

Estimates of vertical eddy diffusivity in the upper mesosphere in the presence of a mesospheric inversion layer

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Abstract. Rayleigh and resonance lidar observations were made during the Turbopause experiment at Poker Flat Research Range, Chatanika Alaska (65° N, 147° W) over a 10 h period on the night of 17-18 February 2009. The lidar observations revealed the presence of a strong mesospheric inversion layer (MIL) at 74 km that formed during the observations and was present for over 6h. The MIL had a maximum temperature of 251 K, amplitude of 27 ± 7 K, a depth of 3.0 km, and overlying lapse rate of $9.4 \pm 0.3 \,\mathrm{K \, km^{-1}}$. The MIL was located at the lower edge of the mesospheric sodium layer. During this coincidence the lower edge of the sodium layer was lowered by 2 km to 74 km and the bottomside scale height of the sodium increased from 1 km to 15 km. The structure of the MIL and sodium are analyzed in terms of vertical diffusive transport. The analysis yields a lower bound for the eddy diffusion coefficient of $430 \text{ m}^2 \text{ s}^{-1}$ and the energy dissipation rate of 2.2 mW kg^{-1} at 76–77 km. This value of the eddy diffusion coefficient, determined from naturally occurring variations in mesospheric temperatures and the sodium layer, is significantly larger than those reported for mean winter values in the Arctic but similar to individual values reported in regions of convective instability by other techniques.

Keywords. Meteorology and atmospheric dynamics (Middle atmosphere dynamics; Turbulence; Instruments and techniques)



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1 Introduction

Turbulence is critical in determining the vertical distribution and transport of minor species in the middle atmosphere as well as contributing to the dissipation of waves and tides in this region. The dynamical processes of gravity-wave instability, overturning, breaking, and nonlinear behavior both contribute to turbulent processes in the mesosphere and are impacted by them (see the collection of papers in the monograph edited by Siskind et al., 2000; and the review articles by Fritts and Alexander, 2003; Hecht, 2004). Efforts to characterize turbulence vary between attempts to describe the time-averaged behavior that supports studies of the composition and circulation of the middle atmosphere at seasonal and climatological time-scales (e.g., Schoeberl et al., 1983; Vlasov and Kelley, 2010) and attempts to describe the small-scale transient processes that generate turbulence locally (e.g., Lehmacher and Lübken, 1995; Hecht et al., 1997; Bishop et al., 2004; Lehmacher et al., 2006). Furthermore there are significant differences in the techniques used to measure turbulence that tend to yield systematic differences in the values of turbulent parameters (e.g., Lübken, 1997; Hecht et al., 2004).

The Turbopause experiment was designed to advance understanding of turbulent processes in the upper mesosphere and lower thermosphere by making rocket-borne independent measurements across the turbopause using two different techniques; (i) spectral analysis of small-scale highfrequency density fluctuations, and (ii) expansion of luminous vapor trails (Lehmacher et al., 2011). In this paper we present lidar observations of the upper mesosphere on the night of 17–18 February 2009 at Poker Flat Research Range, (PFRR), Chatanika, Alaska (65° N, 147° W) in support of the Turbopause experiment. The lidar observations were Rayleigh lidar measurements of temperature profile (\sim 40– 90 km) and resonance lidar measurements of mesospheric sodium profiles (\sim 70–120 km). The rocket-based measurements coincided with the appearance of a mesospheric inversion layer near 75 km, with an overlying near adiabatic lapse rate, and changes in the structure of the bottomside of the sodium layer at the same altitude. We analyze these observations in terms of recent studies of wave-breaking, turbulence, and sodium chemistry and estimate the eddy diffusivity associated with the mesospheric inversion layer.

This paper is arranged as follows. In Sect. 2 we describe the Rayleigh and resonance lidar techniques and the methods used to determine and characterize the thermal structure and the sodium layer. In Sect. 3 we present the lidar observations in terms of the mesospheric inversion layer and the coincident structure of the sodium layer. In Sect. 4 we analyze the observations in terms of turbulent transport and estimate the eddy diffusion coefficient. In Sect. 5 we discuss our observations and results in terms of other studies of turbulence. Finally, in Sect. 6 we present our summary and conclusions.

