Electron mirror branch: Observational evidence from historical AMPTE-IRM and Equator-S measurements

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Abstract. Based solely on now historical magnetic and plasma data and available wave spectra from the AMPTE-IRM spacecraft, and on as well historical Equator-S highcadence magnetic field observations of mirror modes in the

- ⁵ magnetosheath near the dayside magnetopause, we present some observational evidence for a recent theoretical evaluation by Noreen et al. (2017) of the contribution of a global electron temperature anisotropy to the evolution of mirror modes and related low-frequency Lion roars (whistlers) ex-
- ¹⁰ cited by the resonant trapped electron component in the hightemperature anisotropic collisionless plasma of the magnetosheath causing a separate electron mirror branch. These old data most probably indicate that signatures of this electron effect on mirror modes had indeed been observed al-
- ¹⁵ ready long ago in magnetic and wave data though had not been recognised as such. Unfortunately either poor time resolution or complete lack of plasma data would have inhibited the confirmation of the notoriously required pressure balance in the electron branch for unambiguous confirmation of a
- 20 separate electron mirror mode. If confirmed by future highresolution observations, in both cases the large mirror mode amplitudes suggest that mirror modes escape quasilinear saturation being in a state of weak kinetic plasma turbulence.

Keywords. Mirror modes, Electron mirror mode, Magne-²⁵ tosheath turbulence, Lion roars, Weak kinetic turbulence

1 Introduction

In the past four decades, observations of magnetic mirror modes in the magnetosheath and magnetotail of Earth's magnetosphere, and occasionally also elsewhere, have been ubiq-³⁰ uitous (see Tsurutani et al., 2011; Sulem, 2011, for reviews on observation and theory, respectively). They were, however, restricted to the ion mirror mode and the detection of electron-cyclotron waves (Lion roars) which propagate in the whistler band deep inside the magnetic mirror configuration and are caused by trapped resonant anisotropic elec- 35 trons. (There is a wealth of literature on observations of mirror modes and lion roars, cf., e.g., Smith and Tsurutani, 1976; Tsurutani et al., 1982; Zhang et al., 1998; Baumjohann et al., 1999; Maksimovic et al., 2001; Remya et al., 2014; Breuillard et al., 2018, to cite only the basic origi-40 nal ones, plus a few more recent papers). These observations confirmed their theoretical prediction based on fluid (cf., e.g., Chandrasekhar, 1961; Hasegawa, 1969; Thorne and Tsurutani, 1981; Southwood and Kivelson, 1993; Baumjohann and Treumann, 2012) and the substantially more elaborated ki- 45 netic theory (cf., Pokhotelov et al., 2000, 2002, 2004, and further references in Sulem, 2011), which essentially reproduces the linear fluid results, just including some additional complications only (like, for instance, finite Larmor radius effects). 50

Recently, this theory has been extended to the inclusion of the effect of *anisotropic nonresonant* electrons on the evolution of mirror modes (Noreen et al., 2017, for earlier effects including isotropic thermal electrons, see their reference list) in the linear and quasi-linear regimes. Though in principle simple matter, the more interesting finding was that the electrons do indeed substantially contribute to the evolution of mirror modes and in theory also to their quasilinear saturation though in rather different wavenumber and frequency/growth rate regimes. This leads immediately to the question of observation of such effects in the mirror modes, especially to the question whether signatures of the electron mirror branch had already been present in any now historical spacecraft observations of mirror modes. Here we demonstrate that, based on more than three decades old AMPTE-IRM observations in the magnetosheath near the dayside magnetopause and two decades old Eq-S magnetic high resolution observations in the equatorial magnetosheath, both

⁵ branches had most probably indeed already been detected in the data though at that time the electron branch had remained unrecognised.

2 Observations

Figure 1 shows a typical sequence of magnetosheath mirror 10 modes lasting longer than six minutes during an AMPTE-

- IRM passage on September 21, 1984. The lower panel shows variation of the magnitude of the magnetic field that is caused by the (ion) mirror mode with amplitude $|\delta B| \sim 0.5|B|$. The upper panel is the wave electric power spectrogram. The
- ¹⁵ wavy white line is the electron cyclotron frequency f_{ce} which maps the magnetic field from the lower panel into the frequency domain. Lion roars emitted in the central mirror mode minima are indicated for two cases. As was shown a decade later (Baumjohann et al., 1999) from high resolu-
- ²⁰ tion magnetic field measurements on the Equator-S spacecraft, thereby confirming their electromagnetic nature, these emissions which for long time were known as Lion roars, do indeed propagate in the whistler band in wave packets parallel to the magnetic field with central frequency roughly
- ²⁵ $f_{lr} \sim 0.1 f_{ce}$ of the local central cyclotron frequency. The origin of the other sporadic intense Lion roar emissions centred around $f \sim 0.5$ -0.7 kHz remained unclear. They are not related to the mirror mode minima. They occur at the mirror mode flanks, being of more broadband nature, more tem-
- ³⁰ porarily irregular and of higher frequency. In addition there are irregular high frequency broadband electric signals above f_{ce} reaching up to the local plasma frequency at $f_e \sim 60$ -70 kHz. Their spiky broadband nature being independent of the presence of the cyclotron frequency suggests that they
- ³⁵ are related to narrow structures or boundaries of which such broadband Fourier spectra are typical. The broad unstructured (green) quasi-stationary noise below roughly 2 kHz propagates in the electrostatic ion-acoustic band and is of little interest here as it is typical for the magnetosheath be ⁴⁰ ing completely independent from the evolution of the mirror

mode. In order to prove that the above sequence of magnetic fluctuations is indeed mirror modes, Figure 2 shows another

