

Theoretical simulation of O^+ and H^+ densities in the Indian low latitude F-region and comparison with observations

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Abstract. The O⁺ and H⁺ ion density distributions in the Indian low latitude F-region, within $\pm 15^{\circ}$ magnetic latitudes, are simulated using a time dependent model developed on the basis of solution of the plasma continuity equation. The simulated ion densities for solar minimum June and December solstices are then compared with ionosonde observations from the period 1959-1979 and measurements made by the Indian SROSS C2 satellite during 1995–1996 at an altitude of \sim 500 km. The simulated O⁺ density has a minimum around pre-sunrise hours and a maximum during noontime. H⁺ density is higher at nighttime and lower during the day. The simulations reproduced the well-known equatorial ionization anomaly (EIA) observed in electron density at the peak of the F2-region in the Indian low latitude sector during solar minimum. In situ measurement of O⁺ density by the SROSS C2, however, showed a single peak of ionization around the equator.

Key words. Ionosphere (equatorial ionosphere; modeling and forecasting)

1 Introduction

The distribution of plasma in the ionospheric F-region depends on the three processes of production, loss and transport. At equatorial and low latitudes, the F-region is characterized by a depression in ionization densities at the magnetic equator and two maxima on either side of the equator. Besides this well-known phenomenon of equatorial ionization anomaly (EIA), the equatorial ionosphere is known to exhibit some unique features such as the equatorial electrojet, the spread-F, etc. The horizontal orientation of the geomagnetic field lines at the equator and the shift between the geographic and geomagnetic equator are known to be the main reasons for observation of these features and their longitudinal variation. Martyn (1947) put forward the explanation that the E-region eastward electric field at the equator causes

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the F-region plasma to drift upward during the daytime. As the plasma is lifted to greater heights, it diffuses downward along geomagnetic field lines under the twin action of gravity and pressure gradients (Hanson and Moffett, 1966). A plasma fountain thus forms which moves ionization from the equator to the two anomaly crests. After sunset, the electric field reverses in direction and the F-region plasma drifts downward. The fountain reverses and the crests disappear. The location of the two anomaly peaks shifts towards higher latitudes with increase in $E \times B$ drift velocity. Asymmetric neutral winds about the equator produce a north south asymmetry in the EIA. The latitudinal extent of the crests also varies with solar and magnetic activity. The fountain rises to several hundred kilometers at the equator and the crests become weaker with increase in altitudes. At higher altitudes, a single crest of ionization forms over the equator (Su et al., 1995; Balan and Bailey, 1995). Rishbeth (1977), Rajaram (1977), Moffett (1979), Anderson (1981) and Stening (1992) have reviewed the characteristics of the equatorial ionization anomaly and associated physical processes.

Many attempts have been made in the past to theoretically investigate the dynamics of the low latitude ionosphere. Empirical models such as that of Bradley and Dudeney (1973) and the International Reference Ionosphere (Bilitza, 1990) are useful in describing the "climatology" of the ionospheric regions and their average behavior. Rush (1986) discussed the various kinds of empirical models and how they can be used to make prediction of radio propagation conditions. But empirical models fail to provide any insight into the ionospheric processes which govern the day-to-day, solar, magnetic and seasonal variability of ionospheric parameters. On the other hand, theoretical models being sensitive to choice of input parameters can be used to investigate the effect of changes in solar or particle production rates, neutral winds or $E \times B$ drifts or variations in neutral atmospheric constituents. Bramley and Peart (1965), Hanson and Moffett (1966) and Bramley and Young (1968) solved the time independent plasma continuity equation to study the formation of the EIA. Baxter and Kendall (1968) qualitatively explained