2 Experiment and methods

2.1 Rayleigh lidar

Rayleigh lidar measurements of middle atmosphere temperatures have been made at Chatanika on an ongoing basis since 1997 (Thurairajah et al., 2009). The configuration of the lidar system during the Turbopause experiment was the same as that reported in recent studies (e.g., Thurairajah et al., 2010a, b). The lidar observations yielded measurements of the stratospheric and mesospheric temperature profile (~40-80 km) under the assumptions of hydrostatic equilibrium and an initial temperature at the upper altitude. In previous studies we had taken the initial temperature values from a climate atlas. The initial temperature was the major source of uncertainty in the lidar measurement in the altitude range within a scale height (~ 8 km) of the upper altitude. In this study we used the Turbopause rocket-borne ionization gauge measurements of temperature (Lehmacher et al., 2011) to provide the temperature at the upper altitude and thus remove this source of uncertainty from the lidar measurements. The Turbopause rocket-borne measurements were made with four rockets launched over a period of two hours. The ionization gauge measurements were made during the downleg stage of two of the rockets that were launched at 01:29 LST (10:29 UT) and 01:59 LST (10:59 UT). The resolution of the Rayleigh lidar measurements was 50 s and 75 m. We then integrate the Rayleigh lidar data to improve the statistical confidence in the temperature measurements. Except for the choice of initial temperature, we use the same inversion methods as those reported in recent studies (e.g., Thurairajah et al., 2010b). We operated the Rayleigh lidar over an 11h period from 19:47 until 07:12 on the night of 17–18 February 2009 LST (04:47–16:12, 18 February 2009 UT, UT = LST + 9 h).

In this study we report temperature profiles for both the entire night over the 40-90 km altitude range and successive 2-h intervals over the 40-82 km altitude range. When we consider the temperature structure at the time of the rocketborne measurements (i.e., profiles based on the integration over the 2-h intervals centered on the rocket-borne measurement), we use the corresponding ionization gauge temperature measurement as the initial temperature in the lidar inversion. When we consider the temperature structure for the whole night (i.e., the nightly mean or a sequence of 2-h profiles), we use the average of the ionization gauge temperature measurements as the initial temperature in the lidar inversion. We determine the uncertainty in the measurements due to the initial temperature by calculating the variation in the measured temperatures due to changes in the initial temperature $(\pm 10 \text{ K}, \pm 25 \text{ K}).$

2.2 Resonance lidar

Resonance lidar measurements of the mesospheric sodium layer have been made at Chatanika on an ongoing basis since 1995 (Collins et al., 1996; Collins and Smith, 2004). The configuration of the resonance lidar during the Turbopause experiment differed from that reported by Collins and Smith (2004). For this experiment we replaced the 0.35 m diameter telescope with a 1.04 m diameter telescope, and we replaced the flashlamp-pumped dye laser with an excimer-pumped dye laser. Consequently due to the increase in the receiver area, increase in the laser power, reduction in laser linewidth, and increase in laser frequency stability, the lidar signal levels were a factor 10-20 times greater than in earlier studies at Chatanika. The resolution of the resonance lidar measurements was 100 s and 75 m. We then integrated the resonance lidar data to 15 min to improve the statistical confidence in the sodium measurements. We used the same standard inversion methods as used in previous studies to determine the sodium concentration profiles between 70 and 120 km. We operated the resonance lidar over a 10h period from 20:35 until 06:00 LST (05:35-15:00 UT).

3 Observations

3.1 Stratospheric and mesospheric temperature

We plot the average temperature profile for the observation period in Fig. 1. We integrated the lidar signal over the whole observation period to provide a statistically significant profile up to 90 km. We also plot the temperature profile from the monthly reference atlas of the Stratospheric Processes And their Role in Climate (SPARC) (SPARC, 2002; Randel et al., 2004). The measured temperature profile on the night of the 17–18 February was significantly different from the February SPARC profile. The stratopause from the lidar was at an



Fig. 1. Temperature profiles measured by Rayleigh lidar at Chatanika, Alaska on the night of 17–18 February 2009. The nightly average temperature measured over the interval 19:47–07:12 LST (04:47–16:12 UT, thick dashed line) and the temperature profile measured over the two hour interval 01:04–03:04 LST (10:04–12:04 UT, thin solid line) are plotted. The one-sigma temperature errors due to the statistical fluctuations in the lidar signal (dashed lines) and the SPARC February temperature profile (dashed line and solid squares) are also plotted. The linear fit to the topside of the mesospheric inversion layer is indicated.

altitude of 49.8 km and had a temperature of 235.1 K. The SPARC stratopause was at 49.1 km and had a temperature of 253.4 K, nearly 20 K warmer than the lidar measurement. The lidar measurement also shows a mesospheric inversion layer (MIL) that extended from 67.6 km to 73.2 km. The MIL had a maximum temperature of 232.5 K, amplitude of 9.8 ± 2.3 K, and a depth of 5.6 km. We determined the lapse rate over 3 km intervals on the topside of the MIL and find that the maximum lapse rate was 4.7 ± 0.2 K km⁻¹ over the 76.8–79.8 km range.