- nearly identical sequence of AMPTE-IRM observations, in-⁴⁵ cluding plasma data. (Unfortunately, of the former historical sequence no plasma data are available anymore while in the data set used in this figure no wave data have survived.) Maximum time resolution of the magnetic field on AMPTE-IRM was ~ 30 ms (32 Hz). The presentation is adjusted here to
- ⁵⁰ the time resolution of the plasma instrument which was at the spin resolution of roughly ~ 4 s. The magnetic field in this figure is averaged over 200 ms, though a full resolution mag-

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netic record is available which, however, does not provide any deeper insight because of the lack of any higher plasma resolution than spacecraft spin at the best. The similarity between the magnetic data in Figures 1 and 2 is striking both in period and amplitude. Three cases are indicated in Figure 2 in order to demonstrate the detectable (at these time resolutions) anti-phase behaviour in the magnetic and plasma data in the magnetic amplitude (or magnetic pressure) panel 1, density in panel 3, and temperature in panel 6. (One may note the logarithmic scale in the temperature.)

We will argue that the broadband sporadic nature of the unidentified emissions, their relation to the flanks of the ion mirror mode, and intensification below the local cyclotron ⁶⁵ frequency suggests that they are the signatures of electron mirror branch structures which are superimposed on the ion mirror branch which dominates the gross behaviour of the magnetic field.

For this purpose we refer to a rare observation by the 70 Eq-S spacecraft at the high magnetic sampling rate of 128 Hz which is reproduced in Figure 3. Unfortunately, as had already been noted (Baumjohann et al., 1999), no plasma measurements were available due to failure of the instrument. However, even if the plasma instrument would have 75 worked properly, the resolution of optimum only ~ 3 s spacecraft spin and thus comparable to the plasma resolution of AMPTE-IRM would not have been sufficient anyway for resolving the electron structures in the plasma data and establishing/confirming any pressure balance between the electron fluid and magnetic field, as was done with the AMPTE observations for the ion-mirror modes. What concerns the identification of the large amplitude magnetic oscillations as genuine ion-mirror modes, even though no plasma measurements were available on Eq-S, the reader is referred to Lucek 85 et al. (1999a, b) who analysed the whole sequence of magnetic oscillations measured by Eq-S of which our short high resolution example is just a sample selection. Figure 3 shows this high-resolution record (used by Baumjohann et al., 1999, in the investigation of Lion roars) of the magnetic field magnitude from this data pool of Eq-S. Just two ion-mirror oscillations of the cycle analysed in Lucek et al. (1999a, b) and used in that paper are shown here. One may note that their period and amplitude is of the same order as in the case of the AMPTE observations which were approximately at a 95 similar location in the magnetosheath, thereby providing additional independent confidence for them as being ion mirror modes. One observes the general evolution of the magnetic field which is reflected in the slight asymmetries of the structures which pass over the spacecraft. These might be 100 caused by temporal evolution of the mode or also by crossing the spatially densely packed mirror mode oscillations (which form kind of a "magnetic crystal texture" of magnetic bottles on the plasma background in the magnetosheath, as sketched in Treumann and Baumjohann, 1997, pages 57-58) by the 105 spacecraft under an angle. The maximum of the magnetic field in this case is ~ 30 nT with a $|\delta B|/B \sim 50\%$ ampli-

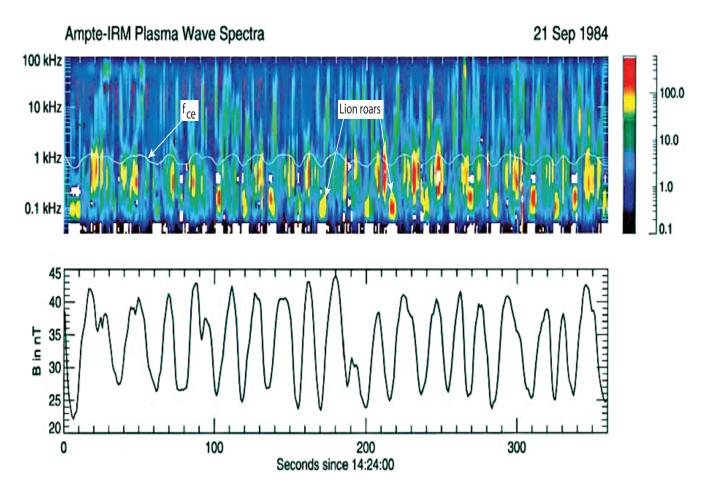


Figure 1. AMPTE-IRM observations of mirror modes in the magnetosheath and related plasma wave power spectra (see the colour bar on the right for relative log-scale intensities). Indicated are the electron cyclotron frequency f_{ce} , and Lion roar emissions in the mirror mode minima at frequency $f_{lr} \sim 0.1 f_{ce}$ (after Treumann et al., 2004a).

tude oscillation, almost identical to what AMPTE-IRM had observed. The very small-amplitude high-frequency fluctuations of the field in the field minima belong to the Lion roars mentioned above and have been investigated in detail $_5$ (Baumjohann et al., 1999, it should be repeated here that the importance of these investigations lies in the fact that, by measuring the magnetic field fluctuations δB frequency

- by measuring the magnetic field fluctuations δB , frequency, amplitude and polarisation, they demonstrated unambiguously that Lion roars are electromagnetic waves propagat-10 ing in the whistler mode. So far all observations were based solely on wave electric field measurements like those in the
- AMPTE-IRM data of Figure 1. The magnetic wave instrument did not provide any measurements in this low frequency range. Moreover, it was shown in that work that the occur-15 rence of Lion roars was related to the presence of a weak
- resonant anisotropy in the electrons.) In the left hand field minimum at the bottom of the ion-mirror oscillation the small local maximum of the magnetic field (like on the bottom of

a wine bottle) can be recognised to which Baumjohann et al. (1999) refer as an unexplained structure.

