of (6). This result shows that the optimal
ionospheric shell height of GOLD and PTBB is periodic, and the 40th-order of
Fourier series is suitable for modelling its variation.

238



240 **Fig.3** Lomb-Scargle spectra of the daily optimal ionospheric shell height

241

We establish two optimal ionospheric shell height models for each region by the 40th-order of Fourier series based on the 11-year data of GOLD and PTBB. To investigate the availability zone of the optimal ionospheric shell height model, we apply the model to the stations of each region as shown in Figure 1 and Table 1. Based on the predicted daily optimal ionospheric shell heights in 2014 calculated by the model of GOLD and PTBB, the DCBs in all stations of each region are estimated in the form of single station by the polynomial model mentioned earlier. The difference of DCBs in all station in each region calculated by the optimal ionospheric shell height model from each reference station and DCBs provided by CODE is then compared to the difference of DCBs calculated by fixed ionospheric shell height (400 km) and DCBs released by CODE.

253 The results of this comparison are shown in Figure 4. The panels for the stations 254 are arranged by their distances to reference station, this is also applied to the 255 following table; from the top panels to the bottom panels, the distance of the 256 corresponding station to the reference station gradually increases. The left and right 257 panels show the daily differences and the histograms of the statistical results in 2014, 258 respectively. For all of the stations, the daily average differences of DCBs calculated 259 by the optimal ionospheric shell height model are reduced compared to the fixed 260 ionospheric shell height. For GOLD and TABV, the reductions are appropriate, the 261 daily average  $\Delta DCBs$  around zero have the most days. For the other stations, the 262 reductions are so much that most of the average  $\Delta DCBs$  are negative. This result 263 shows the improvement of the model seems to be related with the distance to GOLD. 264 Data gap on the figure correspond to days when data from that station are not 265 available. Figure 5 is the same format as Figure 4, which presents the results of 266 Region II. By comparing to the results of fixed ionospheric height, Figure 5 also indicates that the  $\Delta DCB$  calculated by using optimal ionospheric shell heights of 267 PTBB prediction is statistically less than that calculated by using fixed ionospheric 268

shell height. Both Figure 4 and Figure 5 present that the accuracy of DCB estimation





273 Fig.4 Comparisons of the average  $\Delta DCB$  calculated by the predicted optimal

- 274 ionospheric shell heights (red dots) and by the fixed ionospheric shell height (black
- dots) in 2014 for stations in Region I.

277



**Fig.5** Comparisons of the average  $\Delta DCB$  calculated by the predicted optimal ionospheric shell heights (red dots) and by the fixed ionospheric shell height (black

283	Table 2 presents the quantitative statistical results of average $\Delta DCB$ in 2014. For
284	all the stations in each region, the mean values and the root mean squares (RMS) by
285	the optimal ionospheric shell height model are smaller than by the fixed ionospheric
286	height. For Region I, the improvements of TABV are the most significant. Their mean
287	values are reduced to 0.12 and 0.08 TECu, respectively; the root mean squares are
288	reduced by 4.43 and 4.33 TECu, respectively. For Region II, the improvement for
289	DCB estimation are the most obvious for WTZZ, with mean value of $\Delta$ DCB decreases
290	from 2.34 to 0.02. We could note that TABV and WTZZ station are quite close to the
291	reference stations in each region.

292

# **Table 2** Statistical results of mean (ΔDCB) in 2014

	Average $\Delta D$	CB (TECu)	Average $\triangle DCB$ (TECu)	
Station	Optimal Ionos	pheric Height	Fixed Ionospheric Height	
	Mean	RMS	Mean	RMS
GOLD	0.12	1.82	5.96	6.25
TABV	0.08	2.04	6.06	6.37
QUIN	-1.60	2.31	3.91	4.19
PIE1	-1.38	2.50	4.46	4.84
AMC2	-2.12	2.75	3.09	3.53
PTBB	-0.28	1.23	1.82	2.26
POTS	-0.27	1.00	1.84	2.18