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the daily variation of the EIA by solving a time dependent continuity equation. Sterling et al. (1969) studied the effect of neutral winds in maintaining the night-time low latitude F2-region plasma densities and that of $E \times B$ drift velocity on the position of the anomaly peaks. Anderson (1973 a, b) and Chan and Walker (1984 a, b) derived theoretical models to investigate the EIA structure in the American and East Pacific sectors. Bailey and Balan (1996) and Bailey et al. (1997) described the Sheffield University Plasmasphere Ionosphere model (SUPIM) in which time dependent equations of continuity, momentum and energy balance are solved along closed field lines to calculate the electron and ion densities and temperatures at middle and low latitudes. It has been shown that the equatorial plasma fountain is confined to a particular region in altitude and latitude and outside this region plasma flows towards the equator from both hemispheres. The upward flow of plasma outside the fountain region can cause convergence of plasma above the F-region peak close to the equator leading to the formation of an additional layer F3. Using the SUPIM, Balan et al. (1997a) have found that the north-south asymmetries of the equatorial plasma fountain and equatorial anomaly are more dependent upon the displacement of the geomagnetic equator from the geographic equator. Watanabe et al. (1995a) had used a time dependent three-dimensional simulation procedure to study the variation of electron and ion temperature and density within $\pm 30^{\circ}$ and 200 km to 1000 km altitude region. Their results show that the structure of the equatorial ionospheric F-region is strongly affected by the plasma drift which is induced by the ionospheric electric field, neutral wind, exospheric temperature and intensity of solar flux variations. Balan et al. (1997b) theoretically described a plasma temperature anomaly in the equatorial topside ionosphere. Bhuyan and Kakoty (2001a, b) have recently simulated the ion density distribution in the topside F-region of the Indian low latitude ionosphere for solar minimum equinoctial conditions and compared the results with the density measurements made by the Indian SROSS C2 satellite.

In this study, the results of the simulation of O^+ and H^+ density distribution in the low latitude F-region during low solar activity June and December solstices are presented. The model results are then compared with foF2 measurements from 1959–1979 and ion density measured by the SROSS C2 during 1995–1996.

2 Simulation

The ion density in the equatorial ionosphere is simulated by solving the ion continuity equation

$$\frac{\partial N}{\partial t} = P - L - \nabla . (NV) \tag{1}$$

by following the procedure adopted by Bhuyan and Kakoty (2001 a, b). In Eq. (1), N is the ion (electron) density, P and L are the ion production and ion loss rates, respectively and V is the ion transport velocity. Equation (1) is solved

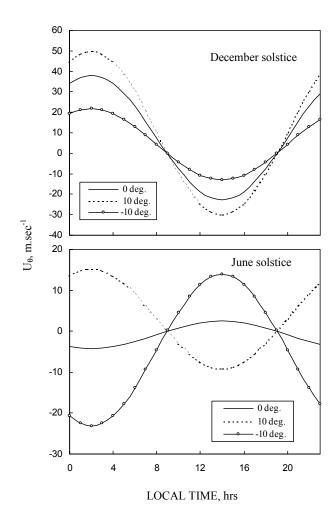


Fig. 1. Diurnal variation of neutral wind velocity for December (top) and June solstice (bottom) at three fixed geomagnetic latitudes.

numerically for ${\rm O}^+$ and ${\rm H}^+$ ions along closed magnetic field lines around the equator under the influence of $E\times B$ drift and neutral winds. The production of ${\rm O}^+$ is assumed to be caused entirely by x.u.v. (extreme ultraviolett) solar radiation (Anderson, 1973a) while ${\rm H}^+$ production is due to the resonant charge exchange reaction with oxygen (Stubbe, 1970). The chemical reaction rates are as given by Raitt et al. (1975) whereas the rate coefficients for loss of ${\rm O}^+$ following charge exchange reactions with ${\rm O}_2$ and ${\rm N}_2$ are taken from St Maurice and Torr (1978) and Bailey and Sellek (1990) respectively.

The concentrations of the atmospheric constituents O, O₂, N₂ and H are calculated from the MSIS-86 thermospheric model (Hedin, 1987) as a function of altitude, latitude and local time. The neutral gas temperature (T_n), ion temperature (T_i) and electron temperature (T_e) are chosen from the IRI-90 model (Bilitza, 1990).