We calculated the temperature profiles over the two-hour period spanning the rocket-borne ionization gauge measurement at 02:04 LST (11:04 UT). We initialized the temperature profile with the ionization gauge measurement at 82 km. The temperature profile is plotted in Fig. 1. The MIL is clearly evident. The 01:04-03:04 LST profile shows a MIL that extends from 71.2 km to 74.2 km. The MIL has a maximum temperature of 251.0 K, amplitude of 27.2 ± 6.8 K, and a depth of 3.0 km. We find that the maximum lapse rate is 9.4 ± 0.3 K km⁻¹ over the 74.5–77.5 km range. MILs of similar amplitude have been reported at Chatanika at lower altitudes (Cutler et al., 2001). In order to study the evolution of the MIL over the entire observation period we calculated a sequence of 19 temperature profiles that are derived from the Rayleigh lidar signal integrated over 2h intervals at 30 min offset. Given the proximity of the MIL to the initial ionization gauge temperature, we also calculated the se-



Fig. 2. Characteristics of mesospheric inversion layer (MIL) measured by Rayleigh lidar at Chatanika Alaska on the morning of 18 February 2009 (solid thick line closed square). The values due to errors in the initial temperature at 82 km (long dashed lines) are also plotted. Upper: Peak MIL altitude as function of local time. Middle: MIL Amplitude, as a function of time. The error bars are one-sigma uncertainties due to the statistical fluctuation in the lidar signal. Lower: MIL Lapse Rate as a function of time. The error bars are one-sigma uncertainties due to the statistical fluctuation in the lidar signal. The dry adiabatic lapse rate is also plotted (short dashed line). The maximum, minimum and average values are noted.

quence of temperature profiles using the initial temperature -25 K, -10 K, +10 K, and +25 K. The MIL appeared in the Rayleigh lidar temperature profiles as a robust feature from 00:30 LST until 06:00. We plot the variation of the MIL altitude, amplitude and topside lapse rate as a function of time in Fig. 2. The MIL generally descends over time with a maximum altitude of 76.4 km and a minimum altitude of 71.4 km, with an average altitude of 73.5 km. The amplitude of the



Fig. 3. Sodium concentration measured by resonance lidar at Chatanika, Alaska on the night of 17–18 February 2009. The concentration is plotted in false color as a function of time (LST = UT - 9h) and altitude. The concentrations have been low pass filtered with Parzen filters having cut-offs of 1 km and 2 h. The contour levels are 100 cm^{-3} , 250 cm^{-3} , 500 cm^{-3} , ... 4750 cm⁻³. The two vertical lines mark when the rocket-borne ionization gauges made their measurements.

MIL varies between 13.2 and 27.2 K, with an average value of 20.8 km. The MIL has maximum amplitude at 02:04 LST corresponding to the 2-h profile in Fig. 1. The uncertainties in the amplitude vary between 5.3 and 8.0 K with an average value of 6.4 K. The MIL lapse rate varies between 5.2 and 9.5 K km^{-1} , with an average value of 7.7 K km^{-1} . We summarize the evolution of the MIL as follows; the MIL forms over a period of an hour, and reaches a maximum amplitude with near adiabatic lapse rate an altitude of 74.2 km where it remains for over an hour (01:04–02:04 LST). The MIL then weakens and descends, before strengthening again at 71.4 km.

From Fig. 2, we see that our estimates of the MIL characteristics are robust and relatively insensitive to change in initial temperature (-25 K, -10 K, +10 K, and +25 K). In general the MIL characteristics are most sensitive to initial temperature when the amplitude of the MIL is smaller. At 00:34 we see that the estimates of the MIL amplitude and lapse rate vary most significantly. The robustness of these observations is due to the large amplitude of the MIL.

3.2 Mesospheric sodium layer

We determine the sodium concentration profiles over successive 15 min intervals at 75 m resolution and then low-pass filter the profiles at 1 km and 2 h with a Parzen filter. We plot the filtered sodium concentration in false color as a function of altitude and time in Fig. 3. The variations in the structure of the sodium layer are typical of those observed at Chatanika. The peak of the layer varies between an altitude of 82.7 and 89.4 km with an average value of 86.5 km and a concentration of 3.3×10^3 cm⁻³ and 5.0×10^3 cm⁻³



Fig. 4. Sodium concentration profile measured by resonance lidar at Chatanika, Alaska on the night of 17–18 February 2009. The nightly average sodium concentration measured over the interval 20:35–06:00 LST (05:35–15:00 UT, thick dashed line) and the sodium profile measured over the 15 min interval centered at 02:00 LST (11:00 UT, thin solid line) are plotted. The profiles are smoothed with a 1 km Parzen filter.

with an average value of 4.2×10^3 cm⁻³. The structure of the sodium layer can be characterized by the column abundance, centroid height, and rms width (Gardner et al., 1986). The column abundance varies between $4.7 \times 10^9 \text{ cm}^{-2}$ and 6.4×10^9 cm⁻² with an average value of 5.6×10^9 cm⁻². The centroid height varies between 87.8 km and 89.3 km with an average value of 88.8 km. The rms width varies between 5.1 km and 5.7 km, with an average value of 5.4 km. We plot the average sodium layer profile for the observation period in Fig. 4. The peak of the sodium layer was at 86.1 km and the peak concentration was 4.0×10^3 cm⁻³. While the column abundance, centroid height, and rms width describe the shape of the sodium layer in terms of a single Gaussian profile, the sodium layer is asymmetric about the peak. The topside-bottomside asymmetry of the layer is evident from the narrower spacing of the contours on the bottomside than the topside of the layer. The topside scale height was 3.7 km while the bottomside scale height was 2.3 km and the topside rms width is 6.9 km while the bottomside rms width is 3.7 km.