WSRT	-0.41	1.14	1.65	2.10
WTZA	0.09	1.20	2.38	2.73
WTZS	0.14	0.99	2.48	2.76
WTZZ	0.02	1.14	2.34	2.65
GOPE	-0.17	1.00	2.12	2.41
BRUX	-0.42	1.12	1.86	2.13
ONSA	-0.88	1.40	1.10	1.63
ZIMJ	0.48	1.17	2.87	3.13
SPT0	-0.84	1.40	1.14	1.67
OPMT	-0.29	1.21	1.93	2.35
HERS	-0.37	1.19	1.84	2.19
IENG	1.05	1.57	3.44	3.69
VILL	0.59	1.67	3.30	3.66
MADR	0.66	1.71	3.50	3.86

295 Figure 6 and Figure 7 present the relation between the statistical results of 296 average  $\triangle DCB$  and the distance to reference stations in each region. The left and the 297 right panels in each figure show the relation of the absolute mean value and the root 298 mean square with the distance to GOLD and PTBB, respectively. For all of the 299 stations, the optimal ionospheric shell height model improves the accuracies of DCB 300 estimation compared to the fixed ionospheric shell height in a statistical sense; both of the absolute mean values and the root mean squares become smaller. For the optimal 301 302 ionospheric shell height model, the absolute mean values present a positive 303 correlation with the distance to reference station GOLD and PTBB in each region, as

304	well as the root mean squares. By using the linear regression, for Region I, the
305	absolute mean value increases at a rate of about 1.84 TECu per 1000 km and start at
306	about 0.05 TECu. The RMS value increases at a rate of about 0.75 TECu per 1000 km
307	and starts at about 1.87 TECu. According to the fitting results, the absolute mean
308	value and the RMS less than 1 TECu and 2.25 TECu in the region around GOLD with
309	a radius of 500 km, and less than 2 TECu and 2.62 TECu for the region with a radius
310	of 1000 km. For Region II, the absolute mean value increases at a rate of about 0.30
311	TECu per 1000 km and start at about 0.25 TECu. The RMS value increases at a rate
312	of about 0.41 TECu per 1000 km and starts at about 1.01 TECu. According to the
313	fitting results, the absolute mean value and the RMS less than about 0.40 TECu and
314	1.21 TECu in the region around PTBB with a radius of 500 km, and less than about
315	0.55 TECu and 1.42 TECu for the region with a radius of 1000 km. For the two
316	regions, the RMSs presents stronger linear relation with distance comparing to the
317	means.





321 red lines are the linear fitting results

322

323



325 Fig.7 Relation of the accuracy for DCB estimation with the distance to PTBB. The

326 red lines are the linear fitting results

327

#### 329 Summary

In this study, we investigate the implementation and validation of optimal ionospheric shell height derived from IGS station to non-IGS station or isolated GNSS receiver. We establish two optimal ionospheric shell height models by the 40th-order of Fourier series based on the data of IGS station GOLD and PTBB in two separate regions These two models are applied to the stations in each region, where the distance to GOLD ranges from 136.67 to 1159.09 km and the distance to PTBB ranges from 190.82 to 1712.27 km. The main findings are summarized as follows:

The optimal ionospheric shell height model improves the accuracy of DCB
 estimation comparing to the fixed shell height for all of the stations in a statistical
 sense. This results indicate the feasibility of applying the optimal ionospheric shell
 height derived from IGS station to other neighboring stations. The IGS station can
 calculate and predict the daily optimal ionospheric shell height, and then release
 this value to the nearby non-IGS stations or isolated GNSS receivers.

2) For other station in each region, the error of DCB by the optimal ionospheric shell height increases linearly with the distance to the reference GOLD and PTBB station. For the mean and the RMS of the daily average  $\Delta$ DCBs, in region I, the slopes are about 1.84 and 0.75 TECu per 1000 km; in region II, the slopes are about 0.30 and 0.41 TECu per 1000 km. This results indicate the horizontal spatial correlation of regional ionospheric electron density distribution. For different region, the error at 0 km (i.e. the error for the reference station) is different, which 350 should be also considered.

As the requirement of this experiment, we just analyze two regions in mid-latitude due to the insufficiency of long-term P1 data. We also ignore the orientation of isolated GPS receivers to the reference station.

354

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360

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