The horizontal meridional component U_{θ} is given by (Chauhan and Gurm, 1980)

$$U_{\theta} = U_o \sin(2\theta_g - \delta_o)(\cos(\phi - \phi_o) - \tau), \tag{2}$$

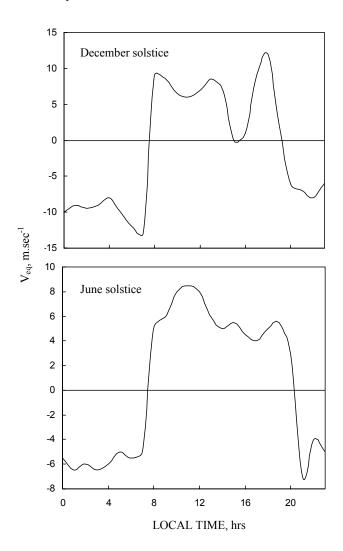


Fig. 2. Local time variation of equatorial vertical $E \times B$ drift velocity in December (top) and June solstice (bottom) over Trivandrum.

where ϕ is the local time (in hour angle), ϕ_o is the local time when the daytime pole-ward neutral wind reaches a maximum, δ_o is the declination of the sun. It is assumed that, U_θ is independent of altitude. The parameter τ is used to produce a diurnal asymmetry in the wind field i.e. the velocity amplitude is larger at night than in the daytime (Fig. 1). This asymmetry is introduced to allow for the fact that the retarding effects of ion drag on the neutral winds are greater during the daytime than that at night.

The $E \times B$ plasma drift velocity has been measured routinely by the incoherent scatter technique at Jicamarca (70° W) and reported extensively in literature (Woodman, 1970: Fejer, 1981). The HF Doppler radar developed at the University of Kerala (Balan et al., 1992) provided systematic measurement of F-region plasma drifts at the equatorial station Trivandrum (77° E, .3° S dip). The drifts have day-to-day, seasonal and solar cycle variation. However, the drift velocities measured by the HF Doppler radar technique are apparent, as the delay caused by the ionization along the traversed path has not been taken into account. Jayachan-

dran et al. (1987) noted that the decay in ionization in the evening hours is unlikely to alter the basic pattern of velocity variation in any significant way. Balan et al. (1992) have shown that the uncertainty due to layer decay in the 15:00–02:00 LST period corresponds to about 0.5 m s⁻¹ under normal conditions and 2–3 m s⁻¹ under spread-F conditions. In our present calculation, the equatorial value of drift velocity, Veq given by Namboothiri et al. (1989) is adopted as shown in Fig. 2 without ionospheric correction. As the present simulations are carried out for the quiet ionosphere, the above mentioned error, less than 5% of the minimum drift velocity at solar minimum, is unlikely to affect the calculated density.

3 SROSS C2 RPA measurements

The Indian satellite SROSS C2 was launched on 4 May 1994, into an orbit of 46° inclination and 930 km apogee with 430 km perigee. In July 1994, the orbit of the satellite was trimmed to 630 km by 430 km. Two Retarding Potential Analyzer (RPA) sensors were placed on board the satellite for in situ measurement of ionospheric electron and ion densities, temperatures and other related parameters of plasma. The "potential probe" is used to estimate the satellite potential with respect to ionospheric plasma. Both the electron and ion RPA sensors, which consist of four grids and a collector electrode, are mechanically identical but provided with different grid voltages suitable for collection of ions and electrons. The charged particles, whose energies are greater than the applied voltage on the retarding grid, pass through various grids and finally reach the collector electrode to cause the sensor current. This current is measured by a sensitive linear electrometer. Thus, by changing the bias voltage on the retarding grid, flux of different energy ranges can be measured. The collector current (1) versus retarding bias voltage (V) generates characteristic curves separately for electrons and ions which are used to derive total ion density (N_i) , ion composition $(O^+, O_2^+, NO^+, H^+, He^+)$, ion temperature (T_i) and electron temperature (T_e) .

In this analysis, we use measured values of ion composition (O⁺ and H⁺) derived from the RPA data collected during the period August 1995–July 1996. The 10.7 cm solar flux, corresponding to the period of observation, varied between 69.6 and 77.5. The average height of the satellite passes was \sim 500 km, which covered the geographic latitude belt of 31° S–34° N and longitude belt of 40° E–100° E.