Three kinds of magnetic variations are visible in this figure. Firstly, we have the large amplitude ion-mirror mode oscillations of which only two periods are shown. Secondly, superimposed on these are the spiky small amplitude excursions from the ion mirror shape which form small peaks and 25 valleys everywhere on the flanks, maxima and minima in rather irregular or at the best quasi-regular sequence. Thirdly and finally, there are very small amplitude oscillations which, as far as the instrument can resolve them, accumulate mainly in relation to the former medium frequency and medium 30 amplitude magnetic modulations. The interesting feature in this high-resolution recording of the magnetic field are these medium frequency medium amplitude tooth-like oscillations of the magnetic field in the flanks, in the maxima and also in the minima of the ion-mirror mode. In this respect the high resolution magnetic field in this figure is quite different from the apparently smooth four-times lower resolution and less

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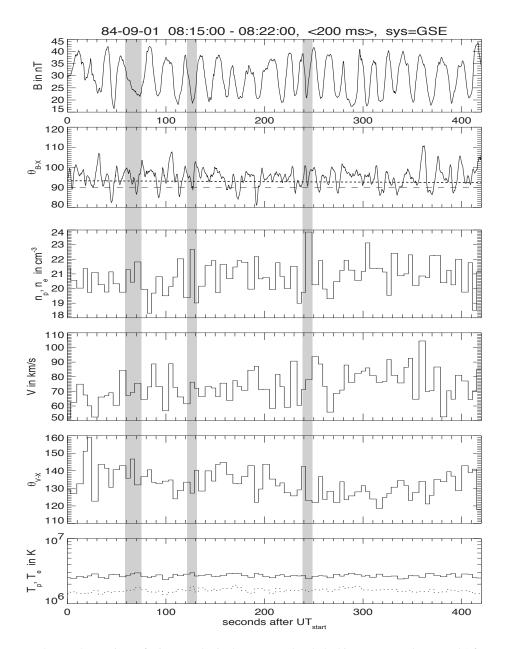


Figure 2. AMPTE-IRM plasma observations of mirror modes in the magnetosheath, lacking any wave data. Panel 1 from top is the magnetic field (averaged here over 200 ms), panel 2 the angle of the magnetic vector in GSE coordinates. The mean direction of the field is indicated by the dotted line during these 6 min of observation. Panel 3 shows the plasma density in the available spacecraft spin resolution of ~ 4 s for a single measurement. Panels 4 and 5 give the mean velocity and direction angle of flow. Panel 6 (in logarithmic scale) is the plasma temperature. Three cases of mirror troughs are shaded showing the anti-correlation between magnetic field (or pressure) and density (or plasma pressure). Though this event is taken at a different occasion, its similarity to the observations in Figure 1, when no plasma data were available, is obvious.

sensitive course of the mirror field in the AMPTE-IRM magnetosheath observations of Figs. 1 and 2. We repeat that these Eq-S chains of magnetic modulations had indeed been identified as mirror modes by Lucek et al. (1999a), even though no 5 plasma data were available. We also repeat that, even if the

plasma instrument on Eq-S would have worked properly, its time resolution of ~ 3 s would not have been sufficient to re-

solve any anti-correlation between the magnetic and plasma pressures in the oscillations which we here and below identify as electron mirror modes. Measuring this anti-correlation ¹⁰ would have required a substantially or even much higher time resolution than the spin resolution, which was only available at the times of those spacecraft.

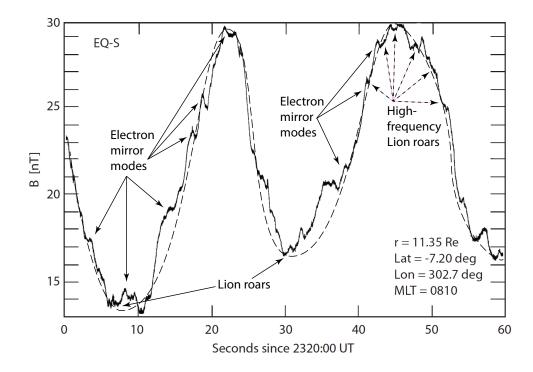


Figure 3. High resolution Eq-S observations of mirror modes in the magnetosheath near the magnetopause at the high sampling rate of 128 Hz. The dashed line is a low-pass filtered trace yielding a quasi-sinusoidal approximation to the ion mirror mode structure. Asymmetries are presumably caused by the obliqueness of the ion mirror mode structure in combination with the plasma flow which transports them to pass over the spacecraft. The strong modulation of their shapes on the smaller scale is produced by the superimposed small-scale electron mirror mode structure on the ion mirror mode. Signatures of low-frequency ($f \leq 0.1 f_{ce}$) Lion roars are found in the ion mirror minima (see Baumjohann et al., 1999, for their identification, packet structure and generation). High-frequency Lion roars concentrate in the minima of the electron mirror mode structures.

