Quarterdiurnal signature in sporadic E occurrence rates and comparison with neutral wind shear

by Christoph Jacobi, Christina Arras, Christoph Geißler, and Friederike Lilienthal

Response to the reviewer’s comments

Reviewer #1

We are thankful for the referee’s comments which helped us to considerably improve the paper. We addressed the raised issues in the revised version, and also corrected the technical points addressed. In response to the specific points, we will repeat each one here in italics and provide a reply below:

1. P-4, Line. 12-13: Authors mentioned that “slightly above 100 km”. Actually, it is mostly below 100 km.

Response: We agree that our statement is only true for higher latitudes. We corrected that in the revised version.

2. P-7, Line. 11-12: “Due to this sampling irrespective of longitude, only migrating components contribute to the diurnal cycle in our analyses”. It is not clear why only migrating components contribute.

Response: The phases of nonmigrating tides at different longitudes are different, so that the nonmigrating components average out if one averages over longitudes. We mention this in the revised version.

3. Figure 1a: In northern winter high OR near 15 latitude around 98 km is evident. What is the reason for that? What is the reason for equinoctial asymmetry in OR during SON while it is very symmetric during MAM?

Response: OR maximize in summer, but are also found in the winter hemisphere at low latitudes. Our Figure 1a is in accordance with climatologies, e.g. in Arras et al. 2008. Actually the winter low-latitude maximum is also seen in the SH winter, but the values are lower because of the South Atlantic anomaly, where the Es OR are low. Regarding the MAM and SON distribution, they are both not really symmetric about the equator, but the shapes of the respective NH and SH maximums during one season are different. On the other hand, during both SON and MAM the autumn as well as the respective spring distributions look similar regarding their shape. The SON SH values are lower than the MAM NH due to the South Atlantic anomaly. Interestingly, the MAM SH values are larger than the SON NH values which might be due to a hotspot over Indonesia and Australia, which is visible in the global distribution e.g. by Arras et al 2008. We detailed this in the revised version.
4. Figure 2: Only winter is shown. Results of all 4 seasons could be shown in order to be complete and consistent with Figure 1.

Response: The figure is mainly shown to visualize the analysis, not to describe the diurnal wind shear. Actually, the QDT component is hardly visibly in the left panel of figure 1, and this is also the case for the other seasons so that plotting all of these figures would not give more insight into the QDT behaviour. We added and discussed, however, the summer wind and wind shear, because there the situation is different, when the positive mean wind shear in most cases dominate over the tidal shear.

5. Figure 4: Only a single representative altitude (110 km) is shown. More altitude bins (3 or more) could be included to strengthen the claim of the authors.

Response: We selected 101 km because this is a MUAM level which is close to the maximum Es OR height. The lat/lon zonal wind amplitude distribution does not change much with altitude so that plotting the other height does not provide too much relevant information, also having in mind that not the wind amplitude but the wind shear amplitude is the important parameter. However, we added some more figures in the appendix (Figs. A1-A3) to the revised version.

6. Figure 6: There is a clear inconsistency in the QDT phase between the occurrence rate and wind shear in summer when QDT is found to be weak as mentioned by the authors. It implies that the estimated phases in the wind shear in summer are incorrect. Authors should substantiate the statement in detail.

Response: We apologise for describing this inadequately. Es and wind shear phases agree within their error bars even during summer. Actually, however, this is to a certain degree unexpected, because both Es and wind shear TDT are not significant. We now describe this more correctly and in more detail.

7. Figure 7: Only 110 km altitude is selected. At least 3 more altitude bins could be shown to corroborate the inference.

Response: We show the vertical structure in Figure 8, so that we think more heights than 101 km in Figure 7 are not absolutely necessary. However, we added more figures in the appendix (Figs. A4-A6).

The technical points have been carefully addressed.

Reviewer #2

Thank you very much for your very positive opinion. Negative wind shear means that the vertical gradient of the considered horizontal wind component (either zonal or meridional, but we do not analyze the meridional one here) is negative, i.e. dU/du < 0 for negative zonal wind shear. We added this information in the revised version.
Quarterdiurnal signature in sporadic E occurrence rates and comparison with neutral wind shear

Christoph Jacobi\textsuperscript{1}, Christina Arras\textsuperscript{2}, Christoph Geißler\textsuperscript{1}, and Friederike Lilienthal\textsuperscript{1}

\textsuperscript{1}Institute for Meteorology, Universität Leipzig, Stephanstr. 3, 04103 Leipzig, Germany
\textsuperscript{2}Helmholtz Centre Potsdam German Research Centre for Geosciences - GFZ, Section 1.1: Space Geodetic Techniques, Telegrafenberg, 14473 Potsdam, Germany

\textbf{Correspondence:} Ch. Jacobi (jacobi@uni-leipzig.de)