4 Results

Equation (1) is solved along centered dipole magnetic field lines, from a base altitude of $120 \, \mathrm{km}$ in the northern hemisphere to the same altitude in the southern hemisphere. The plasma associated with a particular field line can move to a different magnetic field line at different altitude under the influence of the $E \times B$ drifts during the course of the simulation. During the solar minimum period under study, the plasma at the base of the ionosphere can reach a height of

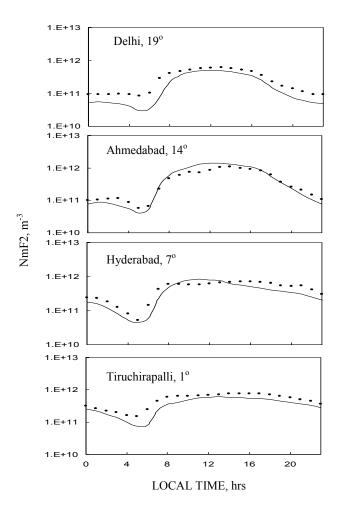


Fig. 3. Measured and simulated *Nm*F2 (shown by dots and solid line, respectively) for selected locations along 75° E meridian. The dots are averages of all data for the December solstice solar minimum conditions during 1959–1979.

700 km within a period of 24 h of simulation. In order to provide reasonable 24 h coverage of the model values within a specified altitude and latitude region, the model equation needs to be solved along many tubes of plasma (Bailey and Balan, 1996). In the present study, 11 field lines have been considered with apex altitude between 200 km and 1600 km. This limits the altitude resolution of the calculations to a few hundred kilometers above the F-region peak. To overcome the problem of the gap created by the drifting plasma at lower altitudes, more points have to be added to the bottom of the flux tube (Millward et al., 1996) or have enough points in the flux. Another way of overcoming this problem is to solve the equations along the lowermost flux tube at different local times (Bailey and Balan, 1996). In the present study, the simulations have been carried out for different local times starting at 06:00 LT with a time increment of 15 min for the next 48 h for the lowermost field line. For other field lines, the simulations are carried out for two diurnal cycles starting at 06:00 LT with equal time increments of 15 min. Thus, a two dimensional grid of points in altitude and latitude is produced for each local time, from which the data at any local time, latitude and height can be recovered taking into consideration the drift of plasma at each time interval. It may also be noted that we have considered the vertical drift to be independent of height. In Fig. 3, NmF2, observed at the low solar activity December solstice during the period 1959– 1979 over Tiruchirapalli, Hyderabad, Ahmedabad and Delhi, are shown with the simulated NmF2 at the respective locations. The simulated values of NmF2 are in good agreement with the measured NmF2 at all the locations. The figure indicates that the model also generates the observed well-known equatorial ionization anomaly (EIA) with its peak around Ahmedabad and trough at the equator. The electron density is considered to be equal to the sum of the O⁺ and H⁺ ion densities. In the ionosphere F-region, it is a good approximation (Watanabe et al., 1995a). Figure 4a shows the simulated and observed diurnal variation of O⁺ for the December solstice (November, December, January and February) at an altitude of 500 km above the geomagnetic equator. The observed density rises in the post-sunrise hours and forms a broad daytime plateau. Diurnal maximum is observed at around 15:00 LT. The afternoon decrease in O⁺ density is slow and secondary post sunset enhancement is absent. The simulated O⁺ density fits well with the observed data except for a few hours in the evening. The theoretical and observed daytime peak values are $\sim 4.8 \times 10^{11} \, \mathrm{m}^{-3}$ and $\sim 3.4 \times 10^{11} \, \mathrm{m}^{-3}$, respectively. The diurnal variation of H⁺ density (Fig. 4b) shows a depression during daytime and higher values at night. In the F-region, below 500 km, the concentration of H⁺ increases with height. It is seen that around 500 km altitude, where the SROSS C2 observations have been made, H⁺ concentration is strongly dependent on the ratio of n(H) to n(O) and the concentration of O^+ . It has also been found that n(H)/n(O) ratio for night-time increases by a factor of 4 or more at 500 km altitude over the equator. Thus, as a result of the increase in the relative magnitudes of the n(H)/n(O) ratio from daytime to night-time and the relative magnitude of O+, the night-time values of H+ are expected to be greater than those during daytime. The observed H⁺ lie close to the model curve ($\sim 5.2 \times 10^9 \,\mathrm{m}^{-3}$) during daytime but are lower ($\sim 4.9 \times 10^9 \,\mathrm{m}^{-3}$) than the simulated density ($\sim 1.1 \times 10^{11} \,\mathrm{m}^{-3}$) at night-time which may be due to a lower rate of increase of the n(H)/n(O) ratio than that used for simulation.