In order to infer about the nature of these oscillations we refer to the period of the (ion) mirror mode. This can be read from the figure to be roughly $\tau_{im} \sim 30$ s, corresponding to a frequency of $f_{im} \sim 0.03$ Hz. The tooth-like oscillations, 5 for instance at the first steep increase of the magnetic field,

- have a time period of $\tau_{em} \sim 2-4$ s (or frequency $f_{em} \sim 0.3$ Hz), roughly a factor of ten shorter than the ion-mirror mode. In addition to their steep magnetic boundaries, these structures also exhibit superimposed small frequency oscillations, which are also present in the modulated maxime of the min
- ¹⁰ which are also present in the modulated maxima of the mirror mode. Since the latter belong to magnetic fluctuations, it is reasonable to assume that they are simply a different kind of Lion roars caused by electrons trapped in the local minima of the higher frequency-shorter wavelength modula-
- ¹⁵ tions. Thus their centre frequency should be higher than the Lion roar frequency in the ion-mode minima. This suggests identification with the higher frequency spectral features observed by AMPTE-IRM, while the weak broadband features in the wave spectra may be related to the steep magnetic and ²⁰ plasma (pressure) boundaries of the modulations.

3 Electron mirror branch

If this is the case then it is suggestive to identify the small amplitude modulations in the magnetic field seen by Eq-S and in the wave spectra by AMPTE-IRM with the electron mirror mode which was theoretically predicted (Noreen et al., 25 2017). These authors put emphasis on the quasilinear evolution of the pure electron (ion) and mixed (electron-ion) mirror modes to numerically show for a number of cases how the normalised magnetic and plasma energy densities evolve and saturate. For our purposes it suffices to consider the mixed linear state, because it is clear from the data in Fig. 3 and as a consequence also in the spectrum of Fig. 1 that the dominant magnetic (and also plasma) structure is the ion mirror mode while the electron mirror mode just produces some modification. Clearly the ion mirror mode is a large-scale perturbation 35 on which the quasilinear contribution of the electron mirror mode does not change very much.

For our purposes we need only the simplified purely growing linear growth rate (normalised to the ion-cyclotron frequency $\omega_{ci} = eB/m_i$) for small ion and electron arguments 40

$$\frac{\gamma(\mathbf{k})}{\omega_{ci}} \approx \frac{k_{\parallel}\lambda_i}{A_i + 1} \sqrt{\frac{\beta_{\parallel i}}{\pi}} \left[A_i + \sqrt{\frac{T_{e\perp}}{T_{i\perp}}} A_e - \frac{k^2}{k_{\perp}^2 \beta_{i\perp}} \right]$$
(1)

with $\lambda_i = c/\omega_i$ the ion inertial length, $\omega_i^2 = e^2 N/\epsilon_0 m_i$ square of ion plasma frequency, $A_j = (T_\perp/T_\parallel)_j - 1 > 0$ $_5$ the temperature anisotropy of species j = i, e, and $\beta_{\parallel i} = 2\mu_0 N T_{i\parallel}/B^2$ the ratio of parallel ion thermal and magnetic energy densities (cf., Noreen et al., 2017). Wave growth occurs for positive bracket which provides angular dependent thresholds. The threshold condition for instability can be 10 written in terms of the magnetic field as

$$B < B_{crit} \approx \sqrt{2\mu_0 N T_{i\perp}} \left(A_i + \sqrt{\frac{T_{e\perp}}{T_{i\perp}}} A_e \right)^{\frac{1}{2}} \left| \sin \theta \right| \qquad (2)$$

where $\theta = \sin^{-1}(k_{\perp}/k)$, and the approximate sign refers to the simplifications made in writing the simplified dispersion relation. Once the local magnetic field drops *below* this 15 threshold value, instability will necessarily set on. Such a critical value B_{crit} exists for all combinations of anisotropies which leave the sum under the root positive. It has a deeper physical meaning (Treumann et al., 2004a) corresponding to

- a classical Meissner effect in superconductivity. This thresh-²⁰ old relates to the critical mirror mode angle of Kivelson and Southwood (1996). It sets an angular dependent upper limit on the critical magnetic field which vanishes for parallel and maximises for perpendicular propagation. In both these cases, however, no instability can arise, as follows from the ²⁵ growth rate, and the instability, as is well known, is oblique.
- The growth rate obtained from the simplified dispersion relation maximises formally at a maximum angle θ_{max} with

$$\sin^2 \theta_{max} \approx \frac{1}{2a} \bigg\{ \sqrt{1+8a} - 1 \bigg\}, \quad 1 < a \equiv \beta_{i\perp} \bigg[A_i + \sqrt{\frac{T_{e\perp}}{T_{i\perp}}} A_a \bigg]$$
(3)

³⁰ For a = 2, for instance, this yields $\theta_{max} \approx 45^{\circ}$ in accord with the exact numerical calculation for the ion mode based on the full dispersion relation (Noreen et al., 2017). No maximum exists for $a \le 1$. Folding the growth rate with the threshold condition and maximising yields the optimum unstable ³⁵ range. This gives a third order equation for $x = \cos 2\theta_{opt}$:

$$x^{3} - \left(1 - \frac{2}{a}\right)x \pm \frac{1}{a} = 0 \quad \text{for} \quad \begin{cases} \theta_{opt}^{(1)} &< \pi/4 \\ \theta_{opt}^{(2)} &> \pi/4 \end{cases}$$

depending on the sign of the last term. Expanding near parallel propagation $x - \xi \approx 1$ for $a \gtrsim 2$ and very roughly keeping only the linear term in ξ , gives two solutions which approximately fix the range $\theta_{opt}^{(1)} < \theta < \theta_{opt}^{(2)}$ of maximum growth for the ion mode, corresponding to angles $\theta_{opt}^{(1)} \approx \frac{1}{2} \cos^{-1} \left(\frac{1}{2}\right) \approx 30^{\circ}$ and $\theta_{opt}^{(2)} \approx \frac{1}{2} \cos^{-1} \left(-\frac{1}{6}\right) \approx 50^{\circ}$. These considerations

apply to the simplified dispersion relation used in this paper. They don't discriminate between the roles of ion and electron

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They don't discriminate between the roles of ion and electron gyro radii. This distinction is contained in the full dispersion relation on which the numerical solution (Noreen et al., 2017) is based, thereby leading to the numerically obtained precise angular ranges for the two branches of the mirror instability to which we refer below.