\textbf{Abstract.} The GPS radio occultation (RO) technique is used to study sporadic E (\textit{E}_S) layer plasma irregularities of the Earth’s ionosphere on a global scale using GPS signal-to-noise ratio (SNR) profiles from the COSMIC/FORMOSAT-3 satellite. The maximum deviation from the mean SNR can be attributed to the height of the \textit{E}_S layer. \textit{E}_S are generally accepted to be produced by ion convergence due to vertical wind shear in the presence of a horizontal component of the Earth magnetic field, while the wind shear is provided mainly by the solar tides. Here we present analyses of quarterdiurnal \textit{tide} (QDT) signatures in \textit{E}_S occurrence rates. \textbf{We find from} a local comparison with mesosphere/lower thermosphere wind shear obtained with a meteor radar at Collm (51.3°N, 13.0°E), \textbf{we find} that the phases of the QDT in \textit{E}_S agree well with those of negative \textit{wind shear vertical shear of the zonal wind} for all seasons except for summer, when the QDT amplitudes are small. We also compare the global QDT \textit{E}_S signal with numerical model results. The global distribution of \textit{the} \textit{E}_S occurrence rates qualitatively agrees with the modeled zonal wind shears. The results indicate that zonal wind shear is indeed an important driving mechanism for the QDT seen in \textit{E}_S.

1 Introduction

In the lower \textit{E} region of the ionosphere, thin layers of high electron density are frequently found, the so called lower ionospheric sporadic \textit{E} (\textit{E}_S) layers. \textit{E}_S layers are thin clouds of accumulated plasma, which occur primarily at \textit{middle latitudes} and maximize during summer (e.g., Arras et al., 2008). They are generally formed at altitudes between 90 km and 120 km, i.e. in the lower thermosphere/lower ionospheric \textit{E} region. According to the wind shear theory (Whitehead, 1961) the process of \textit{E}_S formation is \textbf{an metallic ion convergence owing to the} interaction between the Earth’s magnetic field, the metallic ion concentration, and the vertical \textit{wind shear gradient of the horizontal neutral wind}. ‘\textit{Wind shear}’ in brief. Neglecting diffusion, the vertical velocity component of the neutral gas, and the electric force, the vertical ion drift \( w_I \) may be written as (e.g., Haldoupis, 2012; Fytterer et al., 2014; Oikonomou et al., 2014):

\[
\begin{align*}
  w_I &= \frac{r \cdot \cos I}{1 + r^2} U + \frac{\cos I \sin I}{1 + r^2} V, \\
  &\quad \text{where } U \text{ and } V \text{ are the zonal and meridional wind components of the neutral gas pointing towards } \textit{east and the east and the north}, \text{ resp., while } I \text{ is the inclination of the Earth’s magnetic field. The parameter } r = \nu/\omega \text{ describes the ratio of the ion-neutral}.
\end{align*}
\]
gas collision frequency $\nu$ and the gyro frequency $\omega = eB_0/m_I$, with $e$ as the elementary charge, $B_0$ as the total intensity of the Earth’s magnetic field, and $m_I$ as the ion mass. Note that in Eq. (1), in contrast to the usual notations in the literature, Cartesian coordinates are used. Given that $r \gg 1$ below 115 km (Bishop and Earle, 2003), in the lower E region the zonal wind component is more efficient in causing vertical plasma motion than the meridional wind component. Consequently, the second term of (1) becomes small at these heights, and therefore negative vertical zonal wind shear primarily leads to, i.e., a negative vertical gradient of the zonal horizontal wind, is primarily responsible for the formation of $E_S$. Note that Eq. (1) holds only for magnetic midlatitudes (about $20^\circ$ - $70^\circ$), where electric forces can be neglected.

General correspondence between wind shear and $E_S$ had been found, e.g. from comparison using winds from the Horizontal Wind Model (Chu et al., 2014). Recently, Shinagawa et al. (2017) calculated the global distribution of the vertical ion convergence based on GAIA Earth system model simulations and showed that their global distribution is roughly consistent with $E_S$ occurrence rates (OR). Liu et al. (2018) found correspondence between $E_S$ OR taken from Global Positioning System (GPS) radio occultation (RO) data and wind shear calculated from the TIMED/TIDI satellite-borne zonal winds.

The dynamics of the upper mesosphere and lower thermosphere are strongly influenced by atmospheric waves (e.g. Yiğit and Medvedev, 2015), including the solar tides with periods of a solar day, and its harmonics. Their wind amplitudes usually maximize around or above 120 km. In these regions, the tidal amplitudes are of the order of magnitude of the mean wind. Shorter period waves often have smaller amplitudes, so that the main diurnal variability is owing to the diurnal tide (DT) and the semidiurnal tide (SDT), and also, to a lesser degree, to the terdiurnal tide (TDT). The quarterdiurnal tide (QDT), although it also forms an integral part of the middle and upper atmosphere dynamics, has attained much less attention, mainly due to its smaller amplitude. Assuming that solar tides are a major source of the vertical wind shear, frequently providing and they frequently provide larger vertical gradients - both negative and positive depending on local time - than the background wind. Therefore, tide-like structures are expected in $E_S$ occurrence rates. Actually, the SDT and DT are generally accepted to be the major driver of $E_S$ (Mathews, 1998), leading to the reproduction of downward moving tidal signatures visible, e.g., in $E_S$ ionosonde registrations (Haldoupis et al., 2006; Haldoupis, 2012, e.g.). By combining GPS $E_S$ registrations and radar wind measurements at midlatitudes, Arras et al. (2009) have shown that middle latitudes, Arras et al. (2009) showed that the $E_S$ occurrence frequencies in the course of one day actually maximize when the zonal wind shear provided by the SDT is negative. Modeling by Resende et al. (2018b) showed the connection of between $E_S$ and tides, although they focused in the equatorial region, where electric field effects become important. More recently, Fytterer et al. (2013) found a clear correlation between midlatitude radar zonal wind shear and $E_S$ for the 8-hr component also. Fytterer et al. (2014) showed correspondence between the QDT-TDT in $E_S$ and the wind shear on a global scale. Thus, Fytterer et al. (2013, 2014) confirmed that not only DT and SDT, but TDT wind shear as well contributes to $E_S$ formation.