The simulated and observed O⁺ densities at 10° N geomagnetic latitude in the December solstice of low solar activity, are shown in Fig. 5a. There is a gradual increase in O⁺ density in the post sunset hours and daytime maximum is observed at 14:00 LT. The maximum values of simulated and observed O⁺ density are $\sim 2.8 \times 10^{11} \, \mathrm{m}^{-3}$ and $\sim 2.1 \times 10^{11} \, \mathrm{m}^{-3}$, respectively. It is also seen that the theoretical curve remains close to the observed values at most hours. Similarly, the observed and simulated H⁺ density (Fig. 5b) matches fairly well at this latitude; theoretically expected daytime dip and night-time enhancement of H⁺ density are observed. The observed and theoretical H⁺ density ranges from the daytime minimum value of $\sim 1.8 \times 10^9 \, \mathrm{m}^{-3}$

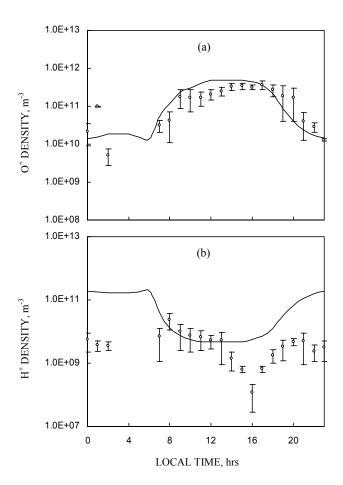


Fig. 4. Diurnal variation of measured (o) and simulated (—-) O^+ density (a) and H^+ density (b) at $\sim 500\,\mathrm{km}$ altitude in the Indian zone over the geomagnetic equator for the December solstice of solar minimum. Bars indicate standard deviation of hourly average data in log scale.

and $\sim 1\times 10^9\,\text{m}^{-3}$ to the night-time maximum value of $\sim 5.7\times 10^9\,\text{m}^{-3}$ and $\sim 3.3\times 10^{10}\,\text{m}{-3}$, respectively.

In Fig. 6a, the observed diurnal variation of O⁺ density, in the June solstice of low solar activity, is shown along with the modeled variation of O⁺ under similar conditions at the geomagnetic equator. The observed O+ density rises from the pre-dawn minimum ($\sim 2.7 \times 10^9 \,\mathrm{m}^{-3}$) to a maximum $(\sim 2.5 \times 10^{11} \,\mathrm{m}^{-3})$ around noon (12:00 LT) after which there is a gradual decrease in density through evening and night. The model simulates the observed O⁺ density well, except for a few hours in the morning. Figure 6b depicts the corresponding observed and simulated H⁺ density variation at the equator. It is seen that both the observed and modeled H⁺ show the expected low values during daytime and high values during the night. The theoretical and observed minimum and maximum H⁺ densities are $\sim 7.9 \times 10^9 \, \text{m}^{-3}$ and $\sim 2 \times 10^9 \,\mathrm{m}^{-3}$ and $\sim 3.5 \times 10^{11} \,\mathrm{m}^{-3}$ and $\sim 7.5 \times 10^{11} \,\mathrm{m}^{-3}$, respectively.