The sodium layer shows coherent oscillations with downward phase progressions that are most pronounced on the bottomside of the layer. These oscillations reflect the passage of upwardly propagating waves through the layer. These sodium oscillations have a period of 3.5 h with a vertical phase progression that indicates a vertical wavelength of 24 km. The amplitude of the oscillations is 0.9 km. There are oscillations of similar period in the relative density fluctuations derived from the Rayleigh lidar observations. The sodium layer also shows overturning in sodium concentrations (e.g., ~81 km at 21:00 LST), consistent with the passage of large amplitude and/or breaking gravity waves (e.g.,



Fig. 5. Characteristics of bottomside of the sodium layer as a function of time (LST = UT - 9h) measured by resonance lidar at Chatanika, Alaska on the night of 17–18 February 2009. The sodium concentration averaged over the 76–77 km altitude range (dashed line with open circle) and the sodium scale height over the 75–78 km altitude range (solid line with full circle) are plotted.

Hecht et al., 1997, 2000; Collins and Smith, 2004; Xu et al., 2006).

Of particular interest is the spreading of the sodium layer on the bottomside that (serendipitously) coincides with the rocket-borne measurements when the $100 \,\mathrm{cm}^{-3}$ contour appears below 76 km from 00:30 LST until 02:15 LST with a minimum altitude of 74.1 km at 02:00 LST and 02:15 LST. This behavior is evident in Figs. 3 and 4. In Fig. 3 the altitude separation of the 100 cm^{-3} and 250 cm^{-3} contours has a median value of 0.9 km and reaches a maximum value of 4.4 km at 02:00 LST. This extension of the sodium layer below 78 km is clearly seen in the profile at 02:00 LST relative to the average profile in Fig. 4. In Fig. 5 we plot average sodium concentration and the bottomside scale height as functions of time. The average sodium concentration over the 76-77 km altitude range reaches a maximum value of $279 \, \text{cm}^{-3}$ at 01:00 LST considerably larger than the local maxima of 110 cm^{-3} at 20:45 LST and 84 cm⁻³ at 04:30 LST. The bottomside scale height over a 3 km altitude range centered on the 184 cm^{-3} sodium contour (at 76.5 km at 02:00 LST) has typical values of about 1 km when the 100 cm^{-3} sodium contour is above 76 km. At 02:00 LST we find a bottomside scale height of 15.2 ± 1.4 km over the 75–78 km altitude range.

4 Analysis

4.1 Motivation

Based on the key observations (i.e., (i) appearance of a MIL with near-adiabatic lapse rate on the bottomside of the sodium layer, and (ii) simultaneous spreading of the sodium layer to unusually low altitudes) we analyze the observations in terms of wave-breaking, instability, and eddy diffusion to estimate the eddy diffusivity associated with the MIL. To illustrate our approach we plot the trajectory of the peak of



Fig. 6. Altitude of sodium concentration contours (alternate solid and dashed lines) and mesospheric inversion layer peak (solid line with closed square) as a function of time measured by resonance and Rayleigh lidars respectively at Chatanika, Alaska on the night of 17–18 February 2009. The sodium concentration contours are labeled in cm^{-3} .

the MIL and bottomside sodium contours in Fig. 6. The MIL forms and appears to entrain the sodium on the bottomside of the sodium layer and moves downward. The maximum spreading of the sodium layer between 01:00 LST and 02:00 LST coincides with the MIL having largest amplitude and largest topside lapse rate (i.e., being strongest), and, we assume, the largest eddy diffusion (see Fig. 2). As the MIL weakens after 02:00 LST the diffusive transport weakens and the sodium disappears. When the MIL strengthens after 04:00 LST it does so at lower altitudes and does not appear to entrain the sodium. We note that the spreading of the sodium layer is evident between the $250 \,\mathrm{cm}^{-3}$ and $500 \,\mathrm{cm}^{-3}$ contour after 00:00 LST and appears to move downward, indicating that wave breaking may begin at that time and move downward following the phase progression of a gravity wave or tide before the MIL is fully detected by the Rayleigh lidar.