There remains the question about the role of the QDT in the formation of $E_S$, and a possible connection with the QDT neutral wind shear at midlatitudes. Some publications report that no QDT signature was found in some ionospheric records (e.g., Cyprus, 35°N, 33°E, Oikonomou et al., 2014). However, 6-hr tidal signatures were observed in lower ionospheric $E_S$ parameters already (Tong et al., 1988; Morton et al., 1993). For the neutral atmosphere,
observations of the QDT in barographic records (e.g. Warburton and Goodkind, 1977; Hupe et al., 2018) have been reported, and some reports on observations from mesosphere and lower thermosphere (MLT) radars are available (Smith et al., 2004; Liu et al., 2006; Jacobi et al., 2017, 2018; Guharay et al., 2018). Few attempts to numerically model the QDT have been undertaken (Smith et al., 2004; Jacobi et al., 2018). On a global scale, the 6-hr harmonics of ozone heating rates were calculated from Aura/MLS satellite observations by Xu et al. (2012), who noted that the main 6-hr forcing during solstice is in the winter hemisphere. Xu et al. (2014) analysed nonmigrating tides from TIMED/SABER observations. In a further study, Liu et al. (2015), again using TIMED/SABER data, analysed the migrating QDT between 50°S and 50°N in the middle atmosphere. Azeem et al. (2016) analyzed temperature data from the NIRS instrument on the International Space Station and from SABER during June and July 2010, and found that the QDT was a significant dynamical feature in the thermosphere. The seasonal/latitudinal structure of the QDT is complex; generally, the seasonal cycle exhibits a maximum in winter and also during equinoxes. Regarding the latitudinal distribution, several maxima were observed and modeled (Smith et al., 2004; Liu et al., 2015; Azeem et al., 2016). The latitudinal structure is dominated by the (4,6) Hough mode, but other modes are also present (Liu et al., 2015).

Returning to $E_S$, their 6-hr component has not yet been analysed in detail using GPS RO observations, which motivates us to search for the QDT signature in $E_S$ OR derived from RO, and compare them with local wind shear observations and global model predictions. Therefore, in this paper we analyse the quarterdiurnal oscillation seen in $E_S$, obtained from GPS RO measurements by the FORMOSa SATellite mission-3/Constellation Observing System for Meteorology, Ionosphere and Climate (FORMOSAT-3/COSMIC). We compare $E_S$ phases with phases of negative wind shear obtained from the local radar observations at Collm (51.3°N, 13.0°E), and compare the global distribution of 6-hour amplitudes $E_S$ with the wind shear amplitudes from numerical modeling. The remainder of the paper is organised as follows. In section 2 the $E_S$ detection and the radar wind observations are briefly described, and the numerical global circulation model is introduced. Results of QDT analysis and comparison with wind shear observations and modeling are presented in section 3. Section 4 concludes the paper.

2 Dataset and model description

2.1 Sporadic E occurrence rates

The FORMOSAT-3/COSMIC constellation consists of six low-Earth orbiting (LEO) microsatellites which orbit the Earth at an initial altitude of 800 km. The satellites perform RO measurement in both the neutral atmosphere and the ionosphere (Anthes et al., 2008). During an occultation, signals of rising or setting GPS satellites are received by a LEO satellite. While the signals pass the Earth’s atmosphere they are modified by the atmospheric conditions, in particular the ionospheric electron density, causing which causes refraction and degradation of the GPS waves, which can be utilized to obtain information about the ionosphere and the neutral atmosphere. More detailed information on the principles of the RO technique is given by Hajj et al. (2002) and Kursinski et al. (1997).
The method to derive $E_S$ information from RO signals has been described in Arras and Wickert (2018). In brief, for our investigations, the Signal-to-Noise ratio (SNR) profiles of the GPS L1 phase measurements are used. The SNR is very sensitive to vertical variations of the electron density, and these occur within an $E_S$ layer. These vertically localized electron density variations lead to phase fluctuations of the GPS signal, which can be observed as changes of the received signal strength (Hajj et al., 2002). In order to avoid influences from the different basic signal power values on the further data analysis, every SNR profile is normalized first. In the case of absence of ionospheric disturbances the SNR value is almost constant at altitudes above 35 km. The SNR standard deviation profile is considered to be disturbed when it exceeds an empirically found threshold of 0.2. If large standard deviation values are concentrated within a thin layer of less than 10 km vertical extent, we assume that the respective SNR profile includes the signature of an $E_S$ layer. The height where the SNR value deviates most from the mean of the respective SNR profile is considered as the altitude of the $E_S$ layer. This has been validated by comparisons with ionosonde $E_S$ observations (Arras and Wickert, 2018; Resende et al., 2018a).