The pure electron effect which applies to the electron 50 branch is obtained for isotropic ions $A_i = 0$ and $T_{i\parallel} = T_{i\perp} \equiv T_i$. On the electron gyroradius scale the ions are unmagnetised, yielding

$$\frac{\gamma_e(\mathbf{k})}{\omega_{ci}} \approx k_{\parallel} \lambda_i \sqrt{\frac{\beta_{e\parallel}}{\pi}} \left[A_e - \frac{k^2}{k_{\perp}^2 \beta_{e\perp}} \right] \sqrt{A_e + 1}$$
$$B_{crit,e} \approx \sqrt{2\mu_0 T_{e\perp} A_e} |\sin \theta| \qquad 55$$

The perpendicular mirror scale and critical threshold magnetic field are determined by the electron anisotropy A_e and perpendicular electron thermal energy ratio $\beta_{e\perp}$.

Effectively, the electron-mirror branch remains to be a separate branch on the ion-mirror instability with parallel ⁶⁰ scale determined by the ion inertia, while its perpendicular scale and critical excitation threshold are prescribed by the electron dynamics. The perpendicular scale of the electron branch is much shorter than the ion scale, while the threshold depends only on the electron temperature and anisotropy. ⁶⁵ Writing the growth rate in pure electron quantities, one has for the isotropic-ion electron branch

$$\frac{\gamma_e(\mathbf{k})}{\omega_{ce}} \approx \sqrt{\frac{\beta_{e\parallel}}{\pi}} \left[A_e - \frac{k^2 e^{\zeta_e}}{k_\perp^2 \beta_{e\perp} [1 - \zeta_e/2]} \right] \frac{k_\parallel \lambda_e}{D}, \quad \zeta_e = k_\perp^2 \lambda_e^2 \beta_{e\perp} < D \equiv 1 + \sqrt{\frac{m_i}{m_e} \frac{T_{e\perp}}{T_i}} (A_e + 1)^{-2} e^{-(\zeta_i - \zeta_e)}$$

The ion term D in the nominator acts stabilising on the elece tron branch though, because of the large square of the ion gyroradius $\zeta_i/\zeta_e = (m_i/m_e) T_{e\perp}/T_i \gg 1$, the additional term in D is exponentially reduced. The electron inertial scale λ_e enters to replace λ_i . This expression shows the similarity be-75 tween the ion and electron branches, however with different scales and an increased threshold for the electron branch. The electron-branch growth rate depends on the ion temperature. When T_i becomes large, the growth of the electron contribution will be suppressed. In contrast to the magnetosheath 80 this should be the case, for instance, in Earth's magnetotail plasma sheet where one has $T_i \sim 10 T_e$. Presumably any mirror modes which evolve there will be void of an electron branch.

In the last expressions the direction of anisotropy is with respect to the local magnetic field as the electrons experience it. It can be rather different from that of the main branch of the ion mirror mode. These effects are still of first order, being independent of any finite Larmor-radius contributions (Pokhotelov et al., 2004) which occur in higher order approximation, having been shown (Noreen et al., 2017) to be of

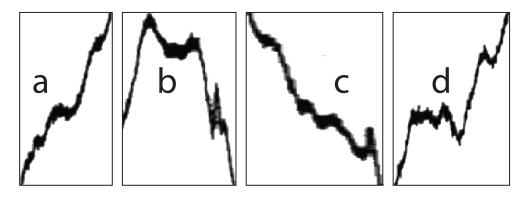


Figure 4. Four cases of high frequency Lion roars related to electron mirror modes extracted and zoomed in from Figure 3. Cases a, c, d are at the flanks of the ion mirror structures, case b is on top in the first absolute magnetic maximum, all causing a broadening of the magnetic trace. At the 128 Hz sampling rate, such oscillations cannot be resolved. It allowed Baumjohann et al. (1999) to analyse the lowest frequencies $(f \leq 0.1 f_{ce} \text{ at } f_{ce} \leq 1 \text{ kHz})$, but inhibits a similar analysis for the higher frequency Lion roars.

minor importance. This might not be the last word, because these authors investigate just the linear and quasilinear evolution of mirror modes. Below we comment on this important point.

- ⁵ It is clear from here that, based on our arguments and the numerical calculations (Noreen et al., 2017, see their Fig. 1), the two branches of the mirror mode grow in separate regions of wavenumber space k_{\parallel}, k_{\perp} , where the indices refer to the directions parallel and perpendicular to the local magnetic
- ¹⁰ field, i.e. in the ion mirror mode to the average ambient magnetic field which is modulated by the mirror mode, on the electron branch the local magnetic field at the location where the electron mirror bubble evolves. This main and well expected effect in the combined electron-ion growth rate found
- ¹⁵ by numerically solving the complete non-simplified growth rate (Noreen et al., 2017, their Eq. 4) is that, because of the different gyration scales of electrons and protons, the growth rate exhibits its two separate branches and maximises at different angles for the two branches. Since in the linear state
- ²⁰ the different modes extract their energy from the component of particles to which they belong, the two modes grow separately but not independently because of their inertial coupling and the modification of the local magnetic field by the ion branch. It is this local field and thus mostly reduced field ²⁵ which the electrons feel. Only in the quasilinear state an ex-
- change in energy takes place (as shown by Noreen et al., 2017).