Our analytic approach is guided by observational and modeling studies of MILs. Whiteway and co-workers performed ongoing soundings of the mesosphere with Rayleigh lidar, and found that MILs were often associated with near adiabatic lapse rates on their topsides (Whiteway et al., 1995). Whiteway and coworkers used a one-dimensional model to show that these observations were consistent with the presence of a well-mixed turbulent layer. Lehmacher and coworkers have reported ionization gauge measurements of enhanced turbulence in layers with near-adiabatic and superadiabatic lapse rates in the upper mesosphere (Lehmacher and Lübken, 1995; Lehmacher et al., 2006). Thomas and coworkers performed wintertime soundings of the mesosphere with Rayleigh lidar and VHF radar and found that the presence of MILs coincided with the presence of enhanced radar scattering and concluded that the presence of the MILs coincided with instabilities and turbulence (Thomas et al., 1996). Liu and coworkers have conducted a series of numerical experiments to show that interactions between tides and gravity waves could result in gravity-wave breaking and the formation of a MIL (Liu and Hagan, 1998; Liu et al., 2000; Liu and Meriwether, 2004). Salby and co-workers used lidar and satellite observations and models to show that the formation of MILs was consistent with breaking planetary waves (Salby et al., 2002). Meriwether and Gerrard (2004) have identified two subtypes of MILs. One type of MIL is found at higher altitudes (\sim 85 km and above) and are formed through interactions of gravity waves with large amplitude tidal waves. A second type of MIL is found at lower altitudes and are formed by dissipating planetary waves. In this study we analyze the lidar observations in terms of vertical transport of a chemically active tracer to estimate the eddy diffusion associated with the MIL. While we expect that the MIL at 74 km is formed by planetary waves, we do not attempt to directly determine the mechanism underlying the formation of the MIL (i.e., planetary-wave breaking or gravity-wave breaking).

From Figs. 3 and 5 we see that the sodium on the bottomside of the sodium layer disappears on the scale of tens of minutes. This is considerably longer than the chemical time constants that are calculated for the sodium layer (e.g., Xu and Smith, 2003). Xu and Smith conducted an eigenvector-eigenvalue analysis of chemical timescales in the mesospheric sodium layer following the approach used by Prather (1994) in studying methane and in control theory since the 1960s (Gilbert, 1963). We have confirmed this behavior in the bottomside of the sodium layer using temperature and concentration profiles from the Thermosphere-Ionosphere-Mesosphere-Electrodynamics General Circulation Model (Roble and Ridley, 1994) and a sodium layer model (Plane et al., 1998). In mixing the atmosphere over several kilometers (e.g., between 75 and 78 km) the atomic sodium converges to the new mixed equilibrium in seconds. The longer sodium lifetime reflects the equilibrium of atomic sodium with other sodium species and background species (e.g., atomic oxygen, ozone, etc.) as they evolve. Liu et al. (2000) modeled the evolution of atomic oxygen associated with the formation of a MIL and show features lasting several hours. Thus the atomic sodium remains in a fast equilibrium with the more slowly evolving background species and eventually disappears as these species disappear.

4.2 Estimation of eddy diffusion coefficient

We determine the value of the eddy diffusion coefficient following the analysis by Hunten of vertical transport in the atmosphere (Hunten, 1975). Ignoring vertical velocity and molecular diffusion, we can express the vertical flux of a minor constituent, ϕ , as,

$$\phi = -K \times n_{\rm a} \times \frac{df}{dz} \tag{1}$$

where *K* is the eddy diffusion coefficient, n_a is the concentration of the background atmosphere, and $f(=n/n_a)$ is the mixing ratio of the tracer, *n*. The sodium lidar provides measurements of *n*, while the Rayleigh lidar provides measurements of the relative concentration of the background atmosphere, r_a , which can be normalized to 1 at the altitude of interest. Thus the expression for the vertical flux becomes,

$$\phi = -K \times \left[\frac{dn}{dz} - n\frac{dr_{a}}{dz}\right] \tag{2}$$

Using the scale height of a tracer with concentration increasing with height, H, and the background atmosphere with concentration decreasing with height, H_a , we can express the flux in terms of the scale heights as,

$$\phi = -K \times n \times \left[\frac{1}{H} + \frac{1}{H_{a}}\right] \tag{3}$$

Following Hunten, we estimate ϕ by assuming that during the disappearance of the sodium, the diffusion is suppressed and the observed loss rate is the chemical loss rate. Thus when the turbulence is fully formed, and the sodium has the largest scale height (02:00 LST), the downward vertical flux rate balances the chemical loss rate, and we can express the flux gradient as,

$$\frac{d\phi}{dz} = -\frac{n}{\tau} \tag{4}$$

where τ is the loss time constant. Following Whiteway et al. (1995), we assume a single slab of uniform turbulence over layer thickness, *L*, and integrate Eq. (4) to yield the flux as,

$$\phi = -\frac{n}{\tau} \times L \tag{5}$$

Finally we determine K from Eqs. (3) and (5) as,

$$K = \frac{L}{\tau} \times H_{\rm eff} \tag{6}$$

where the effective scale height, $H_{\rm eff}$, is,

$$\frac{1}{H_{\rm eff}} = \frac{1}{H} + \frac{1}{H_{\rm a}}.$$
(7)