Figure 1 shows 2007-2016 mean zonal mean $E_S$ OR. OR have been calculated as the number of $E_S$ within a 5° latitude and 10 km height window, divided by the number of RO in the respective latitude window. Figure 1 shows seasonal mean OR for December–February (DJF), March–May (MAM), June–August (JJA) and September–November (SON). The distributions are similar to those shown by Fytterer et al. (2014) obtained from a more limited dataset. Maximum OR are found at altitudes slightly below 100 km for low latitudes, but above 100 km for middle to high latitudes except for autumn. OR maximize in summer, which is thought to be owing to increased meteor influx during that season (Haldoupis et al., 2007). The summer maximum is more pronounced in the Northern Hemisphere, which is due to the South Atlantic Anomaly and the weaker magnetic field there (e.g., Arras et al., 2008; Chu et al., 2014; Arras and Wickert, 2018), so that Southern Hemisphere summer zonal mean OR are smaller than Northern Hemisphere ones. Near the equator, $E_S$ OR are small, owing to the horizontal magnetic field at the magnetic equator, which does not allow the electrons to follow the vertically moving ions (e.g., Arras et al., 2008, 2010; Arras and Wickert, 2018).

Although OR maximize in summer, they are also found in the winter hemisphere at low latitudes. The winter low-latitude maximum is well visible in the NH hemisphere. It is also seen in the SH winter, but the OR values are lower, again because of the South Atlantic anomaly, where the $E_S$ OR are low, which leads so generally lower OR in the SH compared with the NH. Regarding the MAM and SON distribution, they are both not really symmetric about the equator, but the shapes of the respective NH and SH distributions are different during one season. On the other hand, during both seasons the spring as well as the respective autumn distributions look similar regarding their shape. The SON SH values are lower than the MAM NH values due to the South Atlantic anomaly. Interestingly, the MAM SH values are larger than their counterparts in the SON NH, which might be due to an $E_S$ hotspot over Indonesia and especially Australia, which is visible in the global distribution, e.g., presented by Arras et al. (2008).
2.2 Collm mesosphere/lower thermosphere wind shear

At Collm (51.3°N, 13.0°E), a SKiYMET meteor radar is operated on 36.2 MHz since summer 2004. The radar operates in an all-sky configuration, and the main parameter observed are the MLT radial winds determined from the Doppler shift of individual meteor trails. Details of the radar system and the radial wind determination principle can be found in Jacobi (2012), Stober et al. (2012), and Lilienthal and Jacobi (2015). During 2015 the radar had been upgraded by increasing the peak power, and replacing the Yagi antennas by crossed dipoles. The transmit frequency is still the same (Stober et al., 2017). The individual meteor trail reflection heights vary between about 75 and 110 km, with a maximum meteor count rate at an altitude slightly below 90 km (e.g., Stober et al., 2008). The data are binned here in 6 different not overlapping height gates centered at 82, 85, 88, 91, 94, and 98 km. The hourly mean reflection height may slightly deviate from the nominal heights due to the uneven height distribution of meteors within each gate (Jacobi, 2012). Individual radial winds calculated from the meteors are collected to form hourly mean values of horizontal winds using a least squares fit of the horizontal wind components to the raw data under the assumption that vertical winds are small (Hocking et al., 2001). Hourly values of the vertical shear of zonal wind (subsequently ‘zonal wind shear’ in brief) have been zonal wind shear are calculated from adjacent height gates as in Arras et al. (2009) and Fytterer et al. (2013), and the reference height for shear values has been attributed to the center between the nominal heights of the wind values.

An example, except for the upper height gate where the real mean height is close to 97 km so that the uppermost wind shear level is placed at 95.5 km.

Two examples for the diurnal zonal wind and wind shear variation in the MLT over Collm are shown in Figure 2. On the left panels, height-time cross-sections of 2007 - 2016 mean DJF (a) DJF and (c) JJA mean diurnal zonal winds and wind shears $S(t)$ over Collm are shown. Maximum In winter, maximum wind values exceed 70 (50) ms$^{-1}$ in eastward (westward) direction, while the zonal wind shear maximizes at more than $\pm 8\sim 8(\pm 6)$ ms$^{-1}$km$^{-1}$, similar to the values shown by Arras et al. (2009). We note that during two time intervals during one day, strong negative wind shear is prevailing, which according to the wind shear theory supports $E_S$ formation. During summer (Figure 2c), the background wind shear is strongly negative and only at the upper height gate short time intervals of negative wind shear occur. Therefore, at altitudes below $\sim 93$ km, $E_S$ formation is much less supported by the mean wind distribution, which is consistent with the greater mean $E_S$ heights in summer than in winter at middle latitudes (see Figure 1).