Their linear numerical calculations demonstrate clearly that in absolute numbers the electron branch growth rate

- ³⁰ (measured in ion cyclotron frequencies) is about an order of magnitude larger than that of the ion mirror mode. It grows faster and, as a consequence, saturates readily, such that one expects it to be of comparably small final amplitude. The ion mirror mode growth rate maximises at $k_{\parallel i} \approx k_{\perp i}$, which cor-³⁵ responds to an angle of ~ 45° with respect to the ambient
- magnetic field direction, while the electron branch mode is

nearly perpendicular $k_{\parallel e} \approx 0.1 k_{\perp e}$, i.e. it is of much shorter perpendicular than parallel wavelength. On the other hand, the maximum unstable parallel wavelengths are comparable, $k_{\parallel e} \approx 3k_{\parallel i}$, while the maximum unstable perpendicular 40 wavelengths are different: $k_{\perp e}/k_{\perp i} \approx 20-30$ for the parameters investigated (Noreen et al., 2017). The electron mirror branch structure is elongated essentially parallel to the local field, while the ion mirror branch is oblique to the ambient field. Whereas the ion mirror mode tends to form large mag- 45 netic bubbles, the electron mirror mode forms narrow long bottles on the structure given by the ion mirror mode. We may assume that this behaviour will not be very different for other parameter choices than those used in the numerical calculation, as it is just what one would expect: the electron 50 mirror mode being somewhat shorter in parallel wavelengths and substantially shorter in perpendicular wavelengths than the ion mirror mode, an effect of the vastly different gyroradii.

4 Discussion

With this information at hand we consult the high resolution Eq-S observations in Fig. 3. This figure suggests that Eq-S was crossed by the chain of mirror structures *almost* in the perpendicular direction. Comparing the times of crossing the large-scale ion mirror mode and the well expressed small-⁶⁰ scale structures on the flank of the first rising boundary, we infer that the ratio of wavelengths between the long and short structures is of the order of roughly a factor of ~ 10. Though this is not exactly the above value for this ratio in the perpendicular direction, it is pretty close to the expectation that ⁶⁵ the small scale structure is caused by the electron component thus representing the electron mirror mode (indicated already in Sect. 2 by the subscript *em*).

There are a number of shorter structures of smaller amplitudes visible the use of which would come closer to the 70

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canonical scales obtained from the numerical calculation of the maximum growth rates (Noreen et al., 2017). However there are many reasons for staying with this result. The first would be the choice of the parameters chosen by Noreen et

- al. (2017) for their linear and quasilinear calculation. Another and more important one is that even for those parameters the spread of the domain of maximum growth of both the ion and electron mirror modes (cf. Fig.1 in Noreen et al., 2017) is sufficiently large for fitting the spread in the mea-
- ¹⁰ surements. We may apply the half-maximum condition to the numerical calculation for exponential growth. Inspecting the growth rate plot, the wave power is one fourth of its value at maximum growth for wave numbers k_{\perp} with growth rate $\gamma(k_{\perp}) \sim 0.3 \gamma_{max}$. With this value the figure implies a spread
- ¹⁵ in k_{\perp} for the electron mode of $\Delta k_{\perp} \lambda_i \sim 5$, large enough for covering a sufficiently broad interval of electron mirror wavelengths to account for the time or wavelength spread in our Figure 3. Finally, just to mention it, it is not known from the observations, in which direction precisely the elec-
- ²⁰ tron mirror mode would propagate relative to the ion mirror mode. Theory suggests propagation nearly parallel to the *local mean* magnetic field. This might become fixed with MMS observations. Hence, the above conclusion, though still imprecise, should suffice as evidence for the observation of both
- ²⁵ electron and ion mirror modes in the magnetosheath by Eq-S with both modes acting simultaneously in tandem. Unfortunately, as noted above, no plasma observations were available such that we are not in the position to provide a more sophisticated investigation, in particular the wanted pressure
- ³⁰ balance between the electron mirror field and electron pressure implicitly contained in the theory. But even if the Eq-S plasma instrument would have worked properly, its poor time resolution of ~ 3 s would not have been sufficient for demonstration of any pressure balance.
- Accepting that Eq-S indeed observed both modes in the magnetosheath, reference to Fig. 3 further suggests that, as suspected, the intense higher-frequency unidentified emissions beneath the electron cyclotron frequency in Fig. 1 represent the equivalent to Lion roars in the ion mirror mode
- ⁴⁰ though now on the electron mirror branch. Recently Breuillard et al. (2018, see their Fig. 1) in analysing MMS electron and wave data observed high frequency whistler waves at the edges of mirror mode packets in relation to a perpendicular anisotropy in the electron temperature (see Fig. 5 in Breuil-
- ⁴⁵ lard et al., 2018) which, in the light of our claim, provides another indication for the presence of an electron mirror branch. In fact, it would be most interesting to check whether the high sampling rate of 33.3 Hz on MMS suffices for detecting a pressure balance between electron mirror-scale magnetic os-
- ⁵⁰ cillations and electron pressure. This should decide whether the electron branch is an own bulk-electron-anisotropy driven branch of the mirror mode or just a magnetic oscillation which is not in pressure balance.