Given our earlier analysis we calculate the sodium scale height, H, over the 75–78 km altitude region (Fig. 5). We calculate the atmospheric scale height, H_a , over the 75– 78 km range from the Rayleigh lidar atmospheric density profile used to determine the temperature at 02:04 LST. We take the average sodium concentration, n, over the 76–77 km altitude range at 02:00 LST (Fig. 5). We calculate the loss time constant, τ , from the disappearance of sodium over the 76–77 km altitude range (Fig. 5). We tabulate these values in Table 1. Using a value of layer thickness, L, of 1000 m, we estimate an eddy diffusivity of 1.8×10^3 m² s⁻¹ and a downward sodium eddy flux of 5.6×10^7 (atoms m⁻²) s⁻¹. We

Table 1. Measured quantities based on lidar observations of MIL and sodium layer on 17-18 February 2009 at Chatanika (65° N, 147° W).

Measured quantities	Altitude	Value
Atmospheric scale height, H_a	75–78 km	$9.5 \pm 0.1 \text{km}$
Sodium scale height, H	75–78 km	$15.2 \pm 1.4 \text{km}$
Sodium time constant, τ	76–77 km	55 ± 7 min
Sodium concentration, n	76–77 km	$186 {\rm cm}^{-3}$
Temperature, T	76–77 km	$234\pm 6\mathrm{K}$
Lapse rate, γ	74.5–77.5 km	$9.4\pm0.3{ m Kkm^{-1}}$

tabulate these values in Table 2 with a range determined from the uncertainty in the measurements reported in Table 1.

However, our analysis assumes that the observed lifetime of the sodium represents the chemical loss rate. This analysis is only correct if the atmosphere is at rest. The measured lifetime may be significantly shorter than the true lifetime of the layer due to advection. For a layer with horizontal scale length, L_h , and a vertical scale height, H_v , in the presence of winds with horizontal velocity V_h , and vertical velocity V_v , the observed lifetime, τ_{obs} , is related to the true lifetime, τ , as,

$$\frac{1}{\tau_{\rm obs}} = \frac{1}{\tau} \pm \frac{1}{\tau_{\rm h}} \pm \frac{1}{\tau_{\rm v}} \tag{8}$$

where τ_h (= L_h/V_h) and τ_h (= H_v/V_v) are the horizontal and vertical advection timescales respectively. Clearly the observed lifetime can be significantly greater or less than the true lifetime, and from Eq. (6) can yield an estimate of the eddy diffusion coefficient that is significantly biased. We estimate the true lifetime by considering the winds and sodium scale lengths and sizes. The luminous vapor trails released by the rocket yield horizontal wind measurements from 85 to 130 km (Lehmacher et al., 2011). The wind speeds near 85 km are approximately $50 \,\mathrm{m \, s^{-1}}$. We assume wind speeds of $50 \,\mathrm{m\,s^{-1}}$ at the altitude of the MIL (76– 77 km) and a horizontal scale length for the sodium enhancement of 250 km. The 3.5 h oscillation of amplitude $0.9 \,\mathrm{km}$ suggests vertical winds of amplitude $0.44 \,\mathrm{m \, s^{-1}}$ associated with a gravity wave. Analysis of gravity waves in the sodium layer indicate that the sodium displacement oscillations are ~ 25 % larger than the wave displacement perturbations and so we use this value as representative of the gravity wave winds (Collins and Smith, 2004). The amplitude of the wave (0.9 km) is less than the altitude spreading of the sodium (3 km). The measured sodium scale height is 15.2 km. Thus the horizontal advection timescale is 83 min and the vertical advection timescale is 576 min. We used these timescales to calculate a value of the true lifetime between 31 and 225 min. Thus the value of the eddy diffusivity may be as low as $4.3 \times 10^2 \, \text{m}^2 \, \text{s}^{-1}$ and a downward sodium flux of 1.4×10^7 (atoms m⁻²) s⁻¹). We adopt these lower estimates of the eddy diffusivity and sodium flux as conservative estimates of the eddy diffusion and flux associated with the MIL.