Clearly, the main contribution to zonal wind and wind shear variability in particular winter is due to the SDT. On the right panel and partly DT. To visualize the higher frequency wind shear variations, on the right panels of Figure 2, the diurnal zonal wind shear values $S(t)$ at 92.5 km are shown for (b) DJF and (d) JJA, together with a modeled least-squares fit including $S_{Mod}(t)$ including diurnal mean $S_0$, as well as 8 hr, 12 hr, and 24 hr components:

$$S_{Mod}(t) = S_0 + \sum_{i=1}^{3} a_i \sin \frac{2\pi}{P_i} t + b_i \cos \frac{2\pi}{P_i} t,$$

(2)
with $t$ as the time and $P_i$ as the above mentioned periods, and the coefficients $a_i$ and $b_i$ being determined through minimizing $\sum (S(t) - S_{\text{Mod}}(t))^2$. The amplitudes $A_i$ and phases $T_i$ of the wind shear are calculated as

$$A_i = \sqrt{a_i^2 + b_i^2}, \quad T_i = \frac{P_i}{2\pi} \arctan \frac{a_i}{b_i} + \frac{P_i}{2}.$$ (3)

Note that the phases are defined here as the time of maximum negative wind shear, so that a $P_i/2$ - term is added to the right part of (3). The residuals $S(t) - S_{\text{Mod}}(t)$, multiplied by a factor of 5 for better visibility, are added as blue line on the right panel panels of Figure 2. Obviously, there is a quarterdiurnal signature during this season winter (Figure 2b) and at this altitude level. Amplitudes and phases of this variation are calculated via a least-squares fit similar to Eqs. (2) and (3) but in addition including the QDT period $P_4 = 6$ hr in the analysis.

**Figure** In contrast to winter, there is no significant 6-hr component of the wind shear visible during summer (Figure 2d), which is consistent with small QDT amplitudes in summer as was shown by (Jacobi et al., 2017).

**Figure** 3 shows the 2007 - 2016 mean seasonal mean Collm residual zonal wind shear after removing mean shear, the mean shear and the 8 hr, 12 hr, and 24 hr components for (a) DJF, (b) MAM, (c) JJA, and (d) SON. 6-hr phases, defined as the time of maximum negative wind shear according to Eq. (3), are added. The QDT at Collm is relatively strong in winter, but very weak in summer (Jacobi et al., 2017) and insignificant in summer, and consequently as in Figure 2d the 6-hr signal is not visible for JJA. For the other seasons the QDT shear tends to increase with altitude, although in MAM the QDT signal is not the major one at the upper height gate. In SON, the QDT seasonal means consist of a superposition of summer, transition, and winter oscillations (see Jacobi et al., 2017, their Figures 3 and 6). As a consequence, at the upper height gates a clear QDT signature is visible, but these are not connected with the QDT at the lower heights, also leading to a break in the vertical phase change.

### 2.3 MUAM circulation model predictions

We use the nonlinear Middle and Upper Atmosphere Model (MUAM) to investigate the QDT with wavenumber 4. MUAM is a 3-dimensional mechanistic primitive equation model based on the COMMA-LIM (Fröhlich et al., 2003b; Jacobi et al., 2006) model. The more recent version of the model, MUAM, is documented by Pogoreltsev (2007), Pogoreltsev et al. (2007), and Lilienthal et al. (2017, 2018). MUAM extends from the surface (1000 hPa) to the lower thermosphere while the lower 30 km zonal mean temperatures are nudged with monthly mean 2000-2010 mean ERA-Interim reanalyses of zonal mean temperature. This ensures that the zonal mean dynamics of the lower atmosphere is close to the reanalyses, while waves are allowed to form anyway. The model has a horizontal resolution of $5 \times 5.625^\circ$ and a vertical resolution of 2.842 km in logarithmic pressure height coordinates with a constant scale height of $H = 7$ km. Parameterizations of gravity waves, solar, of solar and infrared radiation, as well as of several ionospheric effects are included. The latter, however, are only represented based on simple empirical distributions.

The parameterization of solar:

Solar heating in the middle atmosphere is calculated parameterized following Strobel (1978). This considers heating due to the most important gases such as $H_2O$, $CO_2$, ozone, $O_2$, and $N_2$. Note that these gases are taken as zonal means, different from
other versions of MUAM (e.g., Suvorova and Pogoreltsev, 2011; Ermakova et al., 2017), so that mainly migrating tides are forced through the solar heating. Monthly mean zonal mean ozone fields up to 50 km altitude are taken from the Stratosphere- troposphere Processes And their Role in Climate project (SPARC; Randel and Wu, 2007), and an exponential decrease of ozone is applied above 50 km. Monthly volume mixing ratios for \( CO_2 \) have been chosen according to measurements from Mauna Loa Observatory for the year 2005 (e.g., 378 ppm for January; NOAA ESRL Global Monitoring Division), and the mixing ratio is assumed constant across latitudes and longitudes. \( CO_2 \) values are taken as constant with height until 87.5 km, and then decrease exponentially. Chemical heating due to recombination of \( O_2 \) and \( O \) (Riese et al., 1994), and heating due to extreme ultraviolet radiation are added. This is described in more detail by Fröhlich et al. (2003a).