The perpendicular extension of an electron mirror branch, 55 though being shorter than the ion inertial length $\lambda_i = c/\omega_i$

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is, for a magnetic field of the order of $B \approx 25$ nT as in the measurements of Eq-S, still substantially larger than the electron gyroradius, which is a general condition for the electron mirror branch to exist and grow on magnetised globally anisotropic electrons. Electrons trapped inside those struc- 60 tures on the electron mirror branch will, by the same reasoning (cf., e.g., Thorne and Tsurutani, 1981; Tsurutani et al., 1982, 2011; Baumjohann et al., 1999, and others), be capable of exciting the whistler instability and thus produce high frequency Lion roars, still below the *local* electron cyclotron 65 frequency, which in this case would be around $f \sim 0.5 - 0.7$ kHz, in reasonable agreement with the majority of high intensity emissions below the local electron cyclotron frequency in Fig. 1. (It also corresponds to the MMS observations reported by Breuillard et al., 2018). These are found to coincide 70 with the walls and maxima of the main ion mirror structures, and in some cases evolve even on top of the maxima (see the cases indicated in Fig. 3) in the magnetic field strength. Quasilinear quenching of the anisotropy to a low level is no argument against the presence of Lion roars. A low level of 75 bulk temperature/pressure anisotropy will always be retained even quasilinearly. Excitation of whistler waves will occur if an anisotropic resonant electron component is present.

Hence the higher-frequency waves related to the mirror structures are presumably caused by those anisotropic res-80 onant electrons which may become trapped in the secondary electron mirror branch structures (Breuillard et al., 2018, in their Fig.5, report a perpendicular electron anisotropy in relation to the observation of high frequency waves) which grow on the background magnetic field and plasma structure of the 85 ion mirror mode. Considering that mirror modes trap electrons and that there is plenty of reason for the trapped electrons to evolve temperature anisotropies as well as a higher energy resonant electron component, this is quite a natural conclusion. On the other hand, the weak broadband elec- 90 tric emissions exceeding the ambient cyclotron frequency and being irregularly related to the ion mirror structures then presumably result from steep plasma boundaries on the shorter scale electron mirror branch structures, i.e. from their trapped electron component which should be responsible for 95 the maintenance of the (currently otherwise undetectable) local total pressure balance in them, when traversing the spacecraft at the high flow speeds in the magnetosheath. Generation of such broadband signals in steep electron gradients are well known from theory and observation of ion and electron 100 holes.

At this occasion a remark on the *saturation* of the mirror mode is in place. It is sometimes claimed that quasilinear saturation, because of the exponential self-quenching of the growth rate, readily limits the achievable amplitude of a linear instability to rather low values of at most few percent or less. This behaviour is clearly seen in the numerical calculations of the quasilinear mirror saturation level (cf., Noreen et al., 2017, e.g. their Fig. 2, where the magnetic amplitude settles at $\langle \delta B \rangle / B \lesssim 0.2\%$ of the main field). For the mirror 110

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mode this results in quasi-linear depletion of the global temperature anisotropy (cf., e.g., Treumann and Baumjohann, 1997; Noreen et al., 2017). The same argument applies to the electron whistler instability (leading to Lion roars) which

 ⁵ (since Kennel and Petschek, 1966; Vedenov et al., 1961) is known to quench the responsible *resonant* electron temperature anisotropy until reaching a balance between a rudimentary level of anisotropy/resonant particle flux and moderate wave intensity, an argument that also applies to the genera-¹⁰ tion of Lion roars.

However, there is a big difference between the two saturation processes in mirror modes, whether on the ion or electron mirror branches, and quasilinear saturation of whistlers. This difference frequently leads to misconceptions. Mirror

- ¹⁵ modes result from macroscopic (fluid) instability the source of which is the *global pressure/temperature* anisotropy of the bulk of the particle distribution. It is this anisotropy which provides the free energy of the mirror instability. Whistlers and ion-cyclotron waves, on the other hand, take their en-
- ²⁰ ergy from a completely different source, the presence of a small population of anisotropic *resonant* particles. Depletion of the latter by quasilinear saturation of the whistler instability has no effect on the global temperature anisotropy which drives mirror modes unstable; it just quenches the emission ²⁵ of whistlers (or in a similar way also ion-cyclotron waves).

Though violent quasilinear suppression of the mirror instability and saturation at a low quasilinear level seem reasonable, they contradict the observation of the $|\delta B|/B \sim$ 50% amplitudes reported here and elsewhere. Restriction

- ³⁰ to quasilinear saturation ignores higher-order nonlinear interactions. It is well known that in many cases these additional weakly-turbulent effects undermine quasilinear saturation as, for instance, occurs in one of the most simple and fundamental instabilities, the gentle-beam-plasma inter-
- ³⁵ action (the reader may consult Yoon, 2018, for a most recent and exhausting review of this basic plasma instability which serves as a paradigm for all instabilities in a hot collisionless plasma). In fully developed weak plasma turbulence (cf., e.g., Sagdeev and Galeev, 1969; Davidson, 1972;
- ⁴⁰ Tsytovich, 1977, for the basic theory), various mode couplings and higher-order wave-particle interactions erase the process of flat straightforward quasilinear stabilisation. Under weak turbulence, the instability evolves through various stages of growth until finally reaching a quasi-stationary tur-
- ⁴⁵ bulent equilibrium very different from being quasilinear. In the particle picture, this equilibrium state is described by a generalised Lorentzian thermodynamics (Treumann, 1999a, b; Treumann et al., 2004b, 2008; Treumann and Baumjohann, 2014a) resulting in the generation of power-law tails
 ⁵⁰ on the distribution function which have been observed since decades in all space plasmas.