4.3 Estimation of eddy dissipation rate

Following Weinstock (1978) we relate the eddy diffusion coefficient, K, and the energy dissipation rate, ε , as,

$$\varepsilon = \frac{1}{0.81} \times \left(N^2 \times K \right) \tag{9}$$

where N is the Brunt-Väisälä frequency. We calculate the Brunt-Väisälä frequency as,

$$N^2 = \frac{g}{T} \times (\Gamma - \gamma) \tag{10}$$

where g is the gravitational constant (9.6 m s⁻²), T is the temperature, Γ is the adiabatic lapse rate (9.5 K km⁻¹), and γ is the lapse rate. Using the values in Tables 1 and 2, we estimate a value of the square of the Brunt-Väisälä frequency of 4.1×10^{-6} s⁻² (corresponding to a buoyancy period of 52 min) and an energy dissipation rate of 2.2 mW kg⁻¹. The uncertainty in the measured near-adiabatic lapse rate results in a large uncertainty in the square of the Brunt-Väisälä frequency (0–17 × 10⁻⁶ s⁻²) and contributes to the large uncertainty in the estimated eddy dissipation rate (0–11 mW kg⁻¹).

5 Discussion

5.1 General structure of stratosphere and mesosphere

The difference between the temperature profile measured by the Rayleigh lidar and the SPARC atlas reflected a disturbance of the Arctic middle atmosphere in February 2009. Thurairajah and co-workers have analyzed lidar measurements from Chatanika, high latitude satellite measurements, and meteorological analyses in recent Arctic winters (Thurairajah et al., 2010a, b). During several of these winters they report significant differences between nightly and monthly averaged temperature profiles measured by Rayleigh lidars at Arctic locations. These differences are due to the occurrence of sudden stratospheric warmings (SSW) when the zonal winds are reversed, latitudinal temperature gradients are reversed, the stratospheric vortex is disrupted (and occasionally split in two), the lower stratosphere warms while the upper stratosphere and mesosphere cools, and an elevated stratopause may form. In spring 2009 there was a major SSW in the third week of January that resulted in a splitting of the polar vortex. The vortex remained split for almost three weeks when the upper stratospheric vortex recovered with colder temperatures. By the second week of February the upper stratospheric vortex had completely recovered and strengthened while the mid- and lower stratospheric vortex remained weak. The temperature inside the

 $0-11 \,\mathrm{mW \, kg^{-1}}$

Derived eddy quantities	Value	Range
Effective scale height, $H_{\rm eff}$	5.8 km	5.6–6.1 km
Square of Brunt-Väisälä frequency, N^2	$4.1 \times 10^{-6} \mathrm{s}^{-2}$	$0-17 \times 10^{-6} \mathrm{s}^{-2}$
Eddy diffusion coefficient ^a , K	$1.8 \times 10^3 \mathrm{m^2 s^{-1}}$	$1.5-2.1 \times 10^3 \text{ m}^2 \text{ s}^{-1}$
Eddy sodium flux ^a , ϕ	$5.6 \times 10^7 \text{ (atoms m}^{-2}\text{) s}^{-1}$	$5.0-6.5 \times 10^7 \text{ (atoms m}^{-2}\text{) s}^{-1}$
Eddy diffusion coefficient ^b , K	$4.3 \times 10^2 \mathrm{m^2 s^{-1}}$	$3.7-5.2 \times 10^2 \text{ m}^2 \text{ s}^{-1}$
Eddy sodium flux ^b , ϕ	1.4×10^7 (atoms m ⁻²) s ⁻¹	$1.2-1.6 \times 10^7$ (atoms m ⁻²) s ⁻¹

 $2.2 \,\mathrm{mW \, kg^{-1}}$

Table 2. Derived eddy diffusion quantities based on lidar observations of MIL and sodium layer on 17–18 February 2009 at Chatanika (65° N, 147° W).

^a Under assumption of zero wind; ^b under assumption of nonzero winds

Energy dissipation rate^b, ε

Table 3. Measured eddy dissipation rates and diffusion coefficients in the upper mesosphere and lower thermosphere.

Reference	Altitude (km)	Eddy dissipation rate, ε (mW kg ⁻¹)	Square of Brunt-Väisälä frequency, N^2 (×10 ⁻⁵ s ⁻²)	Eddy diffusion coefficient, $K (m^2 s^{-1})$
Lehmacher and Lübken (1995) ^a	75–78 km	10	0–25	>32
Lübken (1997) ^b	76–77 km	1.3-1.8	31–35	3.4-4.2
Bishop et al. (2004) ^a	85–87 km	31-140	7.6–76	33-1500
Lehmacher et al. (2006) ^a	92–96 km	170	8.0	1700

^a Single rocket-borne measurement; ^b seasonal averages of 12 rocket-borne measurements

vortex was anomalously cold and lead to the formation of an elevated stratopause in February 2009. The formation of the elevated stratopause has been documented in zonal mean temperature measurements at 70° N (Manney et al., 2009). The lower stratospheric vortex remained weak through the end of March 2009.

Despite the disturbed condition of the stratosphere and lower mesosphere, the structure of the mesospheric sodium layer on the night of 17–18 February 2009 was typical for this time of year at Chatanika as reported by Collins and Smith (2004) and as confirmed by both ongoing measurements at Chatanika and measurements made during February 2009 in support of the Turbopause experiment. The values of the sodium layer parameters and the asymmetry of the layer were consistent our understanding of the chemical equilibrium of the sodium layer (e.g., Plane, 2004), and with the latitudinal variation of the sodium layer that have been reported from other sites around the world (e.g., Yi et al., 2009).