Gravity waves in the middle atmosphere are calculated by a linear Lindzen-type (Lindzen, 1981) parameterization based on Jakobs et al. (1986) and updated as described by Fröhlich et al. (2003a, b) and Jacobi et al. (2006). Due to the fact that this parameterization does not account for gravity waves in the thermosphere, it is coupled with a modified parameterization after Yiğit et al. (2008). Yiğit et al. (2008, 2009), and both parameterizations are connected via the eddy diffusion coefficient. To avoid large interactions between both parameterizations, we limit the phase speeds of the Lindzen-type scheme to 5 – 30 ms\(^{-1}\), while the Yiğit-scheme covers larger phase speeds between 35 – 105 ms\(^{-1}\). This way, the Yiğit parameterization mainly attributes the thermosphere while the Lindzen-type parameterization affects the stratosphere and mesosphere. Overlaps between both parameterizations are small and the contributions of both routines to the tendency terms can be simply summed up (Lilienthal et al., 2018).

In the configuration used here, the model incorporates a spin-up of 120 model days. Within that time, the heating rates are zonally averaged and are therefore building up a background climatology without any tidal forcing. Note that we do not explicitly excite any kind of waves at the lower boundary during the whole simulation. In the following 90 model days, the heating rates are allowed to be zonally variable, and, through their diurnal variability, tides start to propagate. In this model version, the sun’s zenith angle does not account for day-to-day variations and refers is kept fixed to the middle of the respective month. The last 30 model days are analyzed and the results of tidal analysis are presented here. Since there is no change of any forcing, the day-to-day variability is negligible, negligibly small.

Figure 4 shows the annual cycle of the simulated monthly 6-hr zonal wind amplitudes at 101 – 101 km altitude. The, which is close to the height of maximum \( E_S \) OR, QDT amplitudes for other model heights are shown in the Appendix. The QDT zonal wind amplitudes are larger in winter than in summer, with winter maximums which have also been observed (Jacobi et al., 2017). Winter maximums are seen at higher and middle latitudes, which have also been observed (Jacobi et al., 2017) and is also predicted by Smith et al. (2004). Winter QDT amplitudes in both hemispheres tend to maximize in early and late winter, with a relative minimum during solstice. There is also a tendency for the spring maximum at midlatitudes as that was reported by Jacobi et al. (2017). We also note maximums at 30 - 40°, as has been reported by Liu et al. (2015). Note that, since the solar forcing is parameterized using zonal mean climatologies of minor species, the MUAM amplitudes only show migrating components, while the radar observations only deliver the total amplitude. However, from amplitude and phase comparisons between two stations, Jacobi et al. (2017) concluded that the major contribution to the QDT observed by radar is
mainly due to the migrating tide, and comparison between model results and radar is justified.

3 Results

3.1 Local comparison of 6-hr radar wind shear and $E_S$ occurrence rates

Here, we compare the diurnal cycle of $E_S$ OR at the latitude of Collm with the wind shear observed by the MR with respect to the QDT signature, similar to the approach of Arras et al. (2009) and Fytterer et al. (2013) for the 12 and 8 hr component, respectively. Similar as in Figure 1, OR have been calculated as the number of $E_S$ divided by the number of RO, but here a latitude window of 10° centered at 51°N was chosen, and the data were sampled in hourly bins according to local time. Due to this sampling, the phases of nonmigrating tides at different longitudes are different, so that the nonmigrating components average out if we sample irrespective of longitude, only migrating and therefore effectively average over longitudes. Therefore, only the migrating tidal components contribute to the diurnal cycle in our analyses. As in Figure 1, the data refer to 10 km height gates. The diurnal cycles for four seasons are shown in Figure 5. We note the downward propagation of $E_S$ OR signatures, which are dominated by the SDT and, to a lesser degree, by a diurnal variation (see, e.g., Arras et al., 2009). The strongest amplitudes are seen in summer, while minimum amplitudes are found in winter, which is owing to the overall seasonal cycle of OR at higher midlatitudes, see Figure 1.

The residuals of $E_S$ OR after removing daily mean, 8 hr, 12 hr, and 24 hr components, i.e. calculated in the same manner as the wind shear residuals in Figure 3, are shown in Figure 6. The QDT phases are calculated according to the right part of Eq. (3), but without the $P_4/2$-term, since we are interested in maximums of the times of maximum $E_S$. Zonal The zonal wind shear phases taken from shown in Figure 3 are also shown added in the lower parts of the respective panels of Figure 6. Again, solid symbols indicate that the amplitudes are significant at the 5% level according to a t-test. The QDT in $E_S$ is strongest in summer, as are the overall OR (see Figure 5). Vertical phase gradients in summer are large, but smaller in winter and autumn, which is also the case with the QDT in neutral winds (Smith et al., 2004; Jacobi et al., 2017). In autumn, significant QDT amplitudes are only found in a small height range at 95 - 100 km. Generally, the QDT in $E_S$ disappears below 90 - 95 km. Except for summer, there is a clear correspondence between In all seasons, negative wind shear phases and $E_S$ phases agree within their standard deviations in the upper two radar height gates, i.e. above 90 km. This indicates is also the case in summer, although both wind shear and $E_S$ amplitudes are not significant then. This indicates that the QDT in $E_S$ actually forms at the nodes of the negative QDT wind shear component, and Therefore the $E_S$ formation process, which is responsible for the strong 12 hr-component in $E_S$, also acts for the much weaker QDT.
3.2 Global distribution of 6-hr wind shear and $E_S$ occurrence rates