The weakly-turbulent generation of the quasi-stationary electron distribution, the so-called κ -distribution (which is related to Tsallis' *q*-statistics, cf., Tsallis, 1988; Gell-Mann ⁵⁵ and Tsallis, 2004, see also the review by Livadiotis 2018,

and the list of references to q statistics therein; the relation between κ and q was given first in Treumann 1997), was anticipated in an electron-photon-bath calculation by Hasegawa et al. (1985), but the rigorous weak-turbulence theory, in this case providing an analytical expression for the power κ_{60} as function of the turbulent wave power, was given first by P.H. Yoon for a thermal electron plasma with stationary ions under weakly turbulent electrostatic interactions, including spontaneous emission of Langmuir waves, induced emission and absorption (Landau damping) (see Yoon, 2014, and the 65 reference therein). Similar electromagnetic interactions take place in weak magnetic turbulence (cf. Yoon, 2007; Yoon and Fang, 2007, for an attempt of formulating a weaklyturbulent theory of low-frequency magnetic turbulence). At high particle energies this power law becomes exponentially 70 truncated when other effects like spontaneous reconnection (Treumann and Baumjohann, 2015) in magnetically turbulent plasmas or particle-particle collisions ultimately come into play when the life time becomes comparable to the collision time (Yoon, 2014; Treumann and Baumjohann, 2014b). 75 Until this final quasi-stationary state is reached, the instability grows steadily in different steps, thereby assuming substantially larger amplitudes than predicted by quasilinear theory.

For magnetic mirror modes no weakly turbulent theory has 80 so far been developed yet. The observed $|\delta B|/B \sim 50\%$ amplitudes of the ion-mirror modes in Figures 1 and 2, and the comparably large amplitudes of the inferred electronmirror branch oscillations recognised in Figure 3 are much larger than quasilinearly expected (Noreen et al., 2017). 85 The electron-mirror branch amplitude inferred from Figure 3 amounts to $\langle \delta B \rangle / B \sim 5\%$, one order of magnitude less than for the ion mode though as well still much larger than quasilinearly predicted. Such large amplitudes suggest that both branches, the ion-mirror as well as the electron-mirror 90 branch, do in fact not saturate quasilinearly. Rather they are in their weakly turbulent quasi-stationary state. Presumably they have not yet reached their final state of dissipation and at least not that of their ultimate dissipative or even collisional destruction. The latter being anyway irrelevant at the plasma 95 flow times in the magnetosheath.

The question for a weak turbulence theory of mirror modes raises the problem of identification of the possible plasma modes which could be involved. The best candidates are ioncyclotron waves/ion whistlers. Similar to electron whistlers ¹⁰⁰ they propagate almost parallel to the magnetic field. Similar to what is believed of whistlers, they quasi-linearly deplete any *resonant* plasma anisotropy. Under the conditions of the AMPTE IRM and Eq-S observations considered here, their frequency should be roughly ~ 1 Hz. They should thus appear about once per second. Inspection of the magnetic trace in Figure 3 gives no indication of their presence. The waves which we identify as the electron-mirror branch are of lower frequency.

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It can, however, not unambiguously be excluded that just these waves represent ion-cyclotron wave *packets* which have evolved nonlinearly to large amplitudes and long wavelengths in the course of weak kinetic turbulence of ion-mirror

- ⁵ modes, thereby erasing the quasilinear depletion of the ion anisotropy and allowing further growth of the mirror mode to achieve their large amplitudes. Hence, here we detect a possible caveat of our investigation. The argument against this possibility is that ion-cyclotron waves, whether linear or
- ¹⁰ nonlinear, should not be in pressure balance nor should they trap any electrons. This means they should not be related to the excitation of the observed high frequency whistlers or Lion roars. However, even that argument may be weak if the ion-cyclotron wave packets locally produce enough radiation
- ¹⁵ pressure to deplete plasma from their regions of maximum amplitude. Electrons reflected from those packets could then possibly locally evolve temperature anisotropies and by this cause high frequency whistlers.

Thus, one identifiable caveat remains in the possibility that ²⁰ ion-cyclotron waves (in both cases of AMPTE IRM and Eq-S

- at frequency ~ 1 Hz) have become involved into the weaklyturbulent evolution of the observed ion-mirror modes (or possibly also other low-frequency electromagnetic drift waves, which could be excited in the magnetic and plasma gradi-
- ents at the ion-mirror boundaries). As noted above, the effect of ion-cyclotron waves is believed to quasi-linearly diminish the *resonant* part of the ion anisotropy which probably does not happen when weak kinetic turbulence takes over. In weak turbulence, the nonlinear evolution of the ion-cyclotron
- ³⁰ waves erases the quasilinear quenching and allows further growth of the ion-cyclotron waves until the waves evolve into the above mentioned wave packets of long wavelength which may become comparable to the structures identified here as the electron-mirror branch waves. This possibility cannot be ³⁵ excluded.

There is no final argument against the involvement of such waves other, than that ion cyclotron waves, like whistlers, are immune against pressure balance. As linear waves they do not trap any electrons which, however, might change when

- ⁴⁰ becoming strongly nonlinear. As long as this does not happen, it would exclude ion-cyclotron waves as source of the Lion roars observed in the wave data of Figure 1. It will be worth investigating these far reaching questions with the help of high resolution plasma, field, and wave observations from
- ⁴⁵ more recent spacecraft missions like MMS. It would also be worth investigating whether any electromagnetic short wavelength (electron) drift modes can be detected. Those waves might, in addition to ion-cyclotron and of course also electron-mirror branch modes themselves, become involved
- ⁵⁰ into the weak turbulence of ion-mirror modes when excited at short wavelengths comparable to the plasma gradient scales in mirror modes. Their excitation is on the expense of the pressure balance. Thus they might directly affect the macroscopic anisotropy and contribute to the weak kinetic turbu-

lence of the mirror mode while at the same time undermining 55 their quasilinear quenching.

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