The variation of simulated and observed O^+ density, in the June solstice at 10° N geomagnetic, is shown in Fig. 7a. Diurnal minimum of O^+ ($\sim 7.2 \times 10^9 \,\mathrm{m}^{-3}$) is observed at

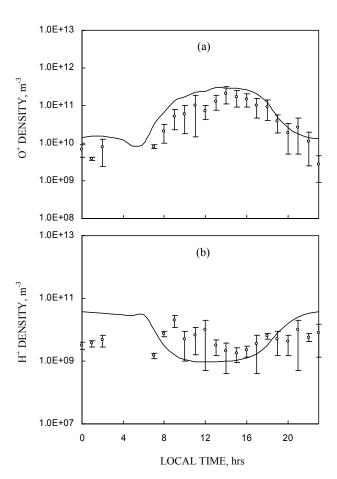


Fig. 5. Same as in Fig. 4 for 10° N geomagnetic latitude.

04:00 LT and the maximum ($\sim 2.7 \times 10^{11} \, \text{m}^{-3}$) at around 13:00 LT. The model fairly simulates the observed density during daytime and evening but gives low values in the presunrise hours. Figure 7b shows the diurnal variation of observed and simulated H⁺ density at 10° N geomagnetic in the same period. The diurnal variation of H⁺ is similar to that at the equator. However, the model predicts slightly lower values than observed in the post noon period. The latitudinal variation of simulated and observed O⁺ density at the altitude of 500 km along the 75° Indian longitude sector in the December solstice is shown in Fig. 8. It may be noted that measured O⁺ density exhibits a broad peak south of the geomagnetic equator while simulations reproduced the EIA with peaks at around $\pm 5^{\circ}$. At other latitudes the simulated and measured O⁺ density is about the same order.

5 Discussion

Modelling of the low latitude ionosphere has been mostly confined to inputs from the American zone. Vertical $E \times B$ drifts used in these models are based on observations for Jicamarca and Arecibo. Neutral wind, used in these models is also based on ground observations in the American zone or satellite observations having minimum coverage of the In-

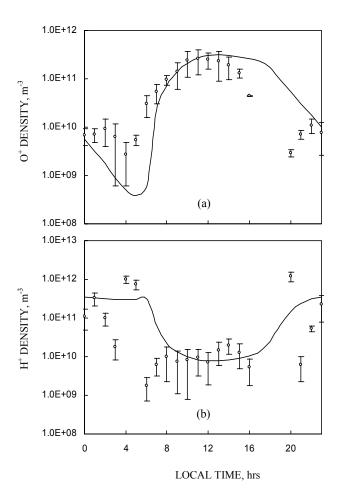


Fig. 6. Local time variation of measured (o) and simulated (—) O^+ density (a) and H^+ density (b) at ~ 500 km altitude in the Indian zone over the geomagnetic equator in the June solstice at solar minimum.

dian low latitude region. Use of any of these models may not be consistent with the dynamical processes prevalent in the Indian low latitude region. For present calculations, vertical drifts measured at Trivandrum have been used. It has been observed that the neutral wind model adopted in the present calculation leads to reasonable agreement of calculated and observed parameters. The simulation of ion densities, during June and December solstices of solar minimum conditions within $\pm 15^{\circ}$ magnetic latitudes in the Indian longitude sector, reproduced the well-known equatorial ionization anomaly at the peak of the F2-layer as seen from measured NmF2. The model calculations also show the presence of the EIA for O⁺, during the December solstice (Fig. 8) within the narrow belt of $\pm 5^{\circ}$ from the geomagnetic equator, whereas the measured O⁺ at the altitude of 500 km in the Indian zone do not exhibit the anomaly. The total electron density (sum of O⁺, O₂⁺, NO⁺, H⁺, He⁺ densities) during the same period also shows that at the altitude of 500 km, the ionization peak in the Southern Hemisphere is higher than that in the Northern Hemisphere in the December solstice. Similarly, in the June solstice a broad peak near the equator in the North-