The $E_S$ QDT amplitudes are not necessarily directly related to the respective wind shear amplitudes, because $E_S$ intensities and OR depend on wind shear, but also on the ionization of metallic ions, and the latter are thought to exhibit a seasonal cycle owing to the variability of meteor influx (Haldoupis et al., 2007). Therefore, e.g., at midlatitudes, at middle latitudes the largest $E_S$ OR amplitudes are found in summer (see Figure 6), while the largest QDT in the neutral wind is seen during winter (Figures 3 and 4). Further, wind shear theory includes the influence of the horizontal magnetic field leading to a latitudinal dependence of $E_S$ OR, as well as to anomalies like the South Atlantic Anomaly. To take this into account when showing the global distribution of $E_S$ QDT amplitudes, following Fytterer et al. (2014) we calculated relative amplitudes $A_{4,r} = A_4/OR$. We show their global distribution at an altitude of 101 km in Figure 7a. The zonal wind shear QDT at the nearest model level at 100.9 km height, calculated from MUAM monthly simulations is shown in Figure 7b. Both parameters show a corresponding maximum in the winter higher midlatitudes hemispheremiddle latitudes in both hemispheres. In the Southern Hemisphere, the QDT in both $E_S$ and wind shear is small during boreal winter. In the Northern Hemisphere summer, a further QDT maximum in $E_S$ is found, which is, however, only very weakly represented in the wind shear. During the equinoxes, again corresponding maximums are found at lower and middle latitudes, especially on the Northern Hemisphere. Overall, there is a striking similarity between $E_S$ and wind shear QDT, in particular taking into account that the wind shear here is not taken from observations, but from numerical modeling with tides being forced self-consistently and not based on observed distributions.

Figure 8 shows on the left column seasonal mean relative $E_S$ amplitudes as latitude-height plots, while the corresponding modeled QDT shear amplitudes are presented on the right column. We show values only between 90 and 110 km, because below and above the OR become small (Figures 1 and 5), and therefore the $A_{4,r}$ distribution tends to become more irregular. There is an overall close correspondence between $E_S$ and wind shear during the solstices (panels a,b and e,f). Wind shear amplitudes then are large on the middle to high latitude winter hemisphere, with large values down to the upper mesosphere, while corresponding $E_S$ amplitudes are large there, too. A secondary maximum in the lower thermosphere winter near 30° is also seen in both $E_S$ and wind shear. In JJA, there is also a qualitatively corresponding maximum on the summer hemisphere.

This is also visible in the DJF wind shear, however, only very weakly expressed in DJF $E_S$. During boreal spring (panels b, c), there are corresponding maximums in $E_S$ and wind shear QDT at higher midlatitudes, maximizing peaking at 60°S and at 45 - 60°N, and. There is also an indication for a joint maximum close to the equator. The latter, however, is probably coincidental, since the wind shear theory according to Eq. (1) does not hold for magnetic latitudes below about 20°. There is a modeled QDT wind shear maximum near 30°S during MAM, which is not visible in $E_S$, similar to the situation during austral spring (panels g,f). Generally, the correspondence between wind shear and $E_S$ QDT is weakest during SON. This may partly be due to the seasonal cycle and the fact that seasonal averages are taken from monthly data that may be very different (e.g., a clear minimum/maximum in September/November at higher northern midlatitudes, see Figure 7). Also, the overall correspondence between $E_S$ and wind shear QDT mainly refers to the position of maximums and minimums, while the absolute values may differ. Still, however, there is a correspondence visible between the global distribution of the QDT in $E_S$ and the one seen in
wind shear, indicating the presence of the wind shear mechanism also for the QDT.

4 Conclusions

We have analyzed the migrating QDT amplitudes and phases from $E_S$ OR obtained from GPS RO observations. Comparing the $E_S$ phases with those from wind shear observed by radar over a midlatitude site shows a clear correspondence, indicating that the wind shear mechanism is indeed an important source for the $E_S$ QDT. Note, however, that we have compared the local QDT phases with the migrating signal from $E_S$, and although the migrating QDT is the dominating one at the latitude of the observations, a future analysis will have to consider this in detail, and also analyze the nonmigrating components from the $E_S$ QDT. Wind shear and $E_S$ QDT phase gradients are smaller in winter than in summer, indicating shorter QDT wavelengths in summer than in winter, which is in agreement with observations (Smith et al., 2004; Jacobi et al., 2017). However, as long as the amplitudes do not increase exponentially, phase gradients also include the effect of amplitude change, and Therefore, wavelengths cannot be derived from the shear phases directly, so that the global $E_S$ OR will not provide the neutral atmosphere wavelengths, but only deliver a qualitative measure.

Amplitudes of tidal signatures in $E_S$ are not only determined by the wind shear, but also depend on the metallic ion concentration and Earth’s magnetic field parameters, so that a correlation of between $E_S$ and wind shear is possible only for a defined region, and for each season separately. Comparing the amplitude distributions on a global scale was possible by dividing the $E_S$ amplitudes by the background OR, which will take out most of the seasonal and regional dependencies of $E_S$ OR. Indeed, the global structure of the QDT in $E_S$ OR and wind shear show strong similarities, which, besides the indication that the wind shear mechanism is actually an important driver for $E_S$ formation, gives some confidence in the horizontal structure of the modeled tides also.