5.2 Eddy diffusion and dissipation

The observations in this study have allowed us analyze turbulence in the upper mesosphere by first determining the eddy diffusion coefficient and then determining the eddy dissipation rate. Experiments that employ spectral analysis of small-scale high-frequency density fluctuations, expansion of luminous vapor trails use analyses that determine the eddy dissipation rate (Lehmacher and Lübken, 1995; Lübken, 1997; Bishop et al., 2004; Lehmacher et al., 2006). Several of these researchers then use measurements of the Brunt-Väisälä frequency and employ the relationship of Weinstock (1978) to determine the value of the eddy diffusion coefficient (Lübken, 1997; Bishop et al., 2004). We summarize these measurements in Table 3. Where the Brunt-Väisälä has not been explicitly presented we have determined it from the data reported in the paper. All these observational studies assume that the observed turbulence is homogeneous and forms in a uniformly stratified fluid. The values reported by Lübken (1997) represent an average of 12 rocket-borne measurements where the individual values of the eddy dissipation rate vary between 0.3 and 10 mW kg^{-1} . The other studies represent values from individual rocket-borne measurements. The measurements by Lehmacher and Lübken (1995) and Bishop et al. (2004) show values that vary by several orders of magnitude over height changes of 1 km indicating strong layering of the turbulence and/or the Brunt-Väisälä frequency. The lidar-based measurement of the eddy diffusion coefficient is in the range of values reported by the single rocket-borne measurements while the value of the dissipation rate is lower. These differences may reflect differences in the turbulence generation mechanisms observed in the different experiments. In high-resolution numerical simulations of turbulence generation by gravity-wave breaking and shear instability, Fritts and coworkers have shown differences in the how the turbulence effects are localized (Fritts et al., 2003). While these simulations do not directly address the conditions observed in this study, they highlight the fact that the characteristics of turbulence observed in the atmosphere varied considerably with the processes that cause the turbulence. The lidar measurements in the Turbopause experiment are made in the presence of a mature MIL where the lapse rates are similar to those reported by Lehmacher and Lübken (1995) and persist for several hours. Bishop et al. (2004) suggest that their measurements of large eddy diffusion coefficient reflect the role of large vortices generated by tides in creating vortex role instabilities. Similarly the measurements of Lehmacher et al. (2006) of large dissipation rates above 90 km may represent the generation of turbulence associated with interaction between large amplitude gravity-waves and/or tides associated with the formation of a high altitude MIL (Meriwether and Gerrard, 2004).

6 Summary and conclusions

Simultaneous Rayleigh and resonance lidar measurements made during the Turbopause experiment have allowed us conduct a detailed investigation of a MIL that formed near the lower edge of the sodium layer. The lidar experiments differed from previous experiments at Chatanika in two distinct ways; the Rayleigh lidar incorporated simultaneous rocket-borne temperature measurements in the upper mesosphere to yield more accurate temperature measurements above 60 km, the resonance lidar incorporated a larger telescope than previously used to allow more precise measurements of the sodium layer.

The thermal structure of the stratosphere and mesosphere is disrupted during a major stratospheric warming that resulted in disruption of the stratospheric vortex with a cold stratopause present throughout February 2009. The general structure of the mesospheric sodium layer is typical of that observed at Chatanika in February.

However, the observations also revealed the downward transport of sodium to unusually low altitudes coinciding with the presence of a MIL. The MIL had large amplitude, near adiabatic lapse rate, and was present for over 6h. The formation and downward motion of the MIL was accompanied by the extension of the sodium layer to unusually low latitudes over a 2-3 h period. The sodium appears to have been entrained in the MIL. Using simple continuity arguments we have modeled the vertical motion of the sodium as due to downward diffusion in the presence of the MIL. Even allowing for the presence of strong winds, our analysis yields an estimate of the eddy diffusion coefficient $(430 \text{ m}^2 \text{ s}^{-1})$ that is significantly larger that that reported for mean wintertime values by Lübken (1997). Our estimates of the eddy diffusion coefficient are similar to values found in a superadiabatic layer near 75 km (Lehmacher and Lübken, 1995) and in a region of static instability near 85 km (Bishop et al., 2004). Our estimate of a relatively low value of the corresponding eddy dissipation rate (2.2 mW kg^{-1}) reflects the presence of a near adiabatic lapse and low value of the Brunt-Väisälä frequency.

Our observations and analysis, based on naturally occurring variations in mesospheric temperatures and the sodium layer (rather than artificial releases or measurement of smallscale density fluctuations), confirm that there is significant eddy diffusion associated with convectively unstable regions of MILs in the upper mesosphere.

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