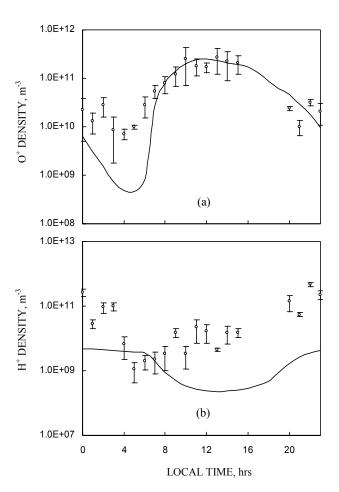


Fig. 7. Same as in Fig. 6 for 10° N geomagnetic latitude.

ern Hemisphere has been observed. The average peak height of the F2-layer, during low solar activity in the Indian zone, is about 350 km where the EIA is seen both for measured and simulated density. The $E \times B$ drift velocity during solar minimum solstices is relatively weak (Fig. 2) compared to that in the corresponding period of high solar activity. Consequently, the plasma fountain fails to reach the altitude required for EIA to be observed at 500 km while producing the effect at the height of peak F2-density. Measurements of electron density made by the Hinotori satellite during 1981-1982, a period of moderate to high solar activity, within $\pm 25^{\circ}$ magnetic latitudes at 600 km (Watanabe et al., 1995b) indicate a broad ionization peak around the equator during daytime in all seasons. Simulations carried out by Watanabe et al. (1995a) show that maximum in ionization starts developing around the equator at $\sim 10:00$ LT and continues until midnight. Balan et al. (1997a), from a study of the equatorial plasma fountain and equatorial ionization anomaly in the ionosphere over Jicamarca (77° E) and Fortaleza (38° W) using the SUPIM model under magnetically quiet equinoctial conditions of high solar activity, have shown that the EIA is evident up to an altitude of 700 km in the three locations. The EIA is asymmetric about the equator in all the three sectors and has been found to be strongly influenced by the asym-

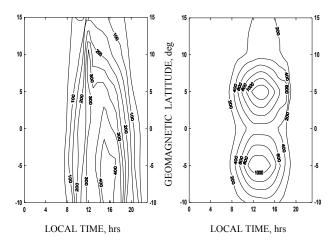


Fig. 8. Latitudinal and local time variation of observed (left panel) and simulated (right panel) $\rm O^+$ density at an altitude of $\sim 500\,\rm km$ within the geomagnetic latitude range from $\rm 10^{\circ}\,S$ to $\rm 15^{\circ}\,N$ during December solstice of low solar activity.

metric neutral winds and displacement of the geographic and geomagnetic equators. The neutral wind model used in the present simulations might be responsible for the discrepancy between observation and simulation as seen in Fig. 8. The SROSS-C2 satellite orbits covered a latitude belt of 3° S–41° N and a longitude belt of 40° E–100° E. The data used for comparison in this study (Figs. 4–7) are the average of all data at the concerned latitude within the covered longitude span of 60°. Therefore, longitudinal variability may be inherent in the data structure, which may partly be responsible for the scatter in the data points for H⁺ and very low O⁺ density during morning hours leading to the disagreement between simulation and observation.

6 Conclusion

The diurnal and seasonal variation of O⁺ and H⁺ densities measured by the SROSS C2 satellite over Indian equatorial and low latitudes at an altitude of 500 km during the low solar activity period of 1995-1996, are simulated by using a time dependent model based on the solution of the plasma continuity equation. The simulated densities are compared with satellite observations for the June and December solstices and with NmF2 measured during the period 1959–1979. Results show that O⁺ density is minimum in the pre-sunrise hours and maximum during noontime. H⁺ density exhibits the opposite diurnal behaviour of high values at night and low values during the day. The O⁺ density peaks early (\sim 12:00 LT) in the June solstice and late (\sim 14:00 LT) in the December solstice. Simulated and measured NmF2 exhibits the equatorial ionization anomaly. But measured O⁺ density does not show the EIA either in June or December solstice at the altitude of 500 km. The effect of a weak $E \times B$ drift in the solstices of low solar activity may be the reason for nonobservance of the EIA in O⁺, which is the major ion at this altitude. Further studies need to be carried out to investigate this point.

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