The modeled QDT amplitudes are too small, compared in comparison with observations. Although it is an ongoing question that numerical models tend to underestimate tides, at least for some regions or seasons (e.g., Smith, 2012; Pokhotelov et al., 2018), the reasons for this underestimation in MUAM is subject to current investigations. Another issue is the relatively coarse meridional model resolution, which may smooth some details of the meridional structure of the QDT. Future experiments will be performed with increased horizontal resolution.

Appendix A: Modeled QDT amplitudes, wind shear amplitudes, and global $E_S$ distribution at different altitudes

Figures A1 - A3 show results of MUAM simulations of the QDT amplitude in zonal wind, similar as in Figure 4, but for different altitudes. Figures A4 - A5 show comparison of global $E_S$ QDT amplitude distributions and MUAM QDT zonal wind...
shear amplitudes, similar as in Figure 7, but for different altitudes.

Code availability. The MUAM model code can be obtained from the corresponding author on request.

Data availability. Radio occultation data are freely available from UCAR on http://cdaac-www.cosmic.ucar.edu/cdaac/products.html. Collm radar wind shears are available from the corresponding author on request.

Author contributions. C. Jacobi performed Collm radar wind measurements and analyses, as well as the tidal analyses based on GPS $E_S$, which had been analyzed by C. Arras. C. Geißler designed and performed the MUAM model runs together with F. Lilienthal. C. Jacobi drafted the first version of the text.

Competing interests. C. Jacobi is one of the Editors-in-Chief of Annales Geophysicae.

Acknowledgements. The provision of FORMOSAT-3/COSMIC data by University Corporation for Atmospheric Research is gratefully acknowledged. Ch. Jacobi, F. Lilienthal, and C. Geißler acknowledge support through the Deutsche Forschungsgemeinschaft (DFG) under grants JA 836/30-1 and JA 836/34-1. C. Arras acknowledges support by the DFG Priority Program DynamicEarth, SPP 1788.
References


Figure 1. Zonal and seasonal mean $E_S$ occurrence rates for (a) DJF (b) MAM (c) JJA (d) SON. Data are averages over 2007 - 2016.
Figure 2. 2007 - 2016 mean winter (December - February) DJF and JJA mean diurnal cycle of zonal wind and wind shear over Collm. Left panels: Height-time cross-sections of zonal wind (color coding) and wind shear (contour lines) for (a) DJF and (c) JJA. Dashed contour lines denote negative wind shear. Note the different color scaling for the DJF and JJA mean mean winds. Right panel: Wind (v = DLF and (d) JJA wind shear at about 91.5 km (black line), together with a fit including mean, 8 hr, 12 hr, and 24 hr components (red line). The residuals, multiplied by a factor of 5, are added as blue line.
Figure 3. 2007-2016 mean seasonal mean Collm residual wind shear after removing diurnal mean shear, 8 hr, 12 hr, and 24 hr components for (a) DJF, (b) MAM, (c) JJA, (d) SON. 6-hr phases, defined as the time of maximum negative wind shear, are added together with their standard deviation calculated from phases of single years. Solid symbols denote oscillations significant at the 5% level according to a t-test.
Figure 4. QDT zonal wind amplitudes at 101 km altitude, as modeled by MUAM.
Figure 5. 2007 - 2016 mean seasonal mean diurnal cycle of $E_S$ occurrence rates for (a) DJF, (b) MAM, (c) JJA, (d) SON in a latitude band 46° - 56° N and in height gates of 10 km. Note the different scaling for JJA.
Figure 6. 2007 - 2016 mean seasonal mean diurnal cycle of $E_S$ residual occurrence rates after removing diurnal mean, 8 hr, 12 hr, and 24 hr components for (a) DJF (b) MAM (c) JJA (d) SON in a latitude band 46 - 56°N and in height gates of 10 km. Note the different scaling for JJA. 6-hr phases of OR and Collm wind shear are added as squares and circles, respectively. Solid symbols denote oscillations significant at the 5% level according to a t-test. The error bars show standard deviations calculated from phases for single years.
Figure 7. Left panel (a): 2007 - 2016 mean monthly mean QDT $E_S$ relative amplitudes at 101 km. Right panel (b): MUAM zonal wind shear at the nearest model level at 100.9 km.
Figure 8. Left column (a): 2007 - 2016 mean monthly mean QDT $E_S$ relative amplitudes for (a) DJF, (c) MAM, (e) JJA, (g) SON. Right columns: corresponding MUAM QDT component of zonal wind shear.
Figure A1. **QDT zonal wind amplitudes at 95.2 km altitude, as modeled by MUAM.**
Figure A2. As in Figure A1, but at 106.6 km altitude.
Figure A3. *As in Figure A1, but at 112.3 km altitude.*
Figure A4. Left panel (a): 2007-2016 mean monthly mean QDT $E_S$ relative amplitudes at 95 km. Right panel (b): MUAM zonal wind shear at the nearest model level at 95.2 km.
Figure A5. As in Figure A4, but showing $E_S$ relative amplitudes at 107 km and zonal wind shear at 106.6 km.
Figure A6. As in Figure A4, but showing $E_S$ relative amplitudes at 107 km and zonal wind shear at 112.3 km.